## Sablefish Growth <br> Katy B. Echave, AFSC/ABL



## Background

"Consider including time-varying or cohortspecific maturity curves, and/or weight-at-age relationships if supported by data."
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## Background

- Last update to growth in the assessment was in 2008 (Hanselman et al. 2007)
- Updated growth information was divided into 2 time periods based on a change in sampling design: 1981-1993 and 1996-2004

| Parameter name | Value | Source |
| :---: | :---: | :---: |
| Time period | 1960-1995 1996-current |  |
| Maturity-at-length - females | $m_{a}=1 /\left(1+e^{-0.4 *(L-65)}\right)$ | Sasaki (1985) |
| Maturity-at-length - males | $m_{a}=1 /\left(1+e^{-0.4 *(L-57)}\right)$ | Sasaki (1985) |
| Maturity-at-age - females | $m_{a}=1 /\left(1+e^{-0.84^{*}(a-6.60}\right)$ | Sasaki (1985) |
| Length-at-age - females | $\bar{L}_{a}=75.6\left(1-e^{-0.208(a+3.63)}\right) \quad \bar{L}_{a}=80.2\left(1-e^{-0.222(a+1.95)}\right)$ | Hanselman et al. (2007) |
| Length-at-age - males | $\bar{L}_{a}=65.3\left(1-e^{-0.277(a+4.97)}\right) \quad \bar{L}_{a}=67.8\left(1-e^{-0.290(a+227)}\right)$ | Hanselman et al. (2007) |
| Weight-at-age - females | $\ln \hat{W}_{a}=\ln (5.47)+3.02 \ln \left(1-e^{-0.238(a+1.39)}\right)$ | Hanselman et al. <br> (2007) |
| Weight-at-age - males | $\ln \hat{W}_{a}=\ln (3.16)+2.96 \ln \left(1-e^{-0.356(a+1.13)}\right)$ | Hanselman et al. (2007) |

- Several above avg. year classes (density dependence?) and warming conditions have occurred since last update of growth


## Objectives

>Have there been temporal changes in sablefish growth?
>If so, are they significant and should they be accounted for in the assessment?


## Temporal Change: Annual LVB growth curves

1. Fit to randomly collected age-weight-length data from 19962019 LL surveys, using non linear least squares.

## Length at age

$$
L_{a}=L_{\infty}\left(1-e^{-K\left(a-t_{0}\right)}\right)+\varepsilon_{a}
$$

Length-weight

$$
\widehat{W}=\alpha L^{\beta} \varepsilon
$$

## Weight at age

$$
\ln \widehat{W}_{a}=\ln W_{\infty}+\beta \ln \left(1-e^{-K\left(a-t_{0}\right)}\right)+\varepsilon_{a}
$$

## Temporal Change: K-means cluster analysis

2. Perform K-means cluster analysis on annual growth parameters (Kaufman and Rousseeuw 1990).

Years that are clustered in the same group have similar growth.


## Temporal Change: K-means cluster analysis

Step 1. Determine the recommended number of clusters to be used by calculating the average silhouette width.


Figure 1.1. Calculated average silhouette width (y axis) per number of clusters ( x axis) for females (a) and males (b). Dotted lines represent recommended number of clusters.

## Temporal Change: $K$-means cluster analysis

Step 2. Define the clusters using the Hartigan-Wong algorithm (1979)
(4) $\quad W\left(C_{k}\right)=\sum_{x_{i \in C_{k}}}\left(x_{i}-\mu_{k}\right)^{2}$

Each observation $\left(x_{i}\right)$ is assigned to a given cluster $C_{k}$ such that the sum of squares distance of the observation to their assigned cluster centers $\left(\mu_{k}\right)$ is minimized

## Temporal Change: K-means cluster analysis



Figure 1.2. Final cluster groupings of annual growth curves for female (a) and male (b) sablefish in Alaska waters. $1996=1,1997=2,1998=3$, and so on.

