

Estimation of selectivity, growth, and natural mortality in the assessment for EBS snow crab

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Juneau, AK

CPT and SSC comments

The CPT had several comments and questions related to formatting and presentation from the September 2016 meeting:

- Review SAFE guidelines to make sure required tables and figures are present
- Plot the relative proportion of new to old shell males to see how important the lack of fit to old shell males really is
- Plot Bayesian posterior intervals for growth parameters
- Model 0 has to be last year's accepted model

These issues will be corrected in the SAFE document presented at the September meeting. The CPT also had several suggestions for potential model runs and expanded analyses, including:

- Estimate M for mature females
- Document rationale for prior on M for immature crab
- Try starting the assessment in 1982 to check the behavior of the survey q_s when the first survey stanza is excluded
- Apply priors to the survey q_s so they are somewhat constrained
- Provide more detailed MCMC chain diagnostics
- Extract bycatch mortality from the Tanner crab directed fisheries that is currently lumped into the groundfish trawl bycatch (in a table in the assessment chapter, not necessarily in the model)

Overview

1. MCMC diagnostics and Bayesian vs. maximum likelihood
 1. Bayesian methods designed to produce distributions
 2. Diagnostics suggests some problematic population processes
2. Survey selectivity
 1. Eliminate the first 4 years of data
 2. Think about how to use BSFRF data
3. Growth
 1. Piece-wise models causes problems, but contributes little to the model
 2. Unclear what the best model is
4. Natural mortality
 1. Mature female natural mortality should be estimated
 2. Priors for immature natural mortality should be revisited

Bayesian methods vs. maximum likelihood

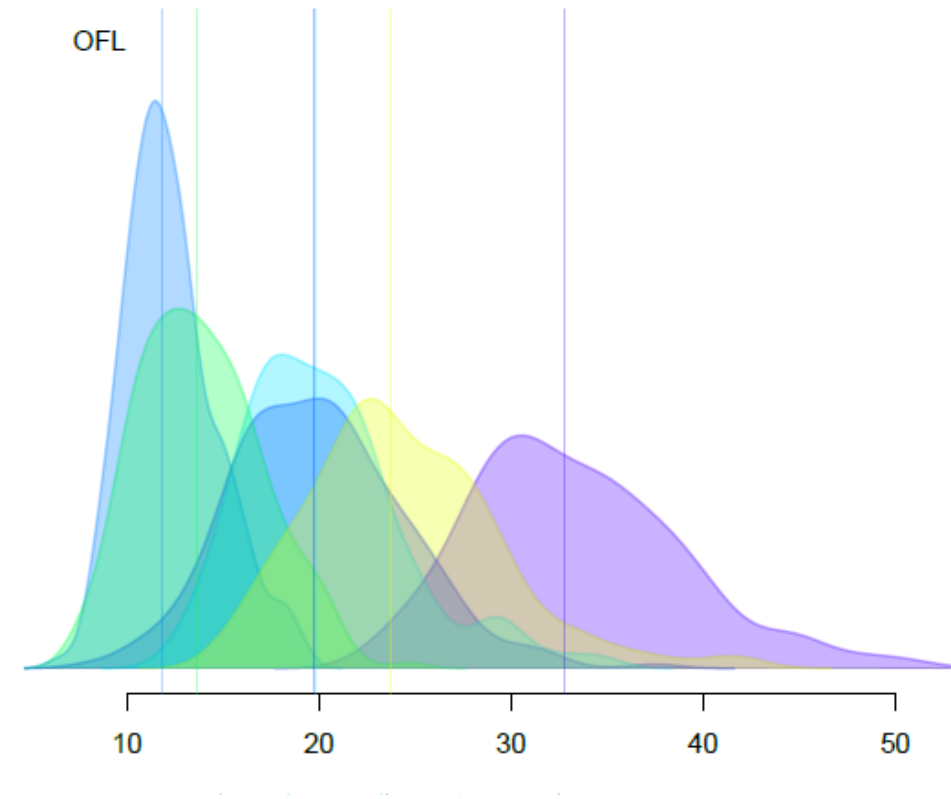
Goal: set a TAC that accounts for scientific uncertainty

Historical methods:

- estimate parameters via ML
- input parameters into projection script
- Input numbers at length for the final year in the projection script with error
- Calculate a distribution of the OFL based on the error added to the numbers at length

Problems with historical methods:

- Parameter values are not perfectly known, but are assumed so.
- Error added to numbers at length is arbitrary, but determines the distribution of the OFL.
- Jittering was required to ensure MLEs were found



Bayesian methods vs. maximum likelihood

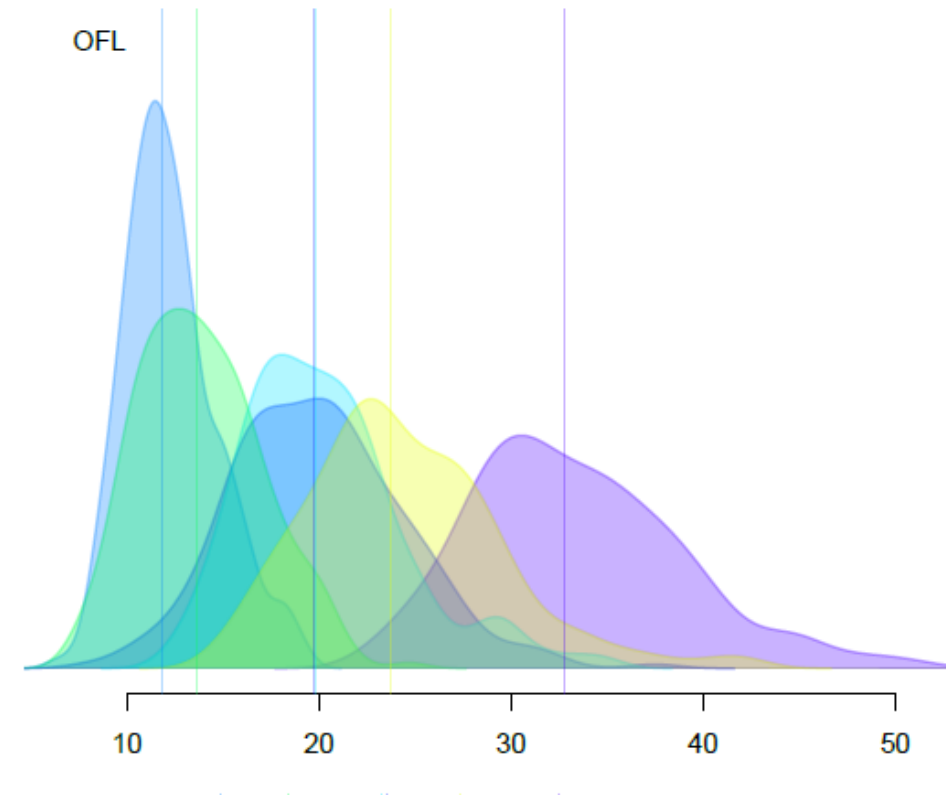
Goal: set a TAC that accounts for scientific uncertainty

Bayesian methods:

- Assume a distribution for each parameter
- Do not require copying and pasting model output
- Posterior distributions of the OFL are a result of the uncertainty in parameter estimates

Issues with Bayesian methods:

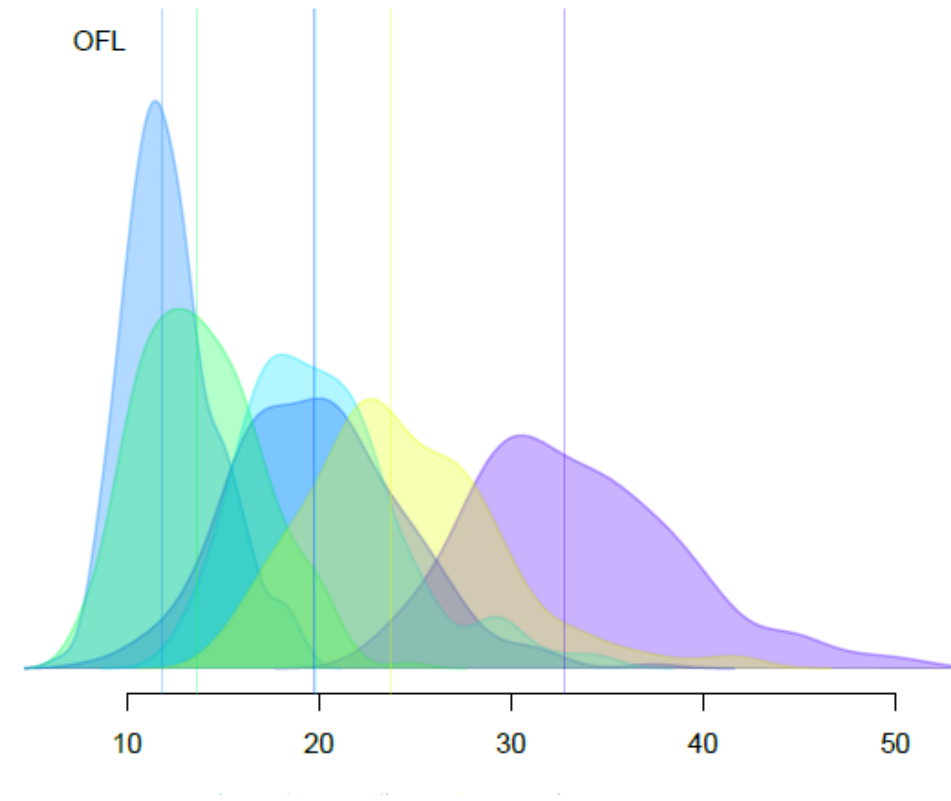
- Priors must be specified
- Time-consuming
- Knowing the model has converged is difficult (though there are many diagnostics to identify non-convergence)
- Reliant on the var/covar matrix; therefore reliant on an appropriately specified model



Bayesian methods vs. maximum likelihood

A possible modification of historical methods that avoids Bayesian methods:

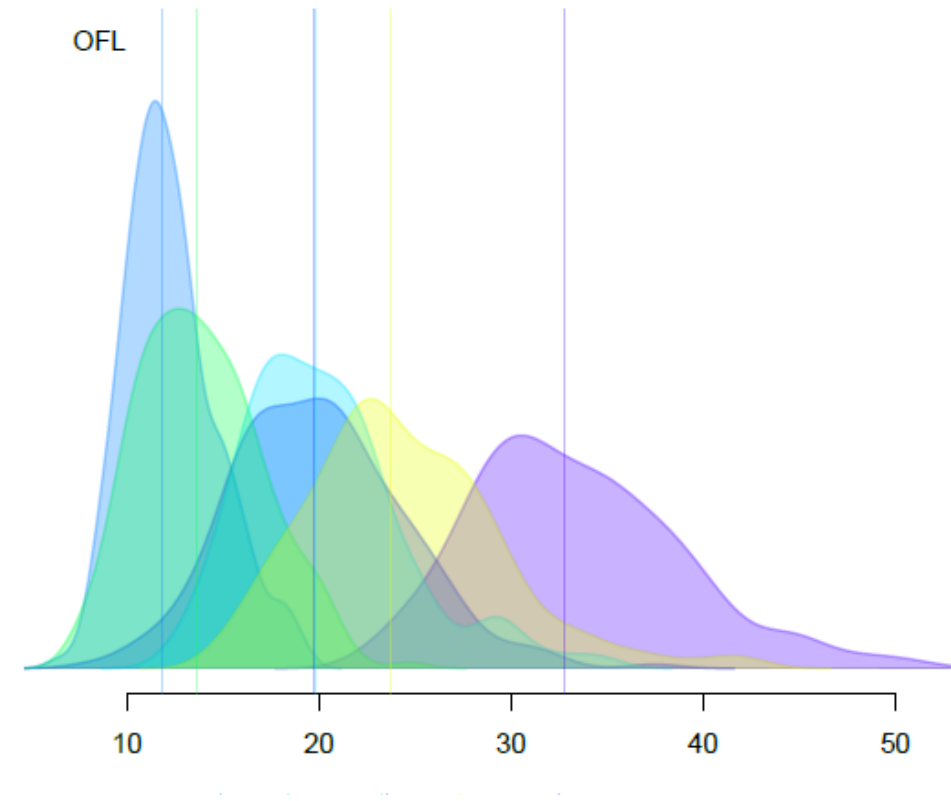
- Calculate the OFL during the fitting of the model instead of in the report section and include the OFL as a `sd_report` variable
- Then produce a distribution of the OFL with its calculated standard deviation
- I tried this once with the 'Trim data' model, but the model blew up.
- It takes forever to fit the model because reference points and the OFL have to be calculated in every step.

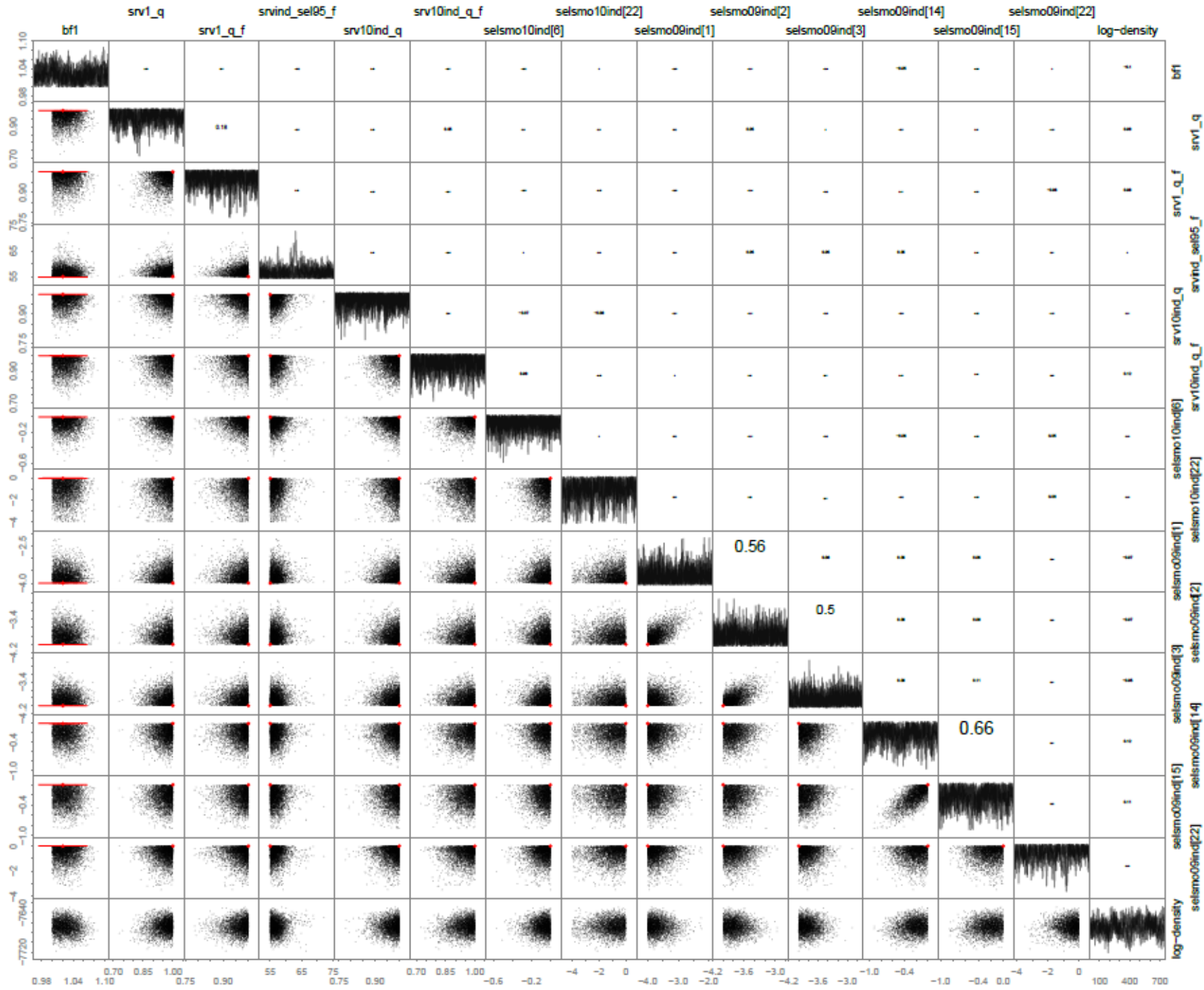


MCMC diagnostics

MCMC is used to 'build' the distributions of parameters and derived quantities

- Diagnostics check for appropriate specification of the model and var/covar matrix (used to explore the posterior)
- Stationarity in the traces for parameters and the objective function (mixing)
- No parameters hitting bounds
- If there are problems in these diagnostics, be cautious about inference from the model





Diagnostic summary

- Several processes have problem parameters
- Slow mixing:
 - Growth parameters
 - Rec devs
 - Initial numbers at length
- Bound hitting
 - Growth parameters
 - Survey selectivity (NMFS) during era 1
 - Industry survey selectivity parameters
- Dealt with slow mixing by using really long chains last year, but this takes a very long time
- Methods for adjustment
 - Priors on parameters hitting their bounds
 - Reformulating the model
 - Excluding problematic periods of data

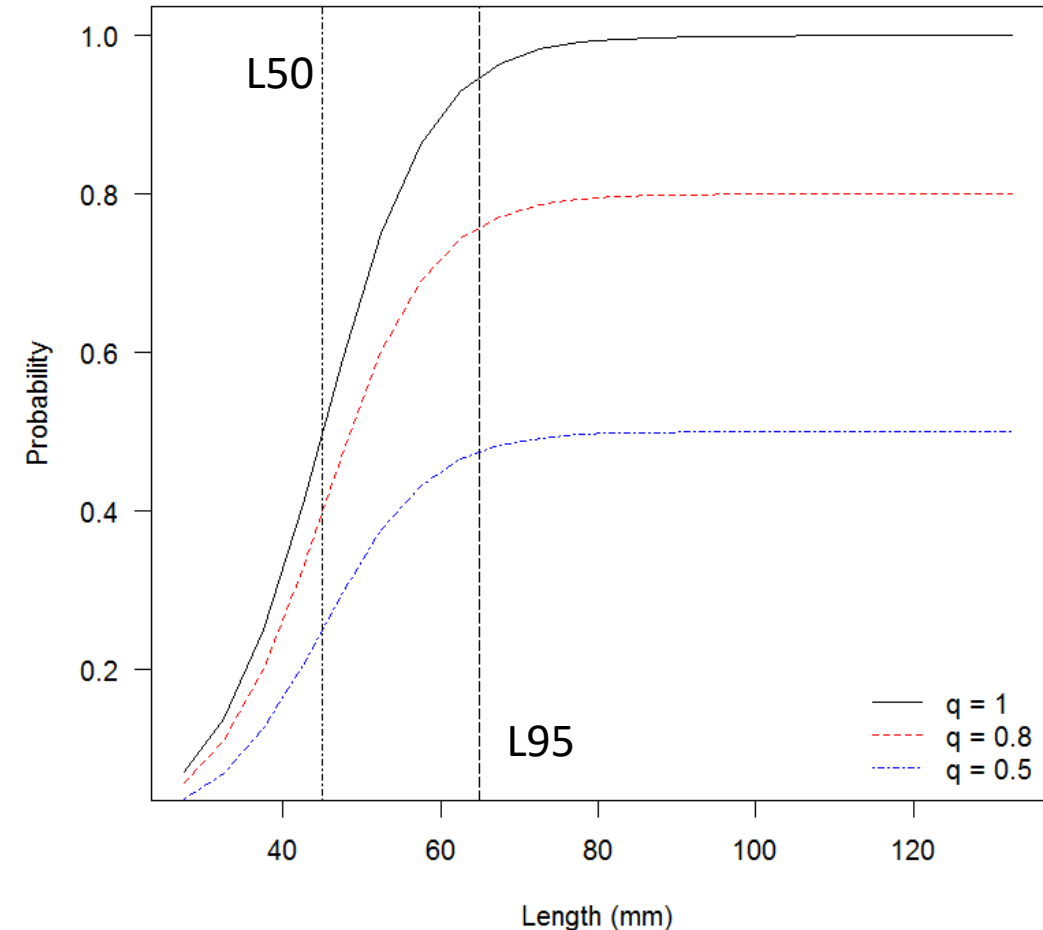
Estimating survey selectivity

- Historical methods
- Data
- Model runs
- Model results
 - Fits
 - OFL and reference points
 - Processes influenced
- Recommendations

Historical methods

- Logistic selectivity
- Three eras
 - 1978-1981: different gear
 - 1982-1988: different area
 - 1989-present: current
- Catchability coefficient (q)
 - Changes in estimates over time
 - Era 1 has always been fixed at 1
- Issues
 - Q modulates the impact of catch on the survey index
 - Foreign fleets were excluded starting 1980, so it's not clear if the catches are fully represented in era 1
 - Q in the first era is consistently estimated on its bounds and anchors the catchability in the other era
- Are the survey eras appropriately chosen?
- Are there alternate sensible configurations?

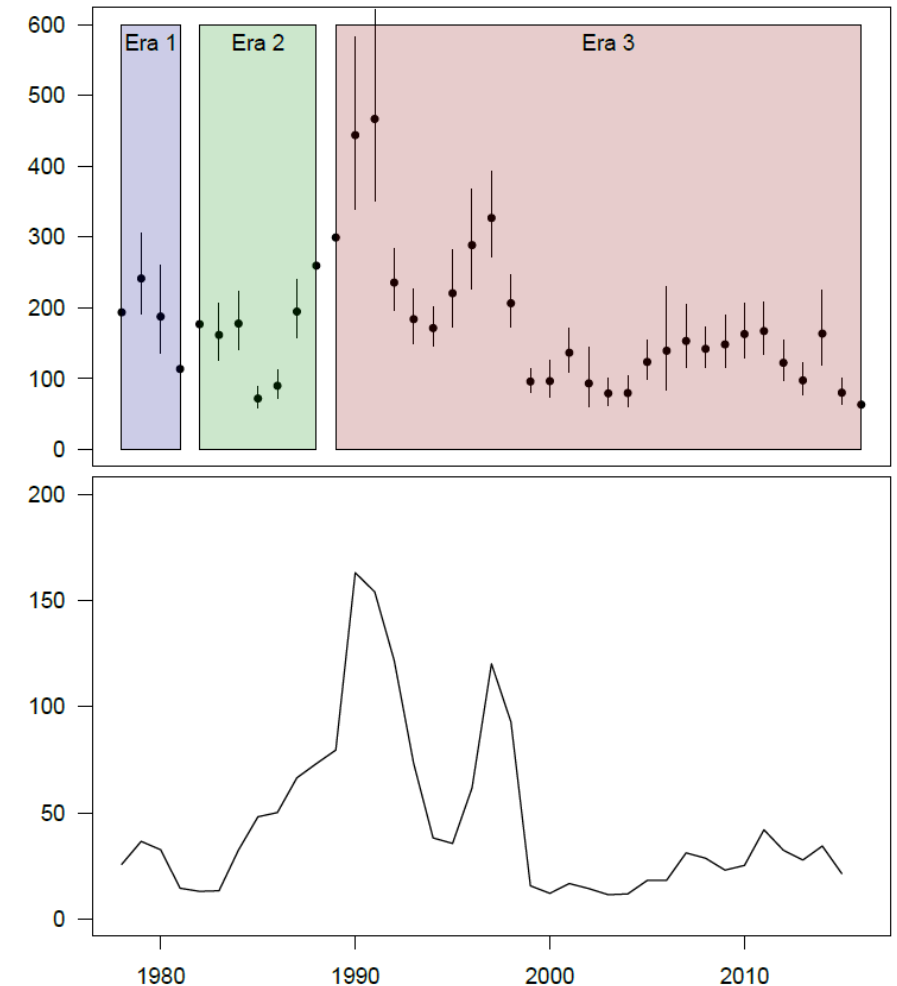
$$S_l = \frac{q}{1 + e^{(-\ln(19))\frac{L_l - L_{50}}{L_{95} - L_{50}}}}$$



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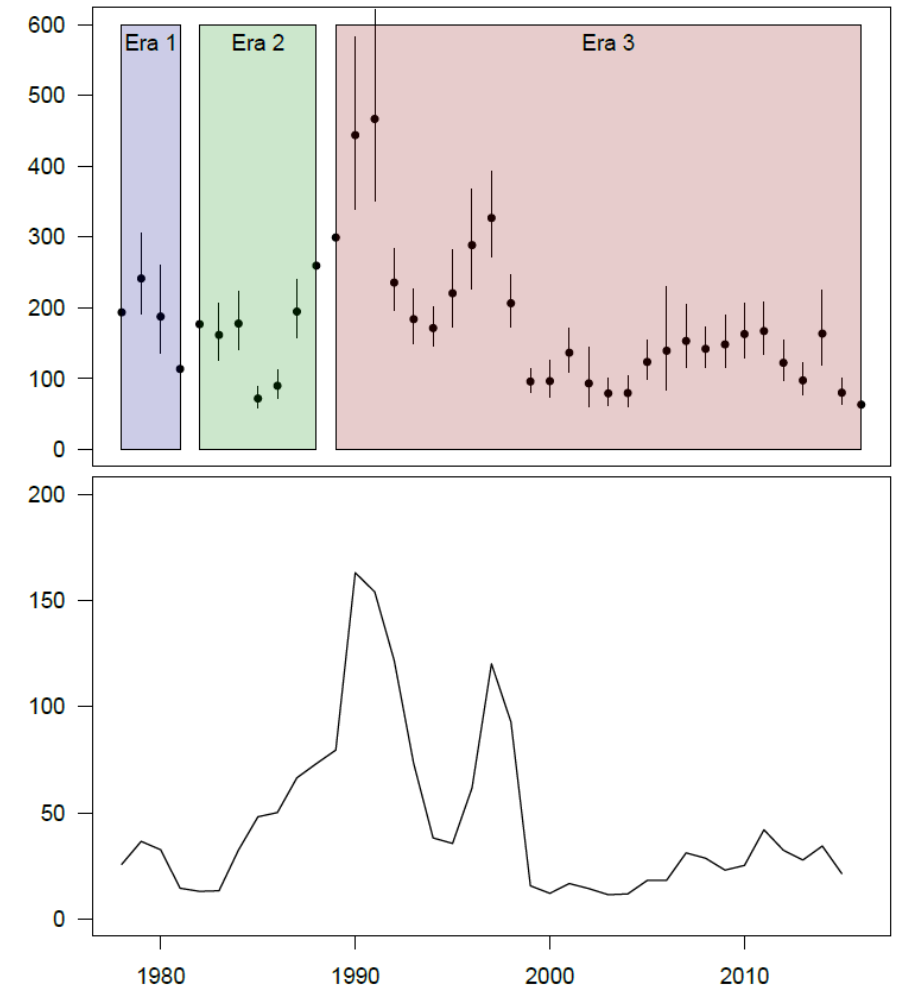
$$S_l = \frac{q}{1 + e^{(-\ln(19) \frac{L_l - \beta_{50}}{\beta_{95} - \beta_{50}})}}$$