## Female:

Cluster 1: 1996-2004 Cluster 2: 2005-2019

Male:
Cluster 1:1996-1999, 2001-2003, 2010, 2017-2019
Cluster 2: 2000, 2004-2009, 20112016

## Temporal Change: Results

The following were the time periods tested for significant growth changes for both males and females.

2 CLUSTERS/TIME PERIODS

- 1996-2004
- 2005-2019



## Growth Model Testing

General Model: Separate parameter estimates for each time period.

$$
L_{a}=L_{\infty}[\text { Year }]\left(1-e^{-K[\text { Year }]\left(t-t_{0}[\text { Year }]\right)}\right)
$$

One parameter in common between time periods:
Common $L_{\infty}$ Model
Common $K$ Model
Common $t_{0}$ Model
Two parameters in common between time periods:
Common $L_{\infty}$ and $K$ Model
Common $L_{\text {inf }}$ and $t_{0}$ Model
Common $K$ and $t_{0}$ Model
Common Model: Same parameter estimates for all time periods:

$$
L_{a}=L_{\infty}\left(1-e^{-K\left(t-t_{0}\right)}\right)
$$

## Length Model Results

| Model | df | AIC: <br> Female | AIC: <br> Male |
| :--- | :--- | :--- | :--- |
|  | 7 | $99,45 \boldsymbol{*}^{*}$ | 77,213* |
| Common $L_{\infty}$ Model | 6 | 99,504 | 77,218 |
| Common $t_{0}$ Model | 6 | 99,615 | 77,265 |
| Common K Model | 6 | 99,668 | 77,305 |
| Common $L_{\infty}$ and K Model | 5 | 99,747 | 77,350 |
| Common $L_{\infty}$ and $t_{0}$ Model | 5 | 99,617 | 77,268 |
| Common $K$ and $t_{0}$ Model | 5 | 99,684 | 77,375 |
| Common Model | 4 | 100,158 | 77,739 |

## Length Model Results

## Females

## Males

## 1996-2004 2005-2019

1996-2004 2005-2019

| $80.2(0.221)$ | $82.8(0.29)$ | $67.8(0.12)$ | $68.3(0.13)$ |
| :---: | :---: | :---: | :---: |
| $0.22(0.005)$ | $0.14(0.002)$ | $0.29(0.008)$ | $0.20(0.004)$ |
| $-1.9(0.119)$ | $-4.3(0.13)$ | $-2.3(0.16)$ | $-4.1(0.15)$ |
| 5,767 | 9,591 | 4,889 | 8,503 |

## Length Model Results



Male Length at Age


## Weight Model Results

| Model | df | AIC: Female | AIC: Male |
| :---: | :---: | :---: | :---: |
| General Model | 7 | 44,475* | 24,359 |
| Common $W_{\infty}$ Model | 6 | 44,566 | 24,358* |
| Common $t_{0}$ Model | 6 | 44,570 | 24,378 |
| Common K Model | 6 | 44,740 | 24,445 |
| Common $W_{\infty}$ and K Model | 5 | 44,820 | 24,534 |
| Common $W_{\infty}$ and $t_{0}$ Model | 5 | 44,595 | 24,830 |
| Common K and $t_{0}$ Model | 5 | 44,795 | 24,531 |
| Common Model | 4 | 45,264 | 24,962 |

## Weight Model Results

|  | Females |  | Males |  |
| :---: | :---: | :---: | :---: | :---: |
|  | $\mathbf{1 9 9 6 - 2 0 0 4}$ | $\mathbf{2 0 0 5 - 2 0 1 9}$ | $\mathbf{1 9 9 6 - 2 0 0 4}$ | $\mathbf{2 0 0 5 - 2 0 1 9}$ |
| $\mathrm{W}_{\infty}$ | $5.6(0.05)$ | $6.2(0.08)$ | $3.3(0.02)$ | $3.2(0.02)$ |
| $k$ | $0.24(0.005)$ | $0.14(0.003)$ | $0.34(0.01)$ | $0.23(0.005)$ |
| $\mathrm{t}_{6}$ | $-1.34(0.07)$ | $-4.23(0.08)$ | $-1.53(0.09)$ | $-3.25(0.15)$ |
| n | 5,767 | 9,591 | 4,889 | 8,503 |