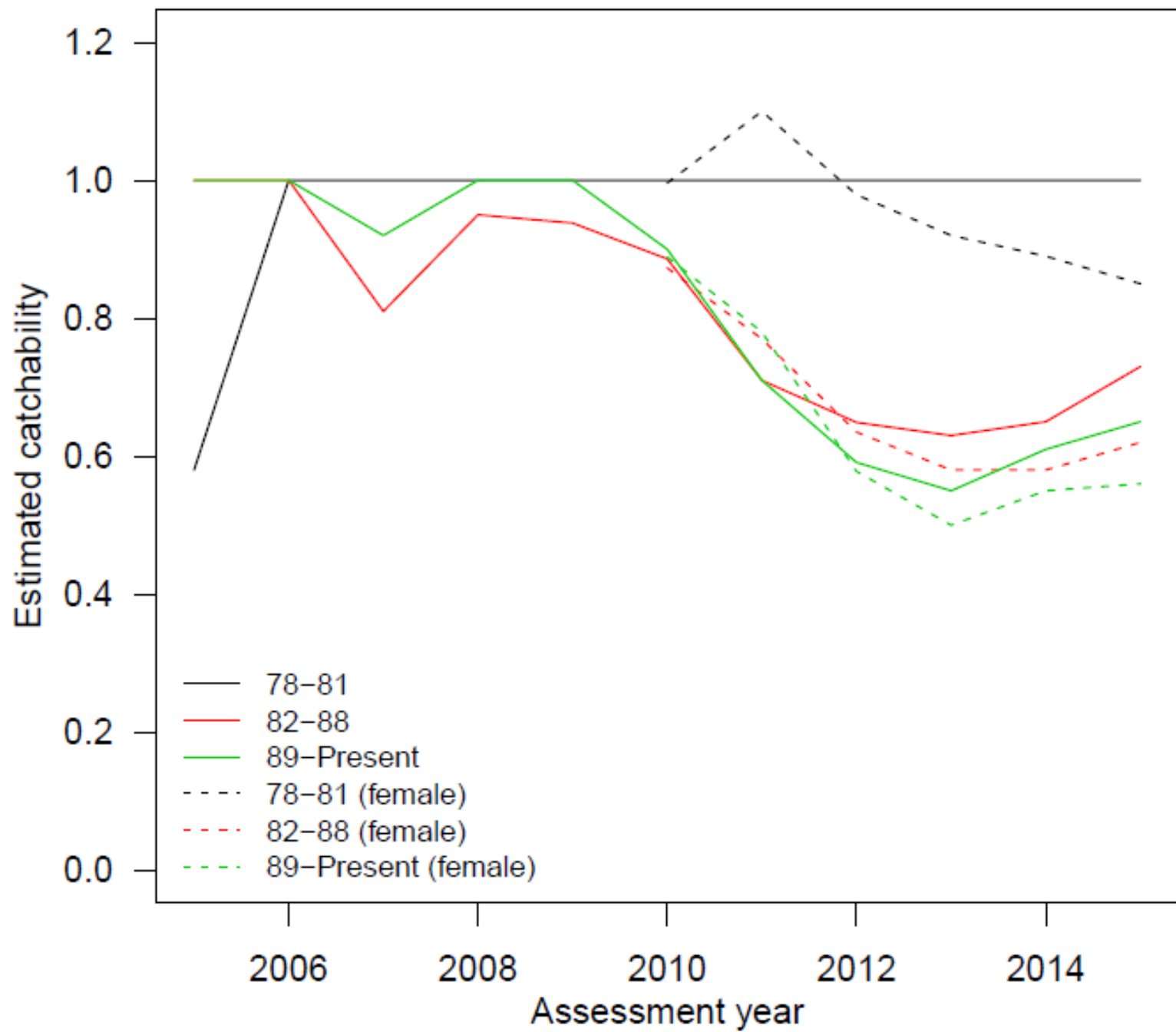


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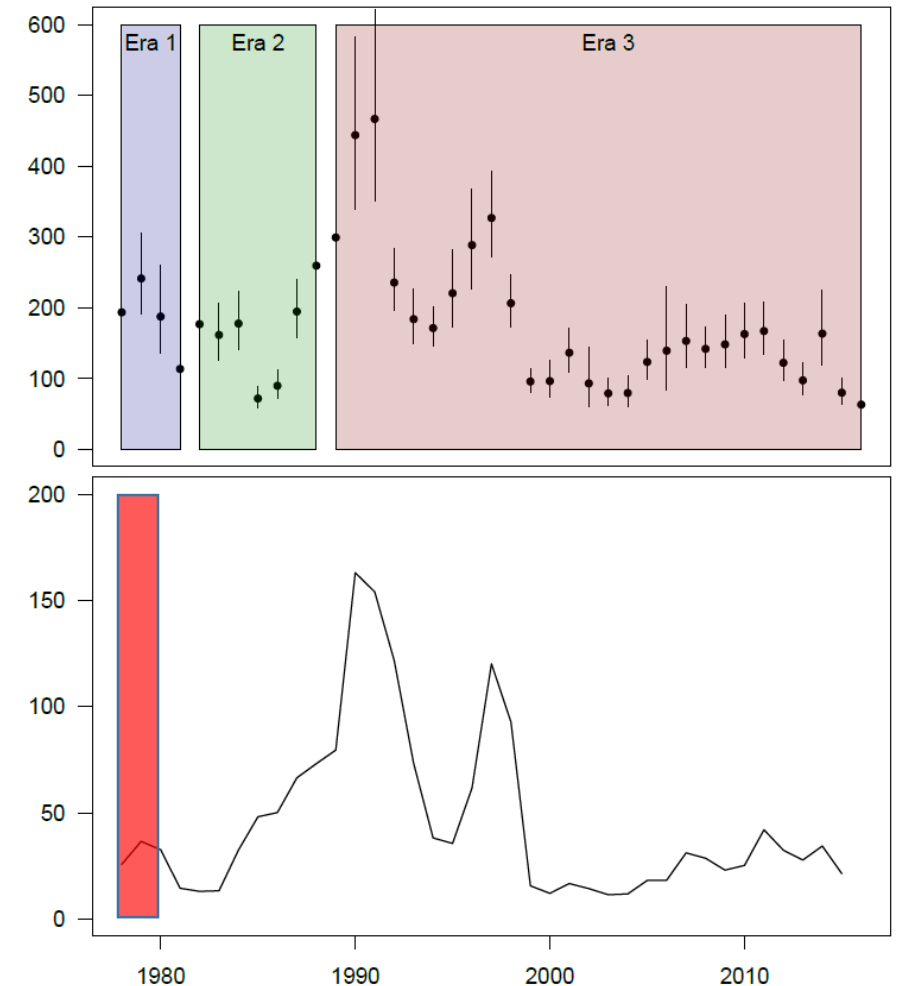




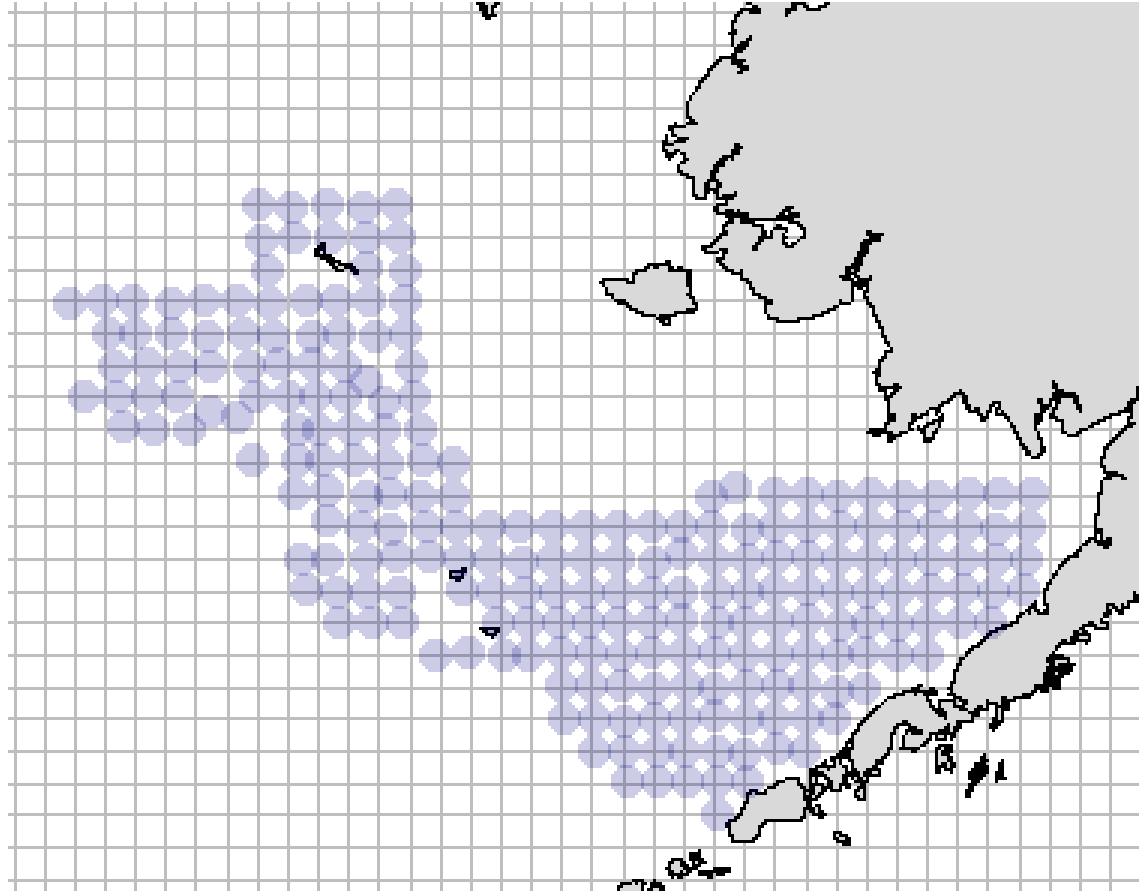
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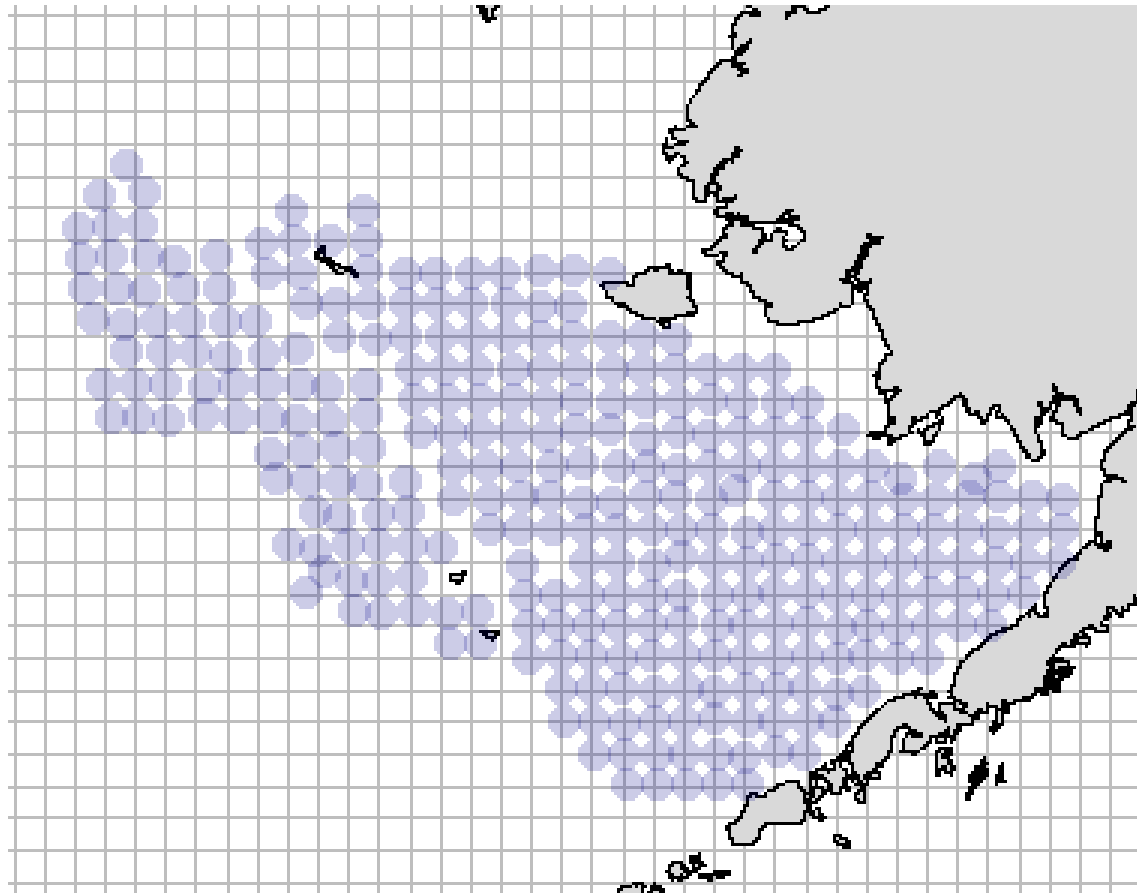
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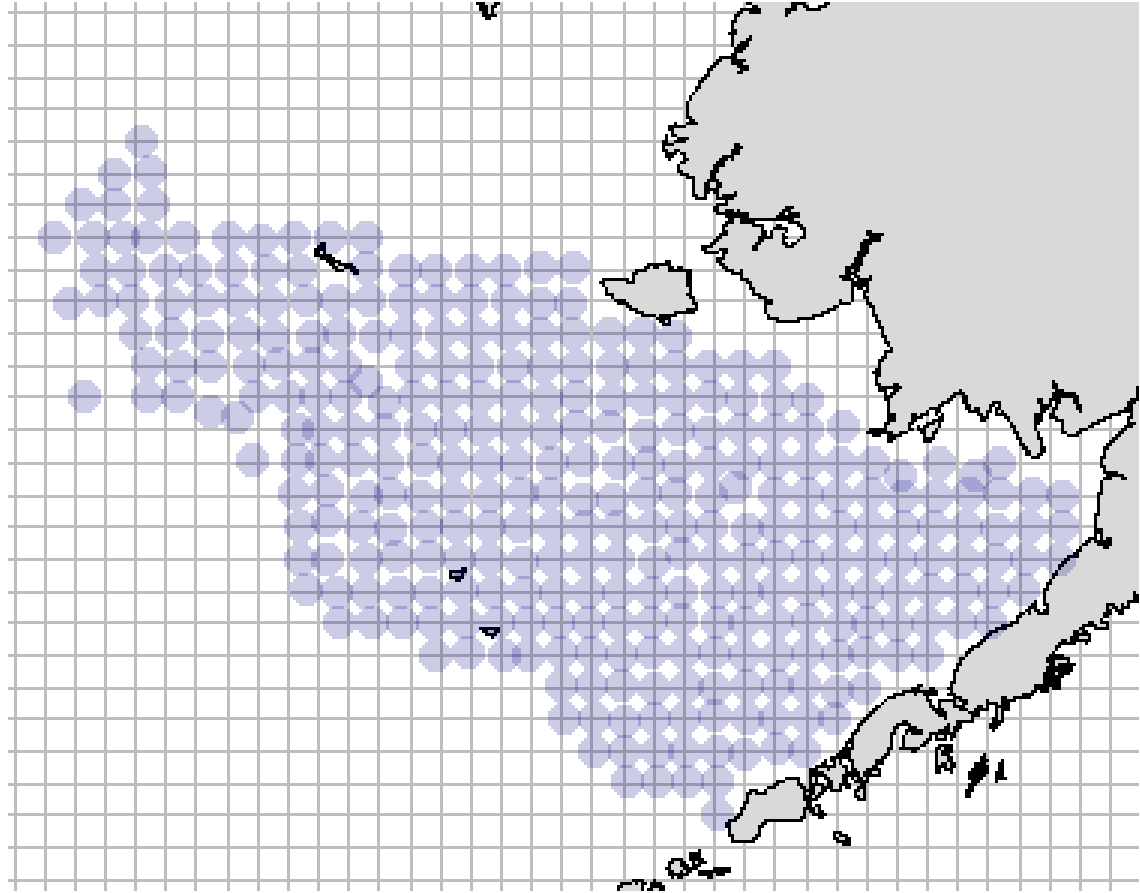
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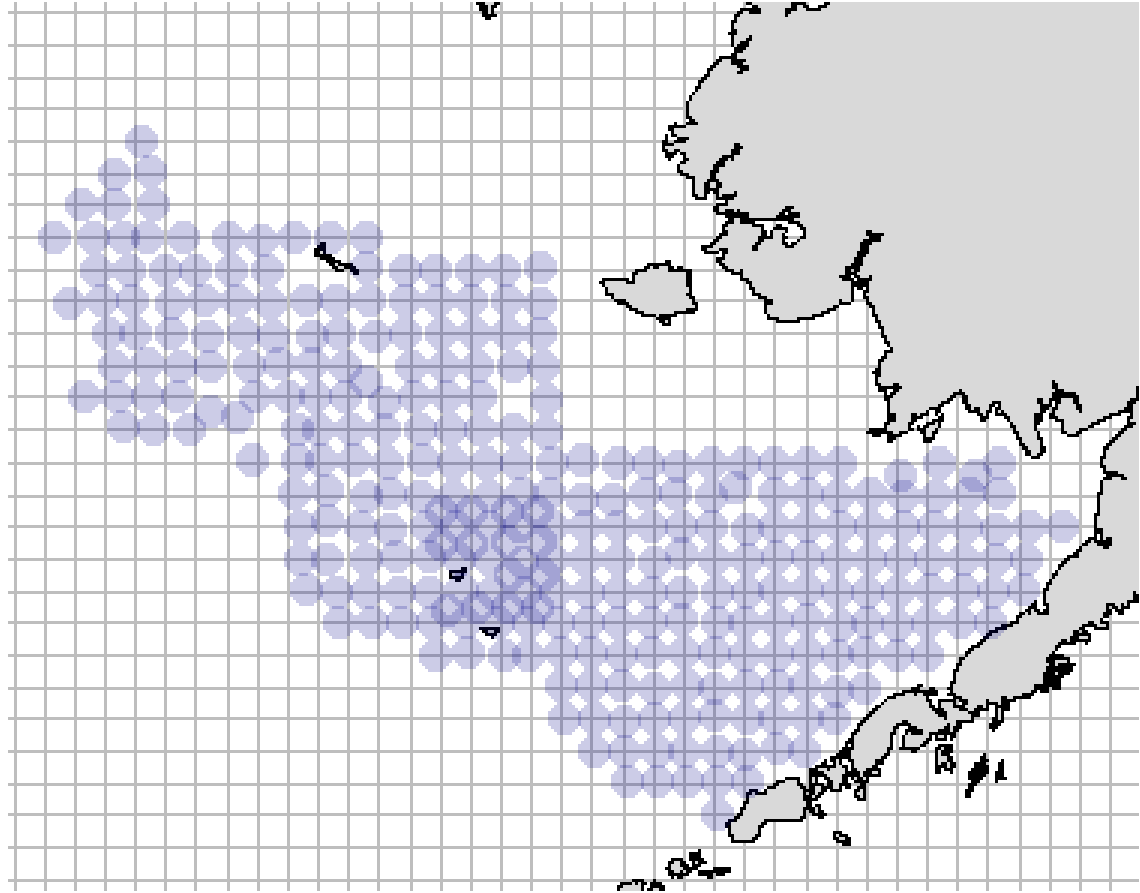
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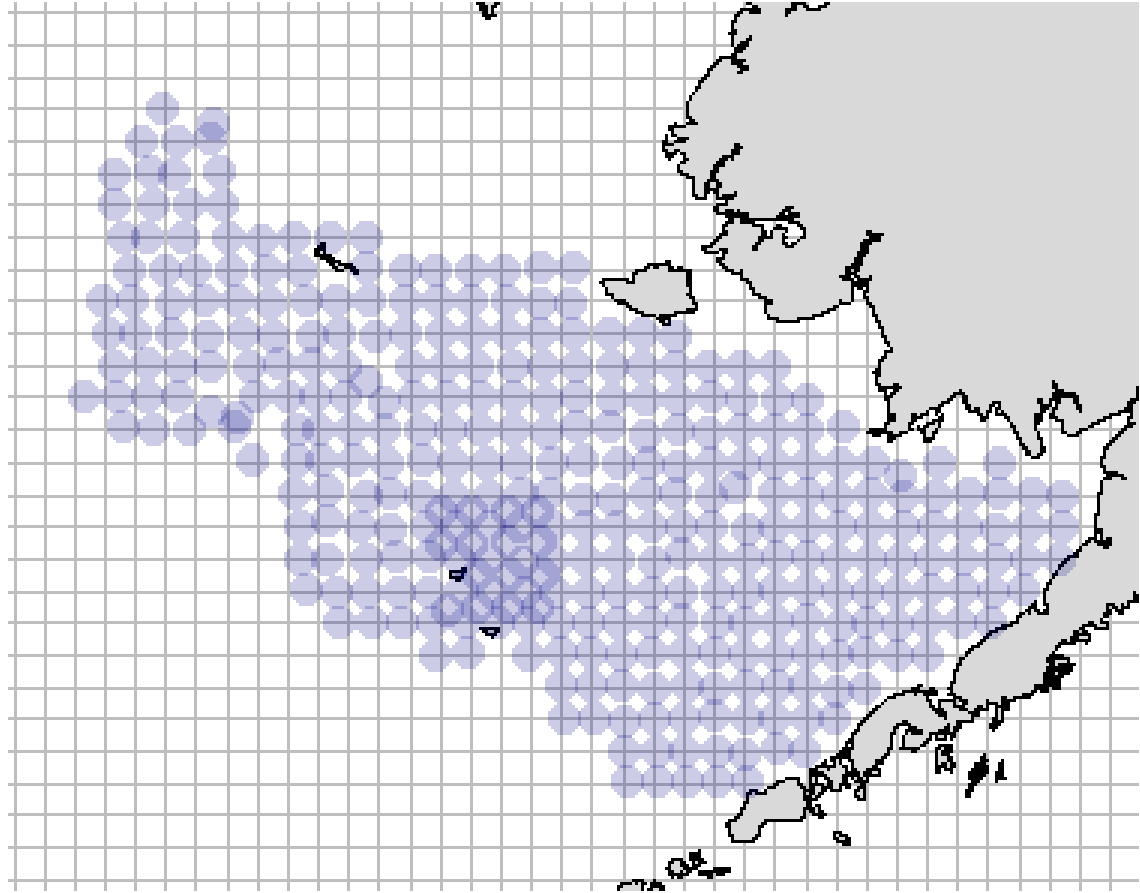
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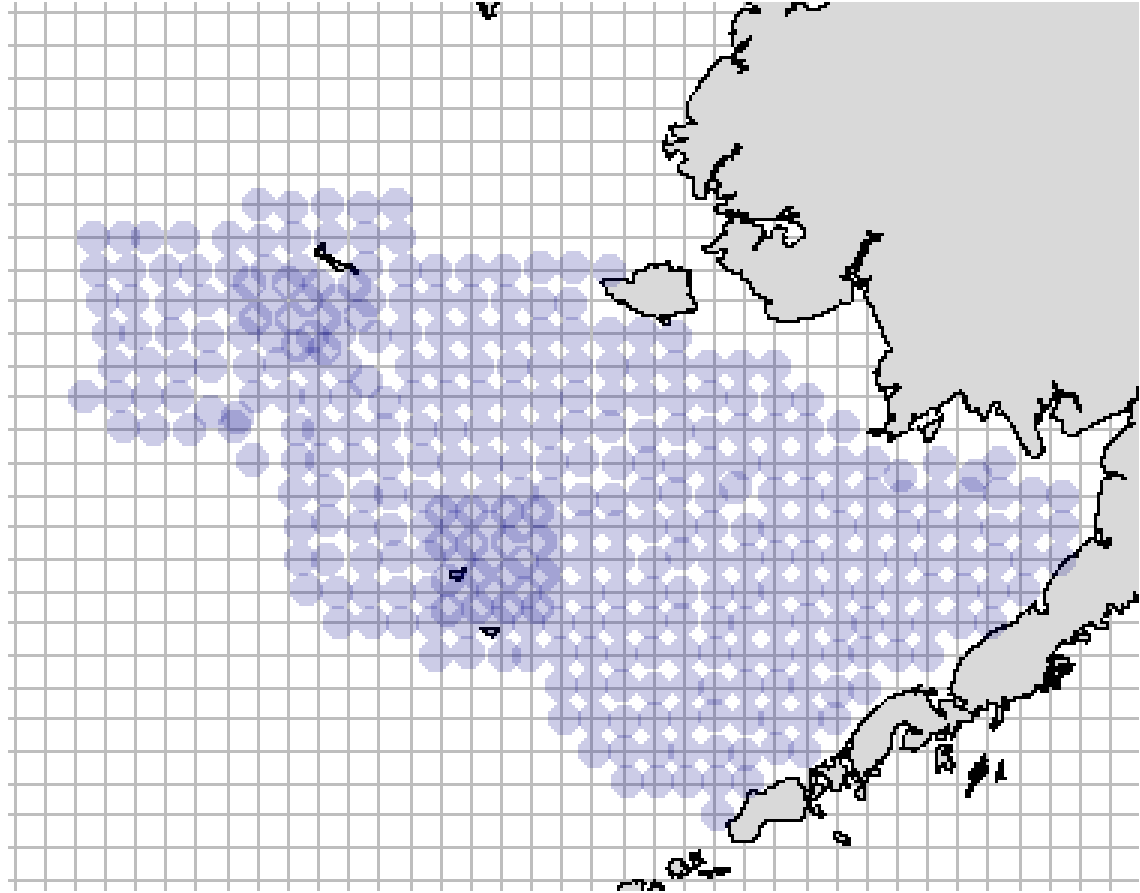