## Weight Model Results

Female Weight at Age


Male Weight at Age


## Results

$>$ There have been temporal changes in the growth of both male and female sablefish: an obvious change occurred after 2004 for females, and a less obvious change around this time for males.
$>$ Sablefish are growing to a larger maximum size, but at a slower rate, which translates to smaller sized fish during the critical early ages when fish are reaching maturity.

## However....Final Recommendation

Recommend updating size at age parameters with all available post-1996 data:

1981-1993
1996-2019


## Final Recommendation - Length at Age

|  |  | 1981-1993 | 1996-2004 | 2005-2019 | 1996-2019 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Female | $\mathrm{L}_{\infty}$ | 75.5 (0.460) | 80.2 (0.221) | 82.8 (0.29) | 81.2 (0.19) |
|  | k | 0.208 (0.018) | 0.22 (0.005) | 0.14 (0.002) | 0.17 (0.003) |
|  | t。 | -3.62 (0.523) | -1.9 (0.119) | -4.3 (0.13) | -3.28 (0.09) |
|  | n | 31 | 5,767 | 9,591 | 15,358 |
| Male | $\mathrm{L}_{\infty}$ | 65.2 (0.341) | 67.8 (0.12) | 68.3 (0.13) | 67.9 (0.09) |
|  | k | 0.2 (0.029) | 0.29 (0.008) | 0.20 (0.004) | 0.23 (0.003) |
|  | t。 | -4.09 (0.936) | -2.3 (0.16) | -4.1 (0.15) | -3.3 (0.11) |
|  | n | 30 | 4,889 | 8,503 | 13,392 |

## Final Recommendation - Length at Age



## Final Recommendation - Weight at Age

|  |  | 1996-2004 | 2005-2019 | 1996-2019 |
| :---: | :---: | :---: | :---: | :---: |
| Female | $\mathrm{W}_{\infty}$ | 5.6 (0.05) | 6.2 (0.08) | 5.87 (0.04) |
|  | k | 0.24 (0.005) | 0.14 (0.003) | 0.17 (0.002) |
|  | t。 | -1.34 (0.07) | -4.23 (0.08) | -2.98 (0.06) |
|  | n | 5,767 | 9,591 | 15,358 |
| Male | $\mathrm{W}_{\infty}$ | 3.3 (0.02) | 3.2 (0.02) | 3.2 (0.01) |
|  | k | 0.34 (0.01) | 0.23 (0.005) | 0.27 (0.002) |
|  | t 。 | -1.53 (0.09) | -3.25 (0.15) | -2.41 (0.07) |
|  | n | 4,889 | 8,503 | 13,392 |

## Final Recommendation - Weight at Age

Female Weight at Age


Male Weight at Age


## Final Recommendation

## 1981-1993 <br> 1996-2019

Length-at-Age: Female

$$
L_{a}=75.5\left(1-e^{-0.208(a+3.62)}\right)+\varepsilon_{a} \quad L_{a}=81.2\left(1-e^{-0.17(a+3.28)}\right)+\varepsilon_{a}
$$

Length-at-Age: Male
$L_{a}=65.2\left(1-e^{-0.2(a+4.09)}\right)+\varepsilon_{a} \quad L_{a}=67.9\left(1-e^{-0.23(a+3.3)}\right)+\varepsilon_{a}$
Weight-at-Age: Female

$$
\ln \widehat{W}_{a}=\ln (5.87)+3.02 \ln \left(1-e^{-0.17(a+2.98)}\right)+\varepsilon_{a}
$$

Weight-at-Age: Male

$$
\ln \widehat{W}_{a}=\ln (3.2)+3.02 \ln \left(1-e^{-0.27(a+2.41)}\right)+\varepsilon_{a}
$$

## Questions?