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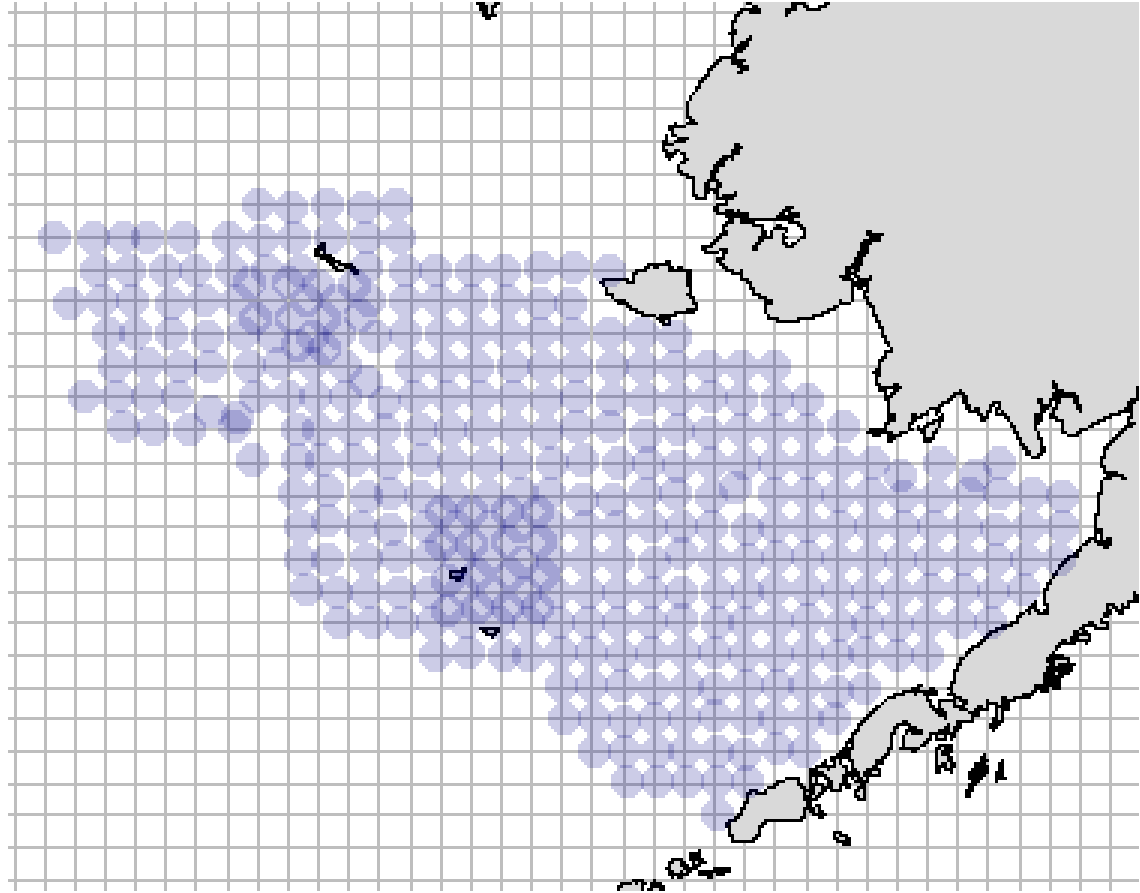
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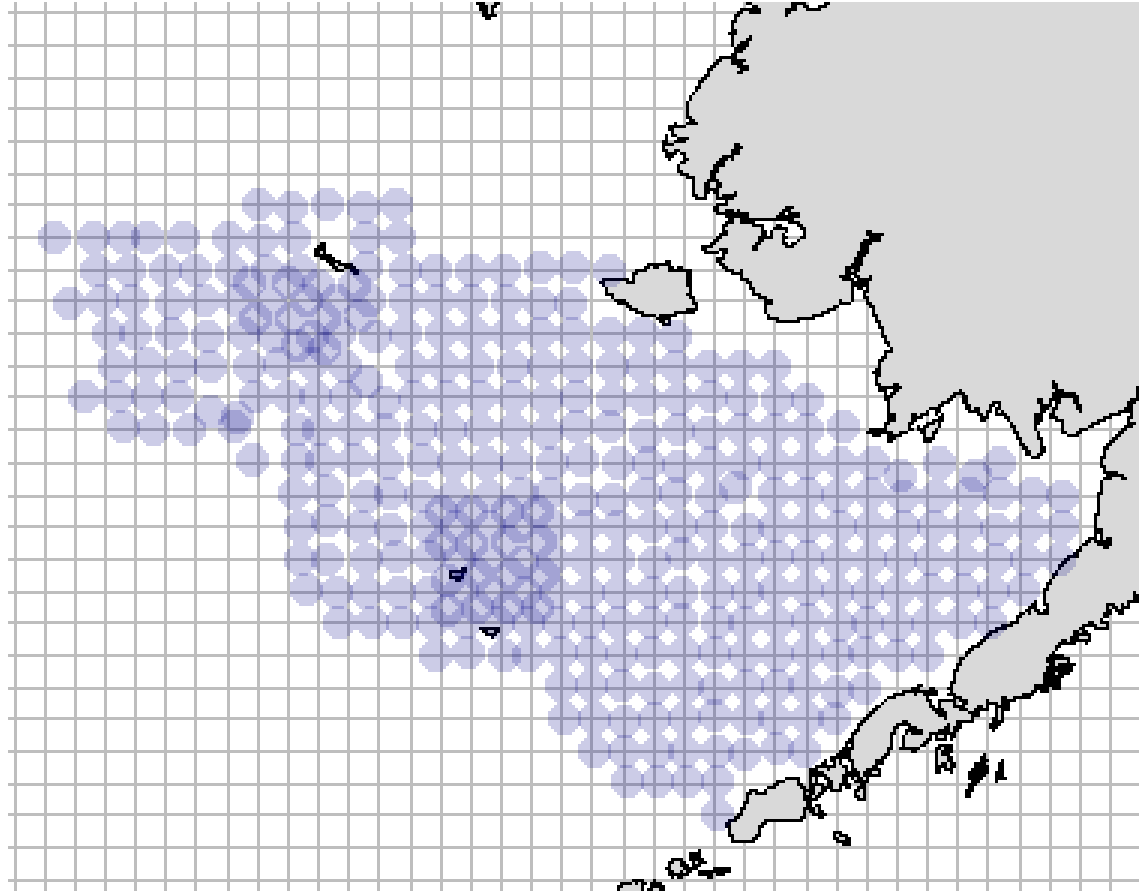
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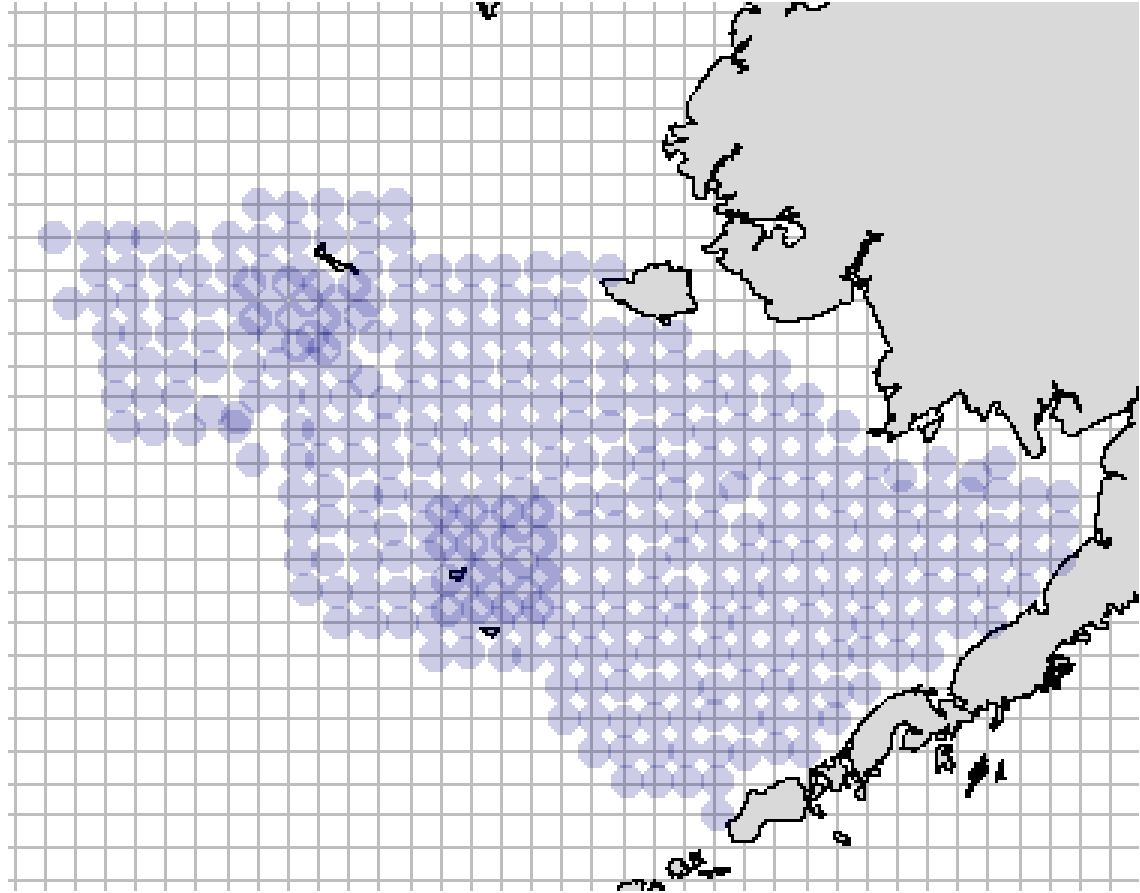
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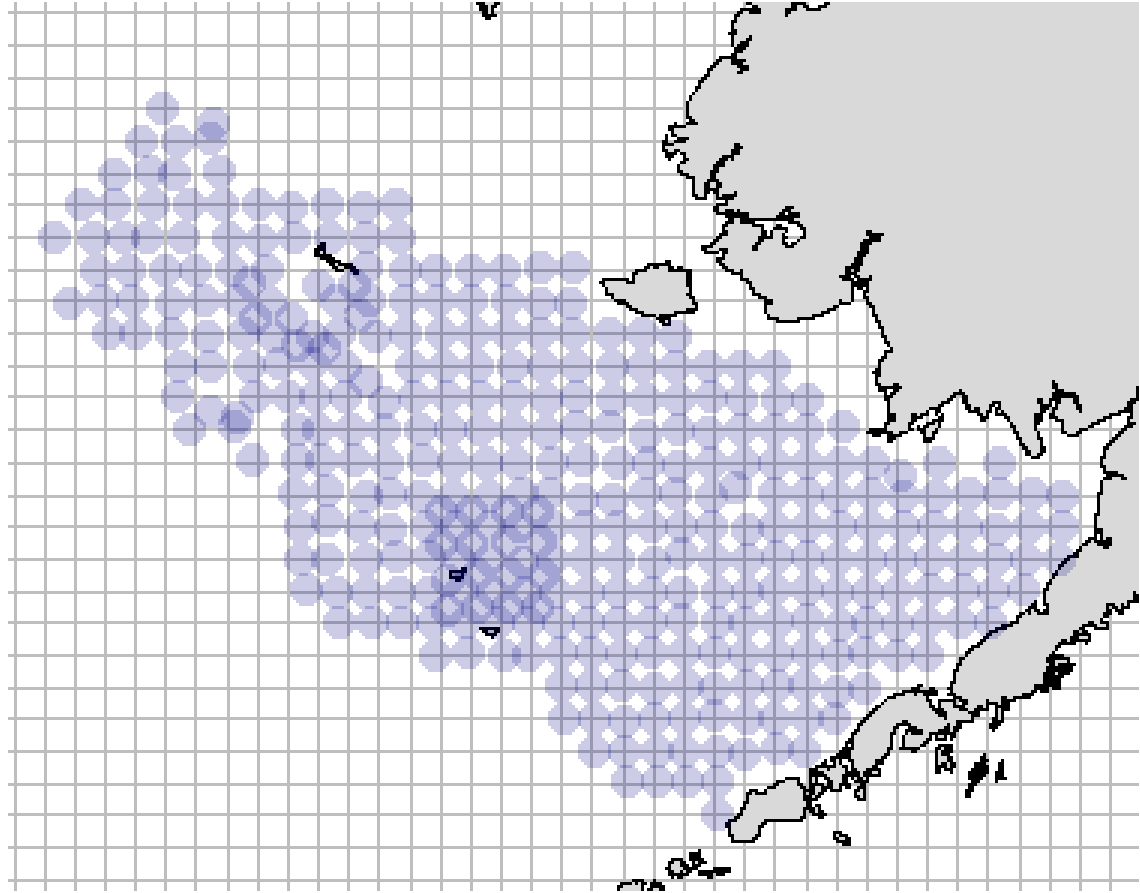
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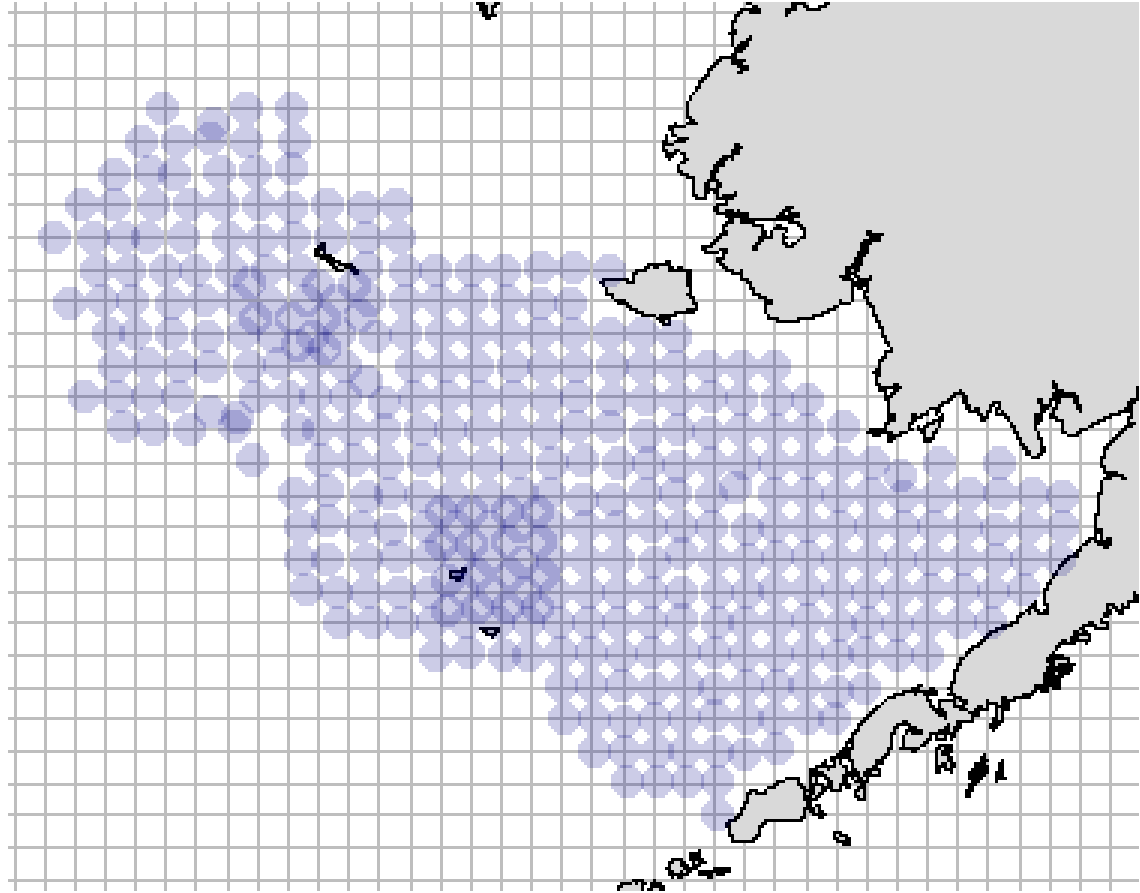
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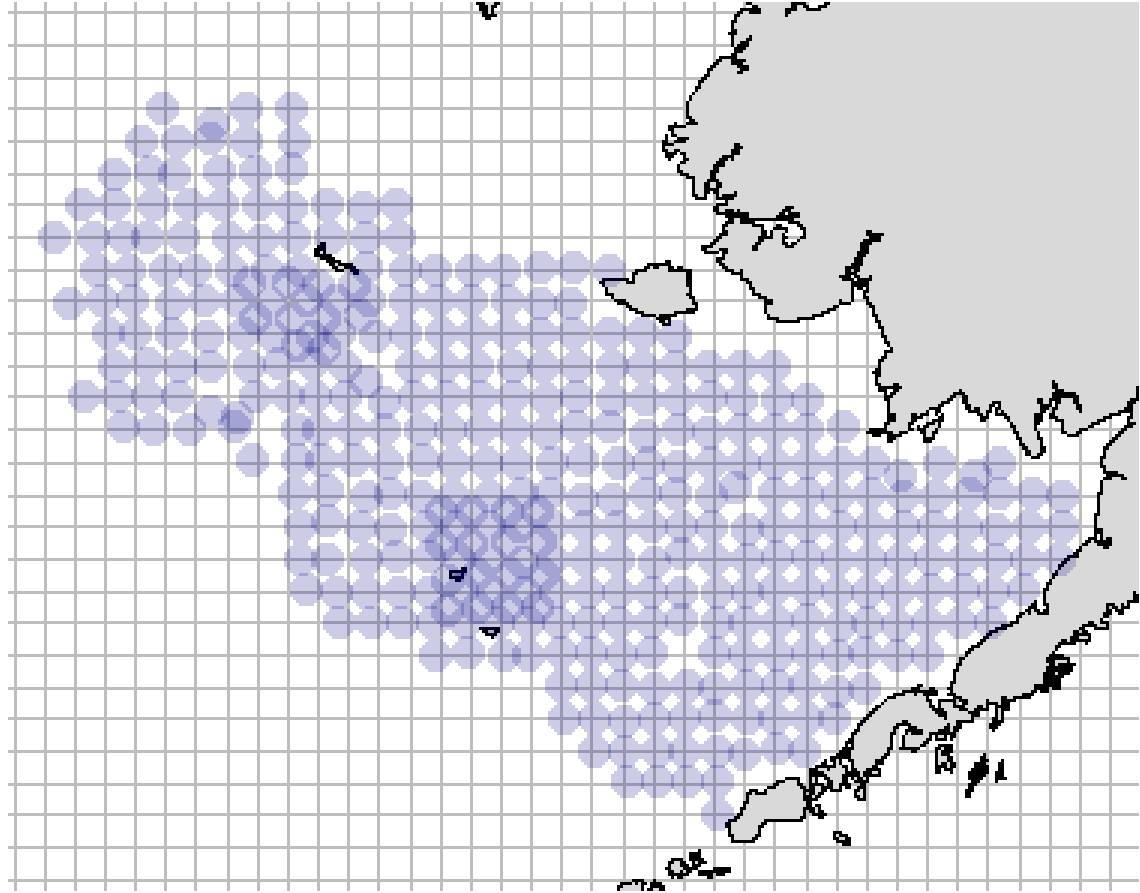
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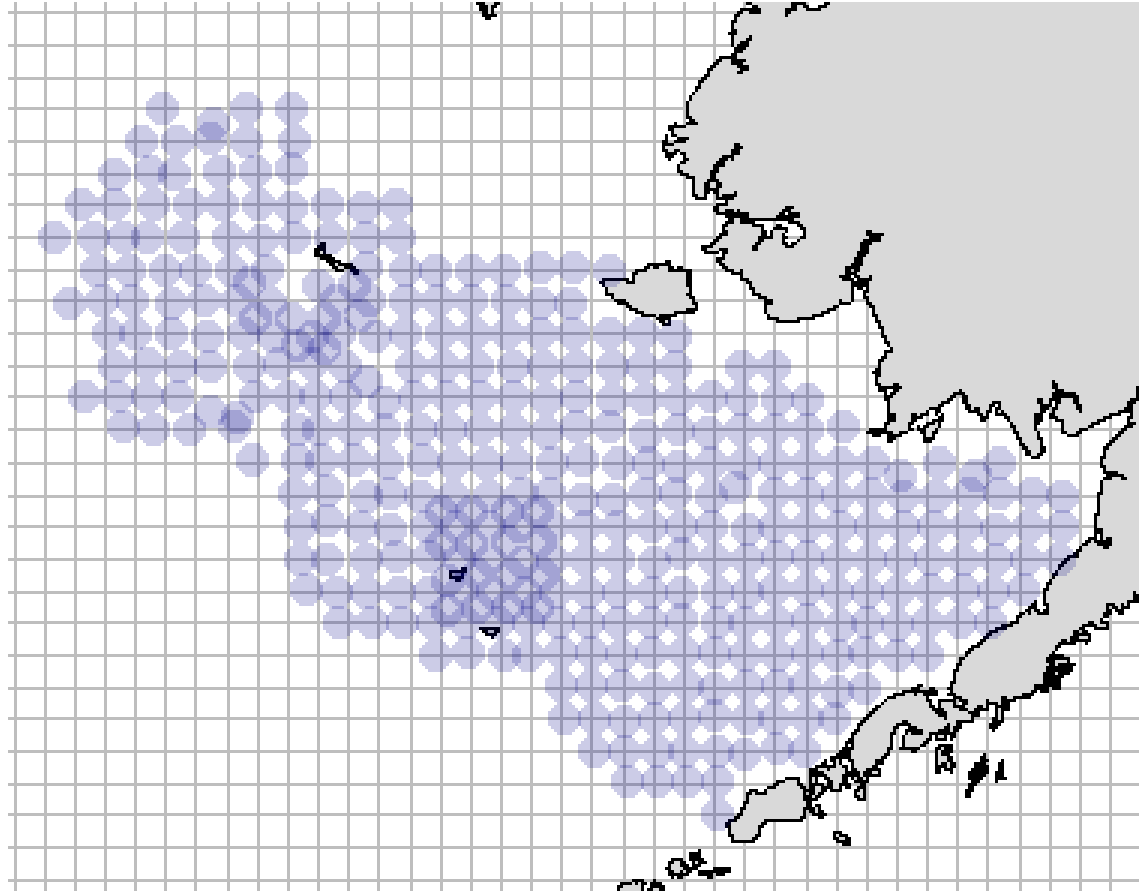
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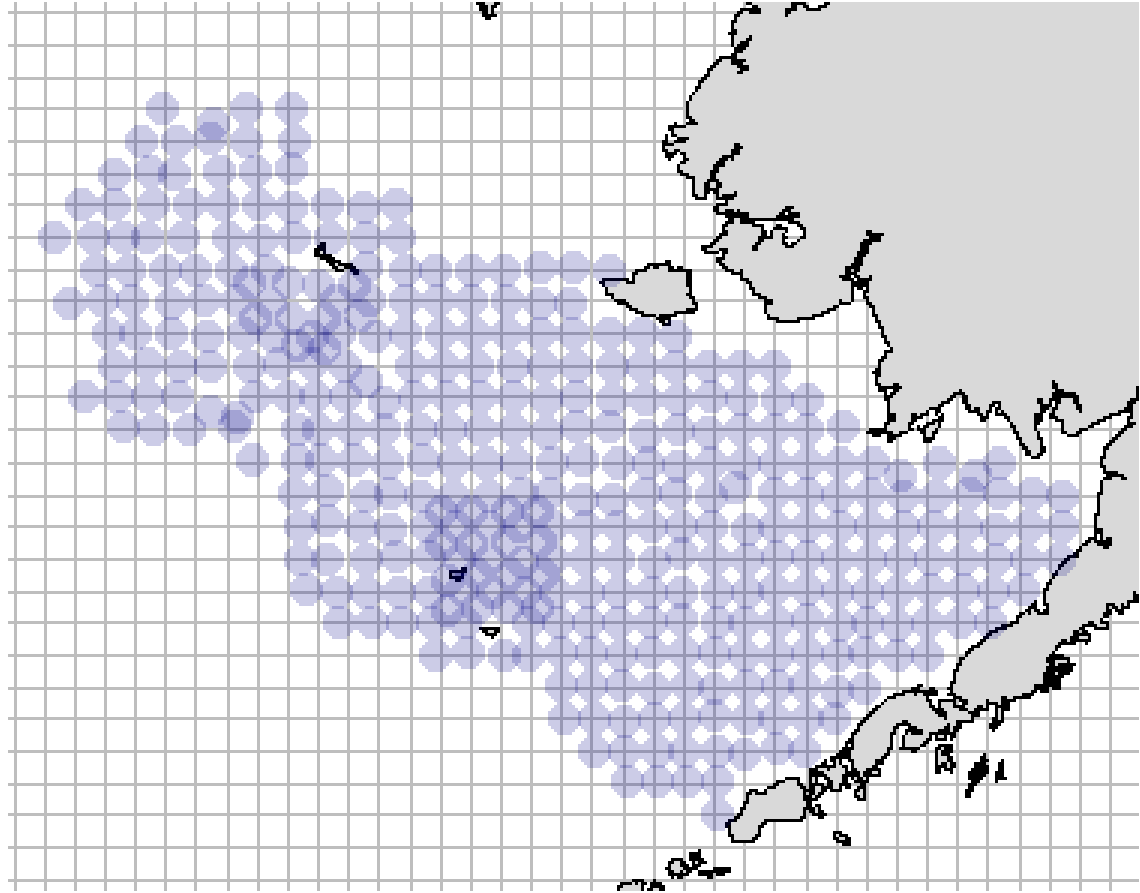
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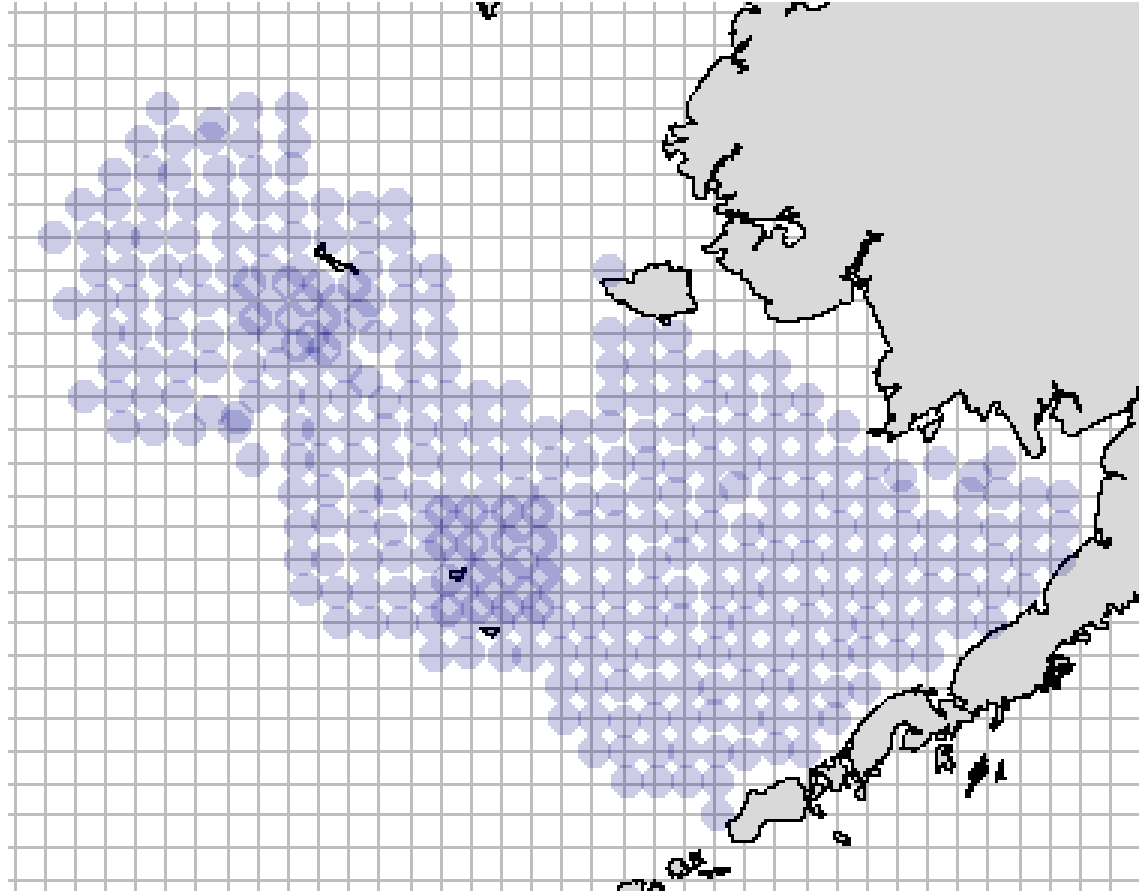
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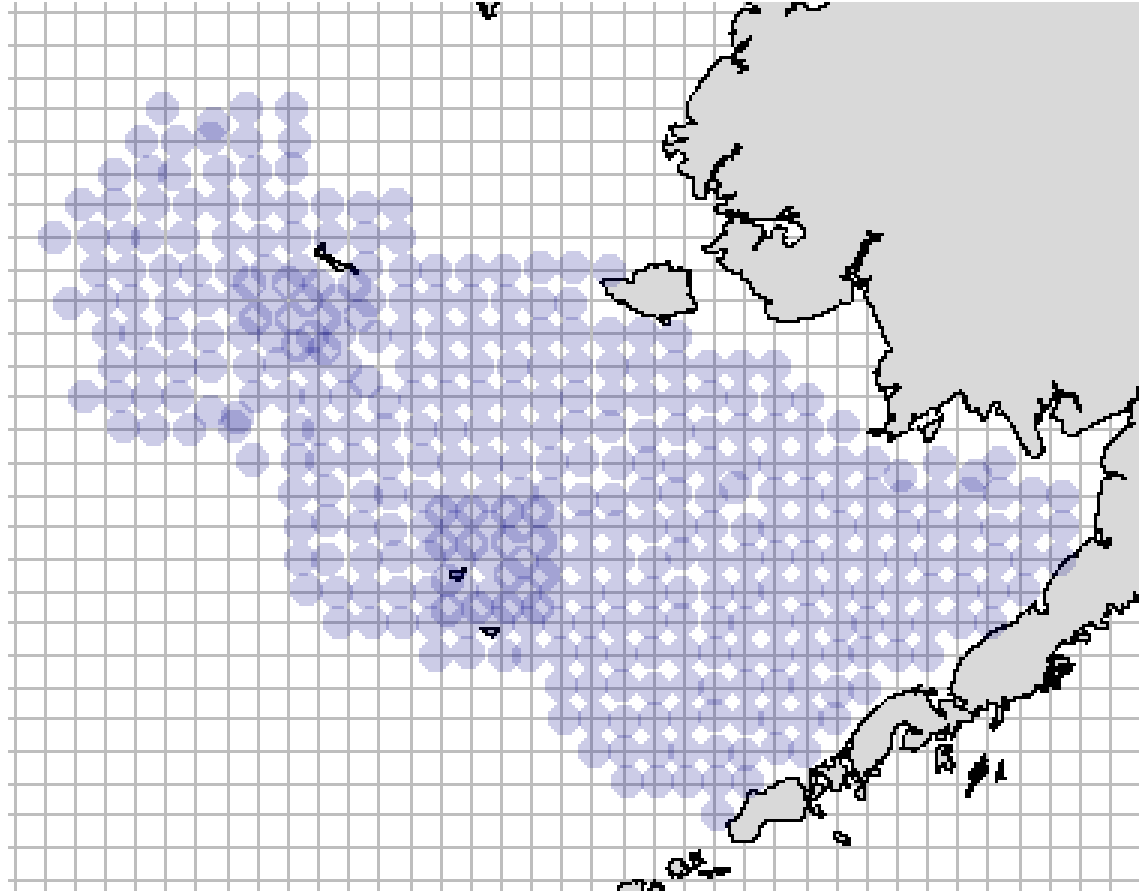
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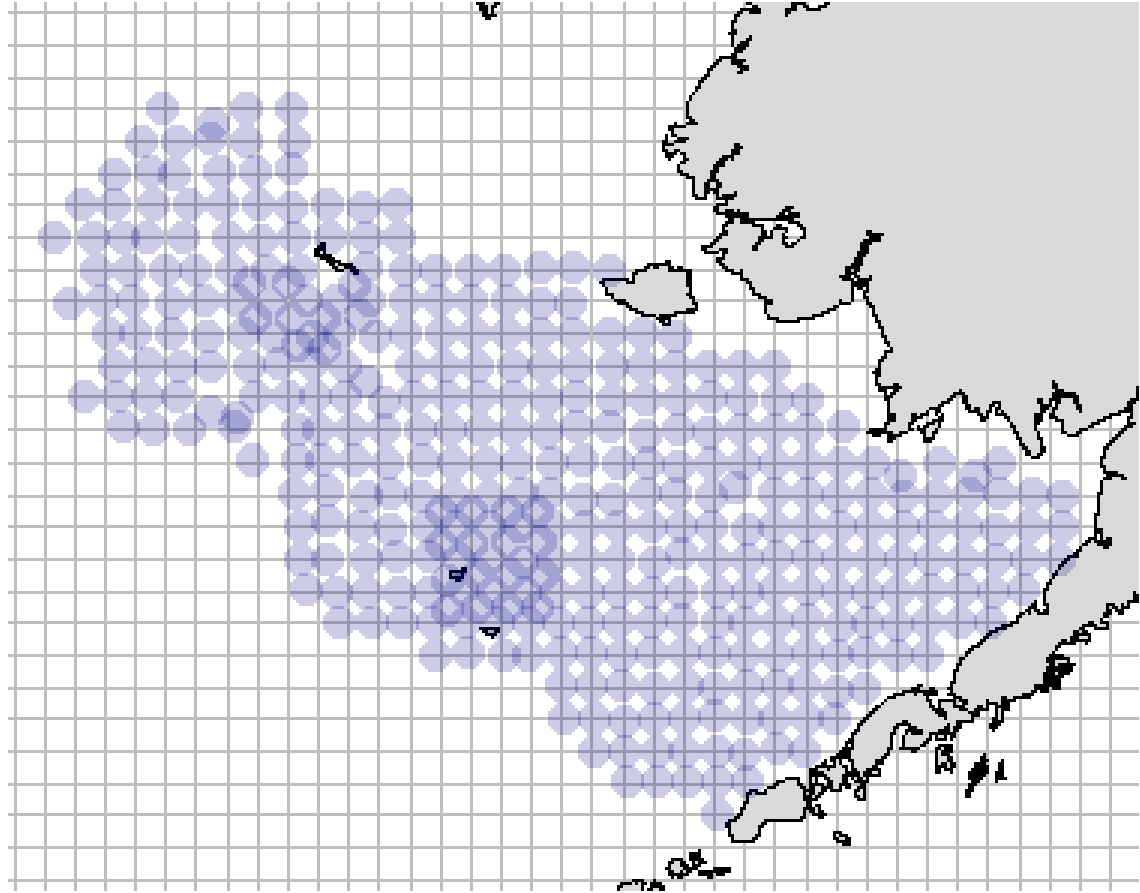
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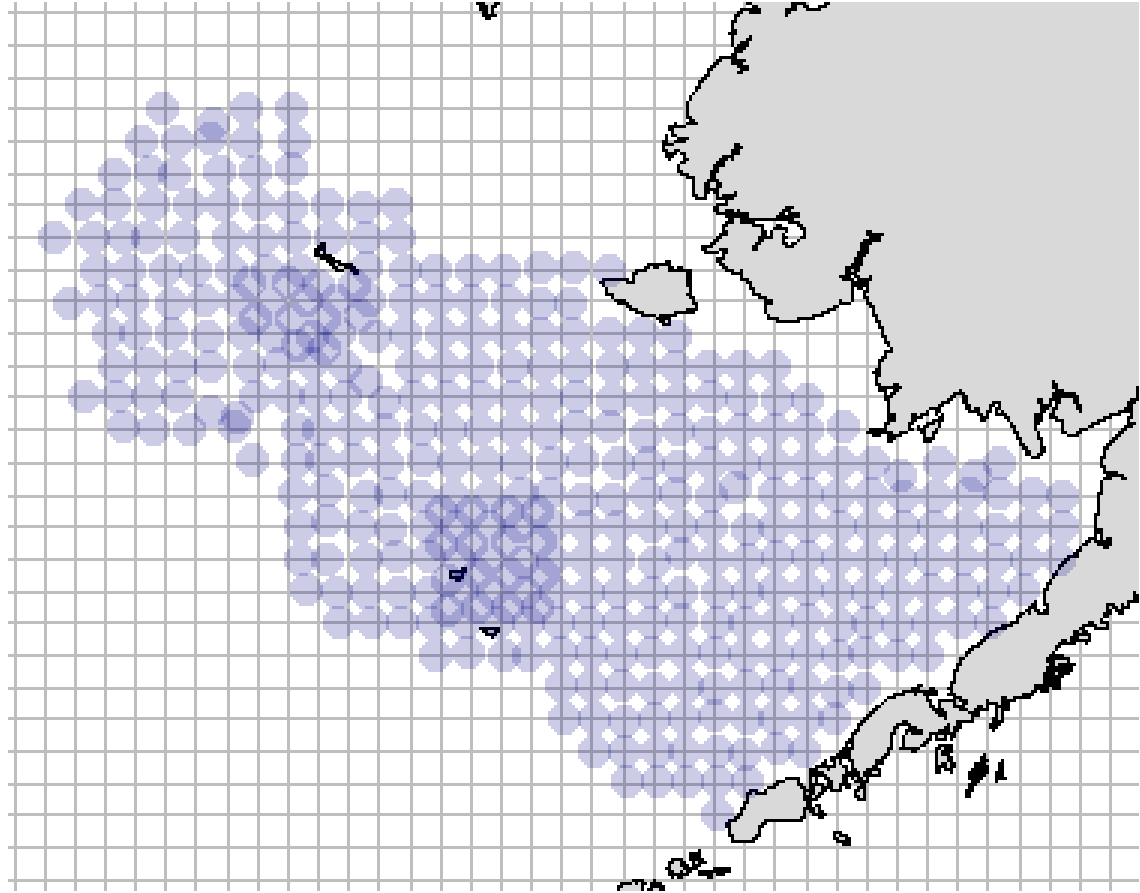
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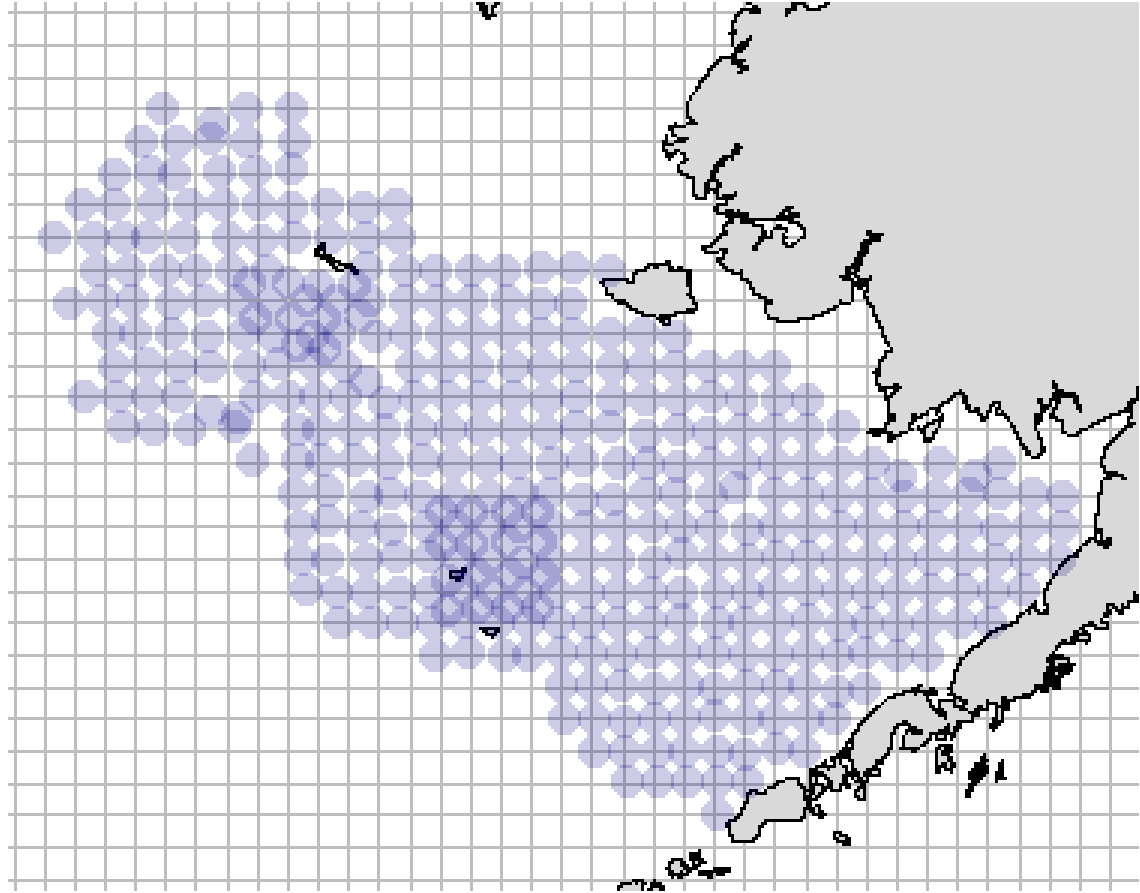
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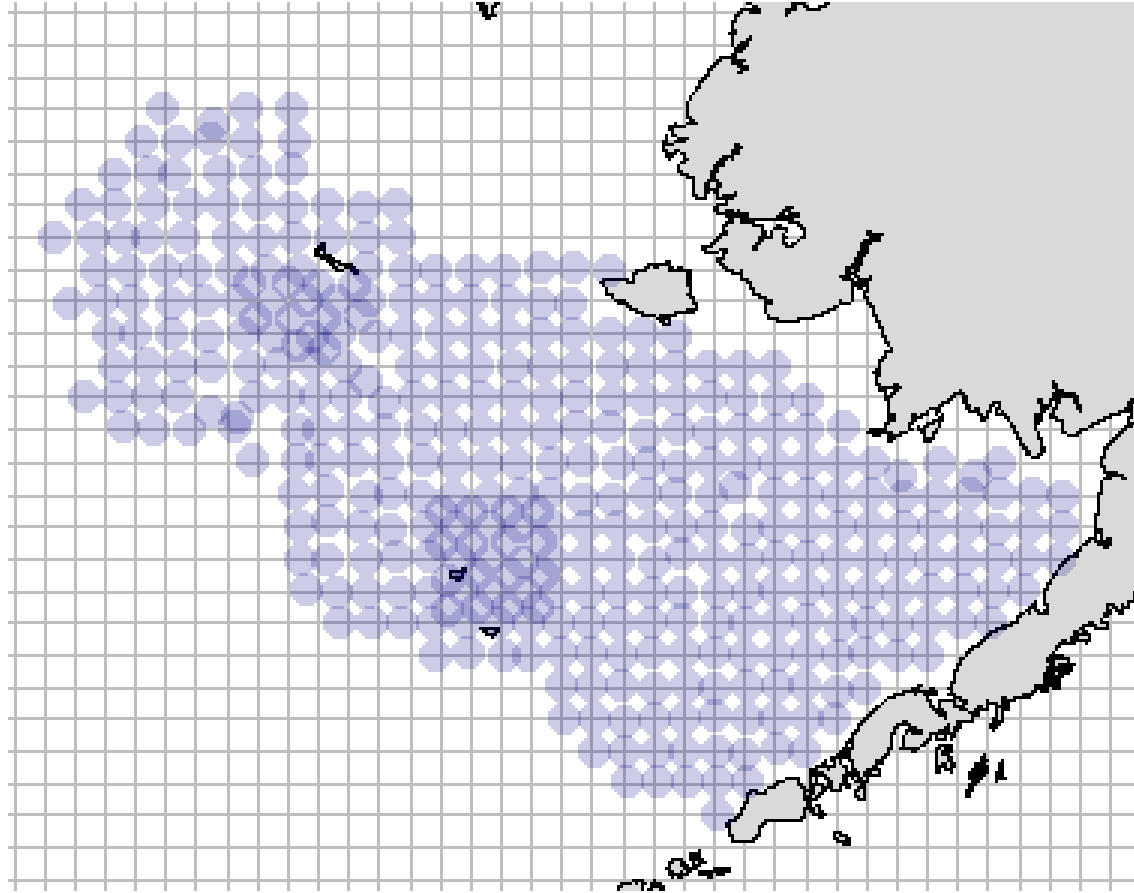
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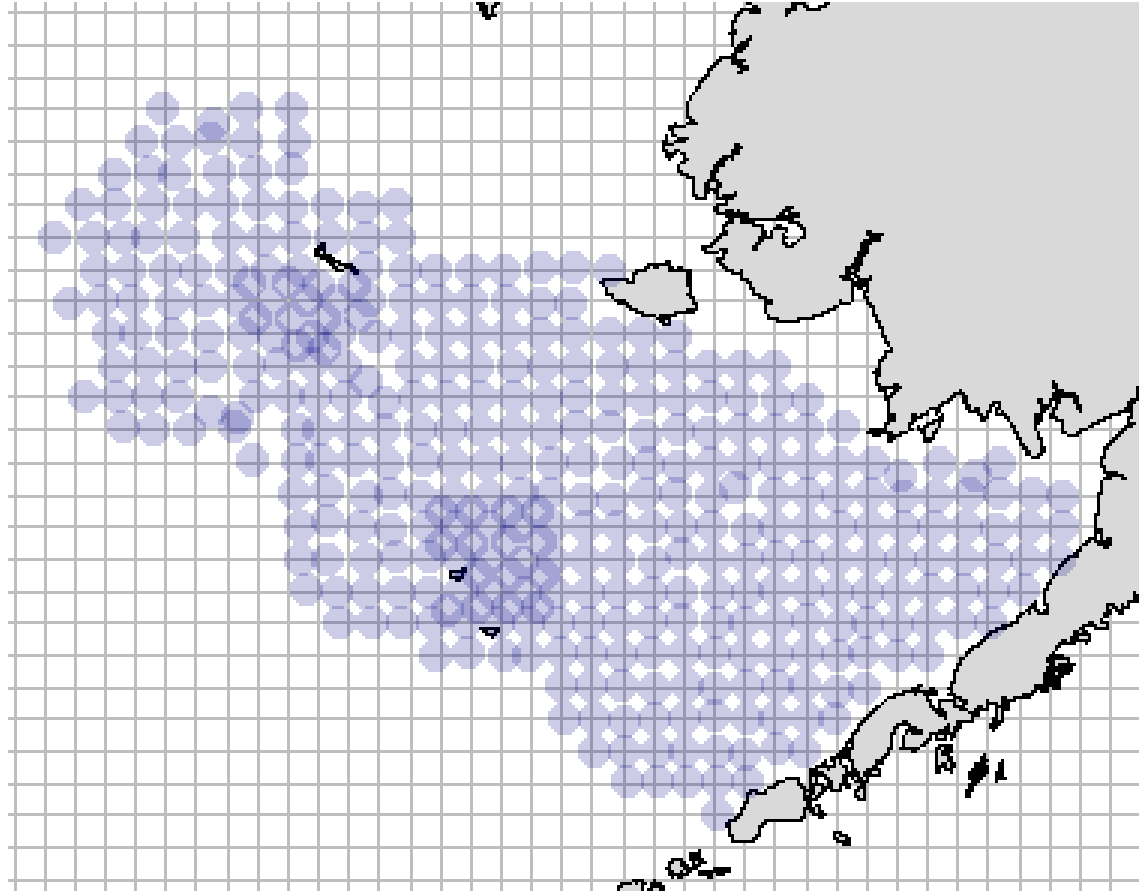
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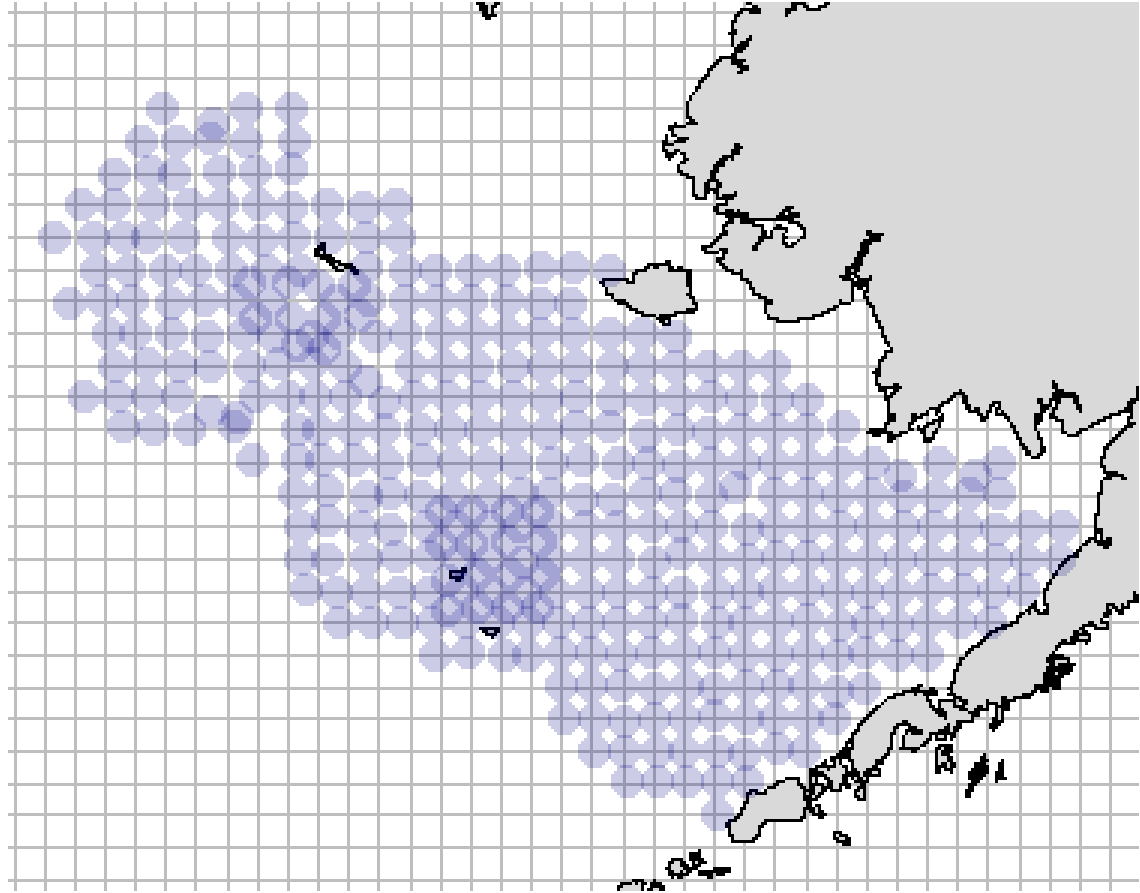
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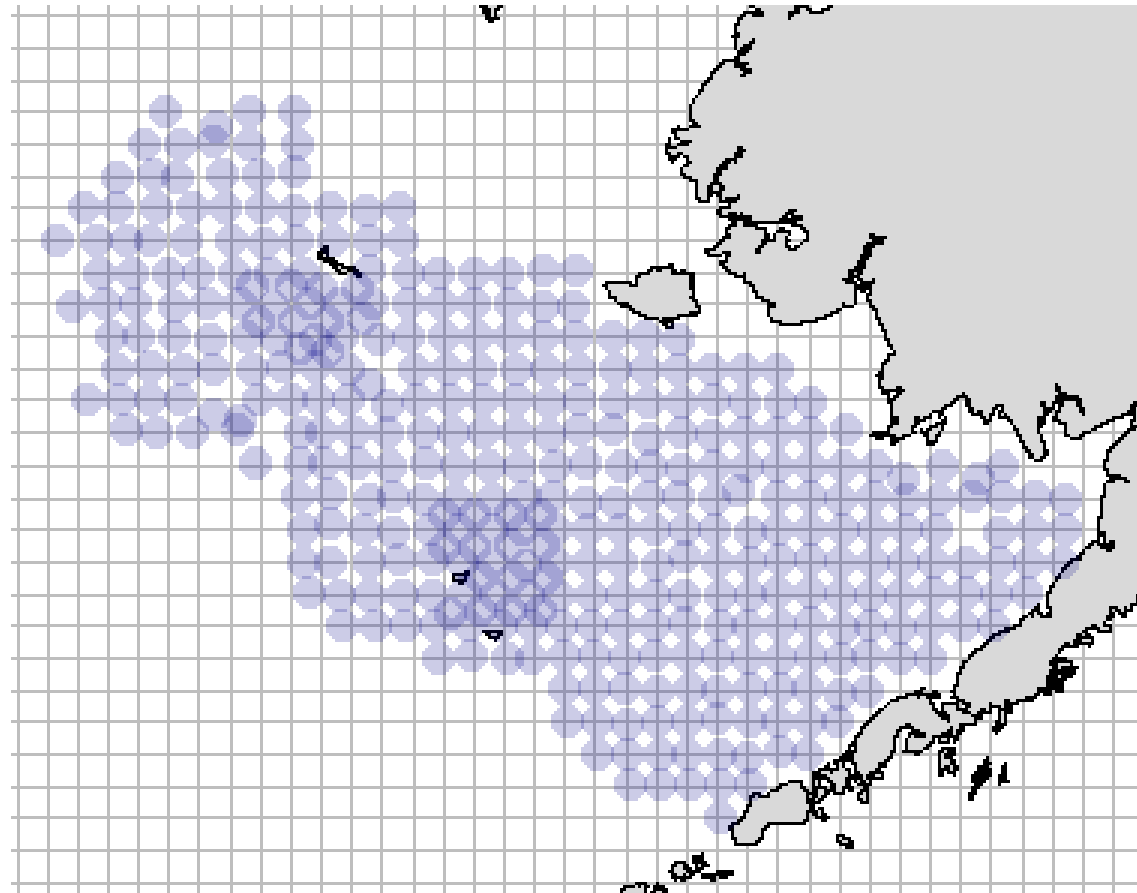
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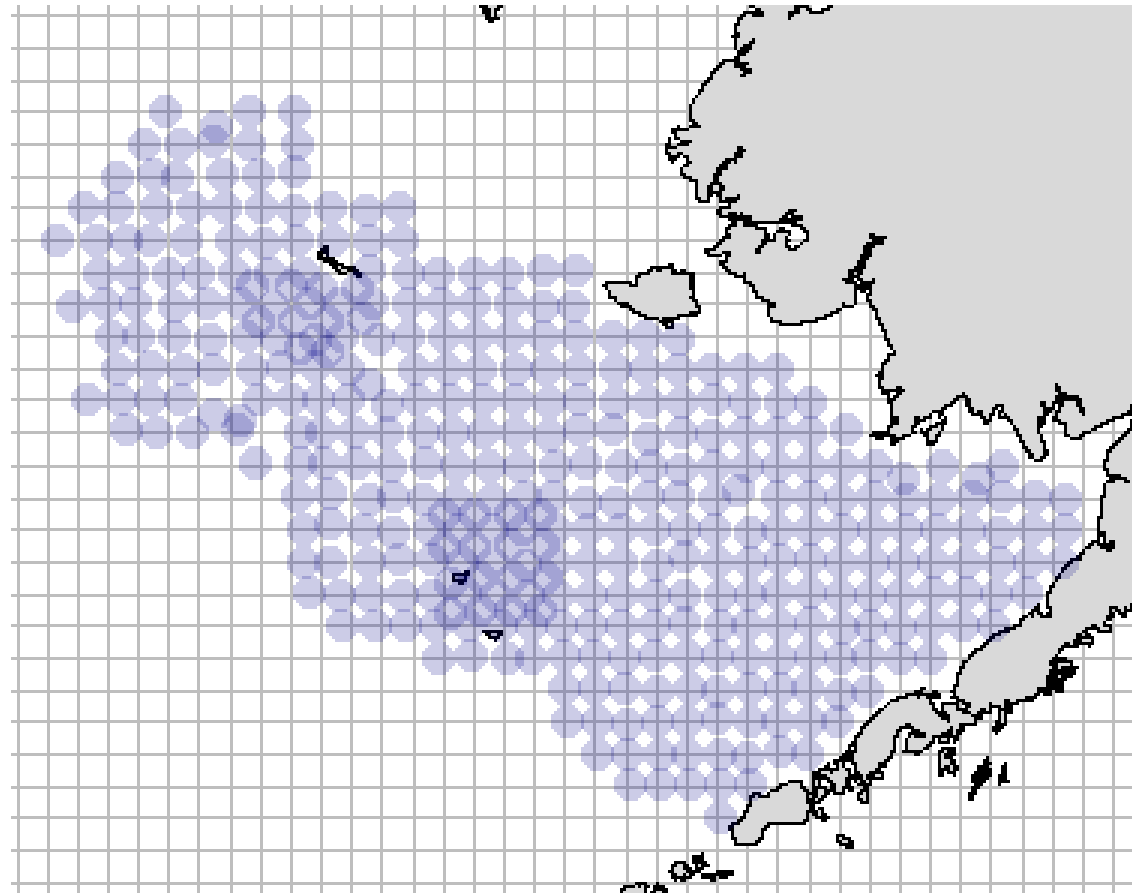
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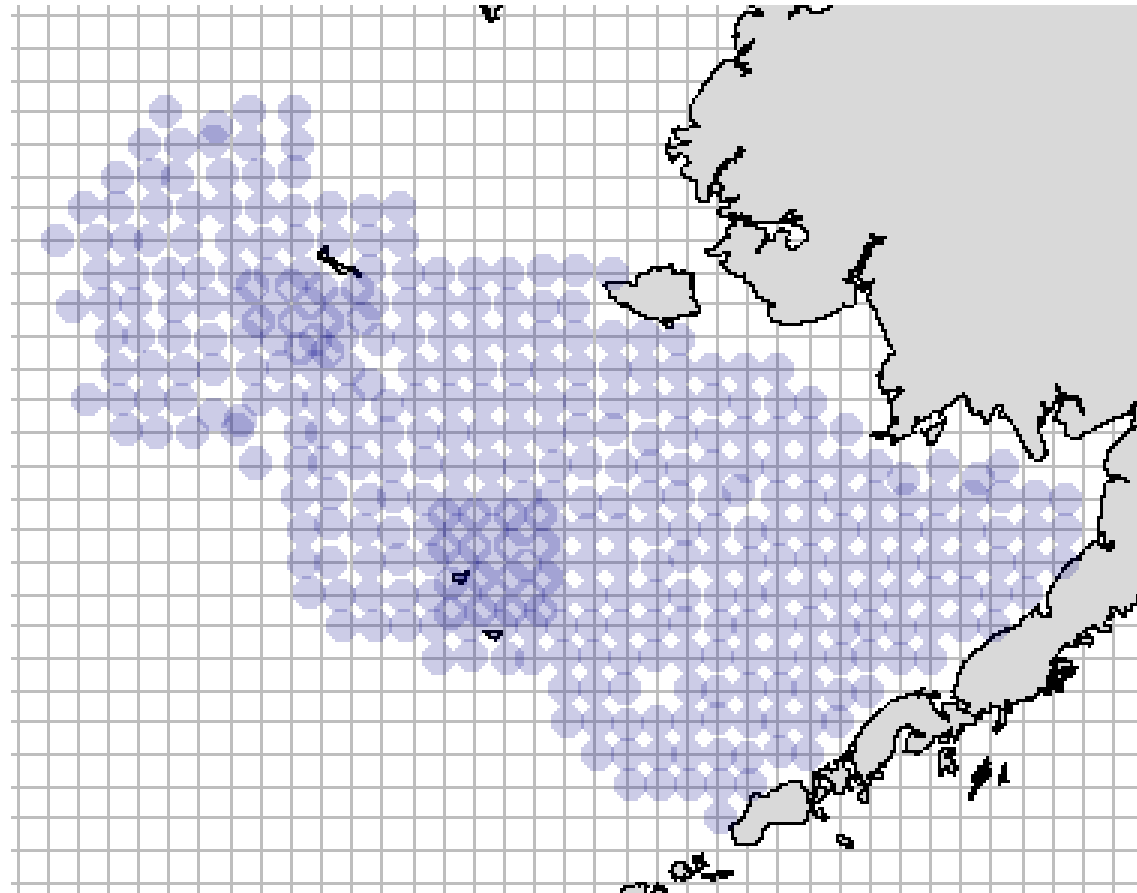
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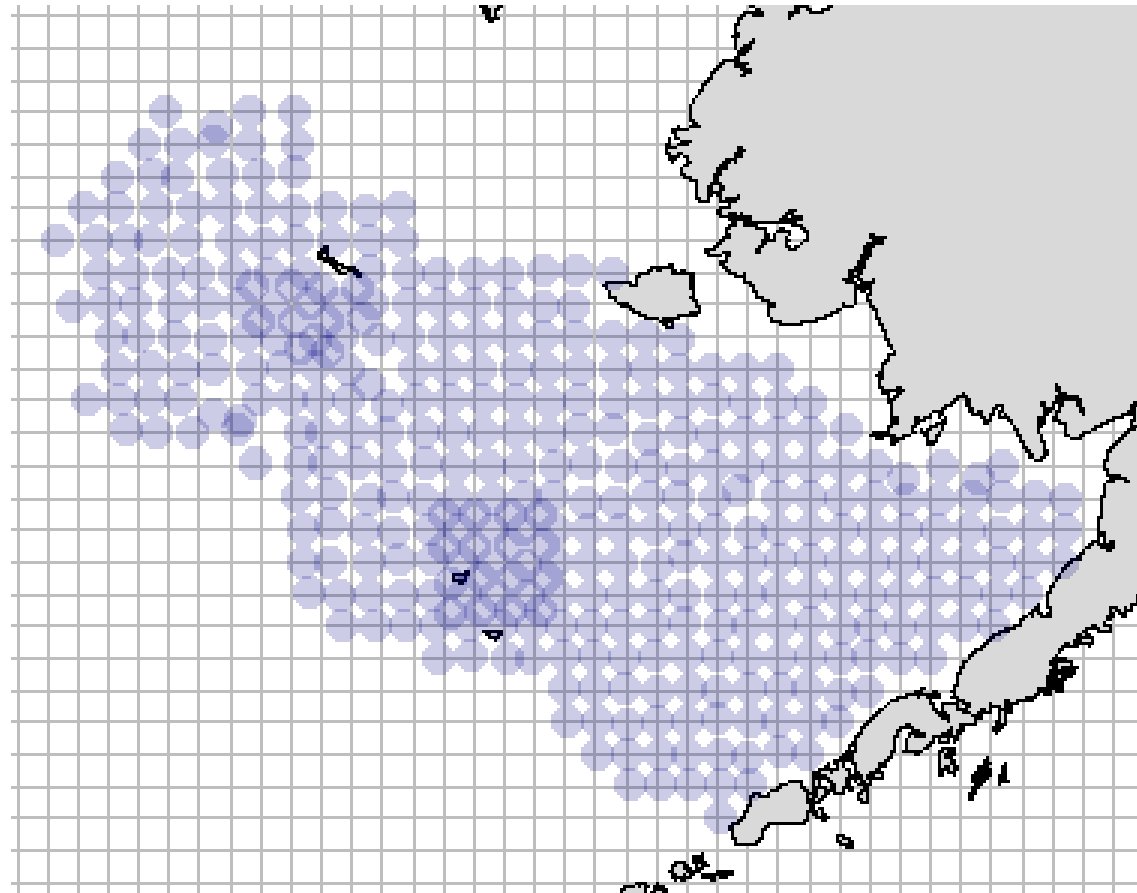
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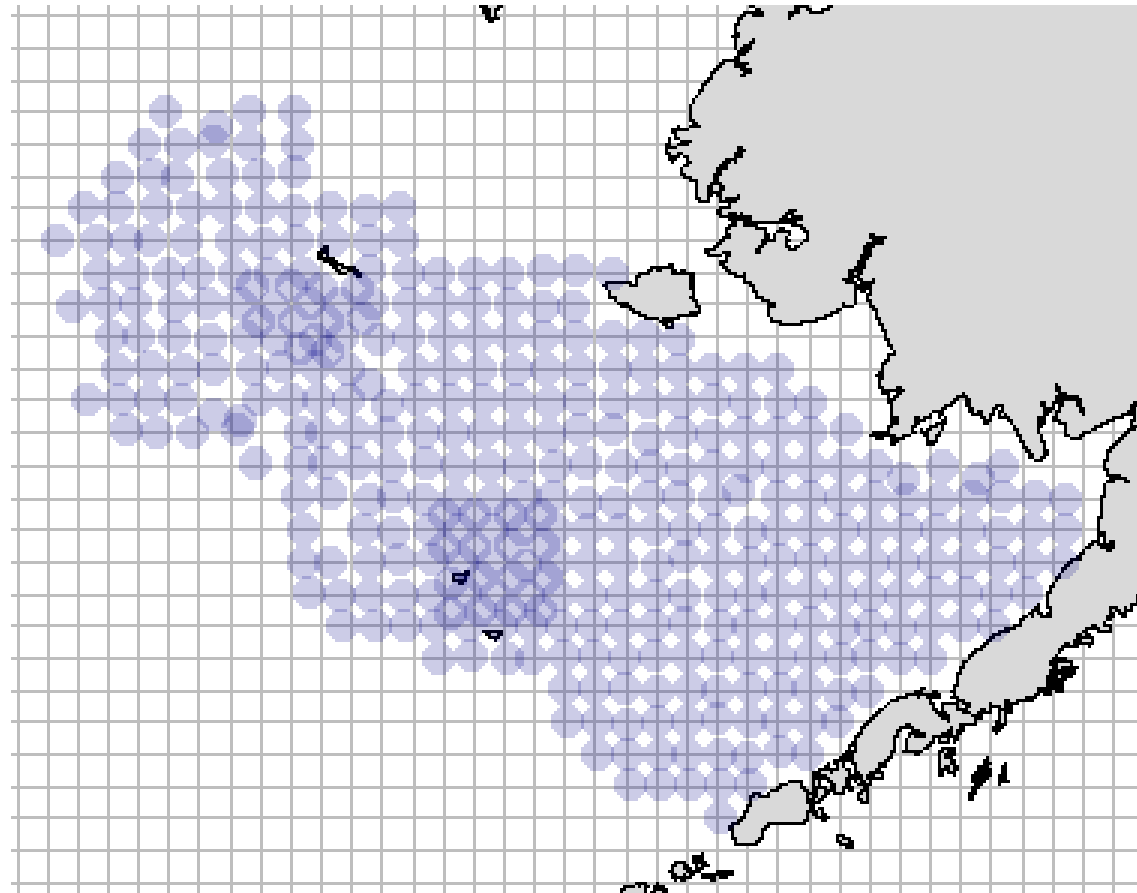
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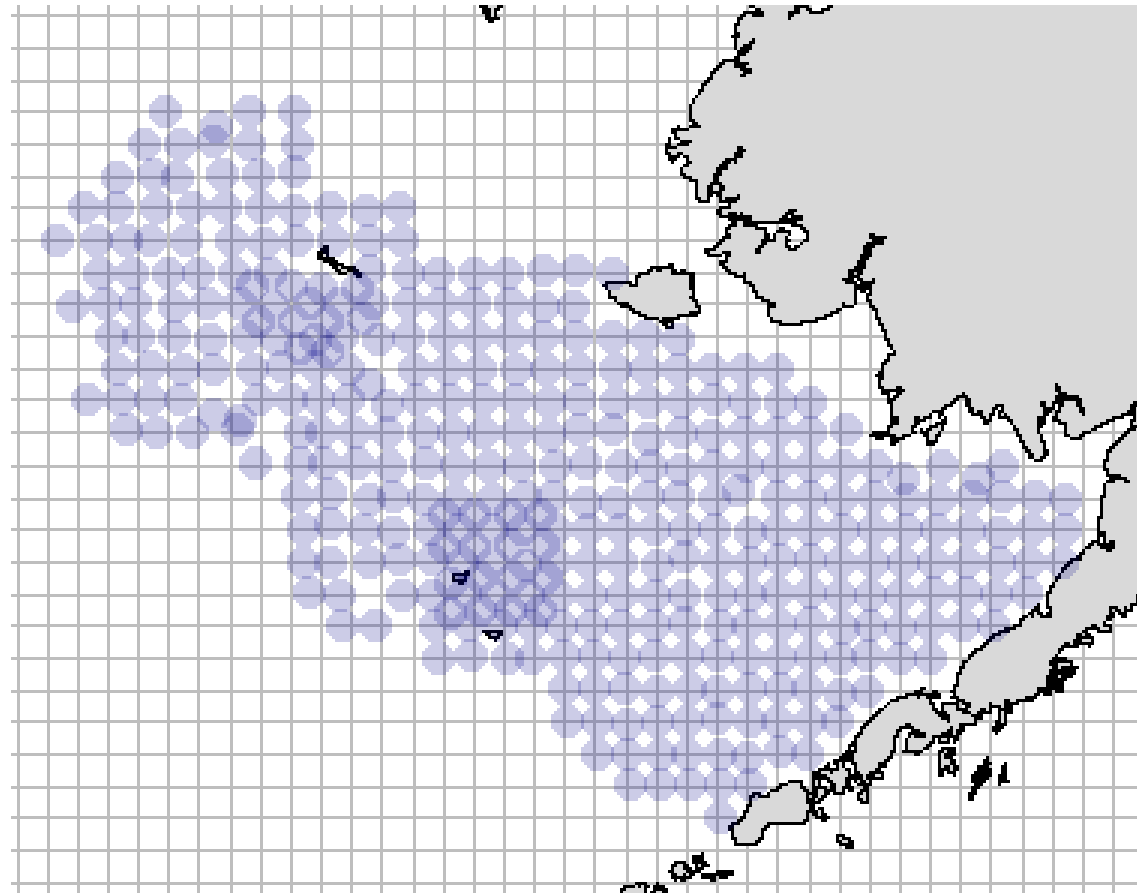
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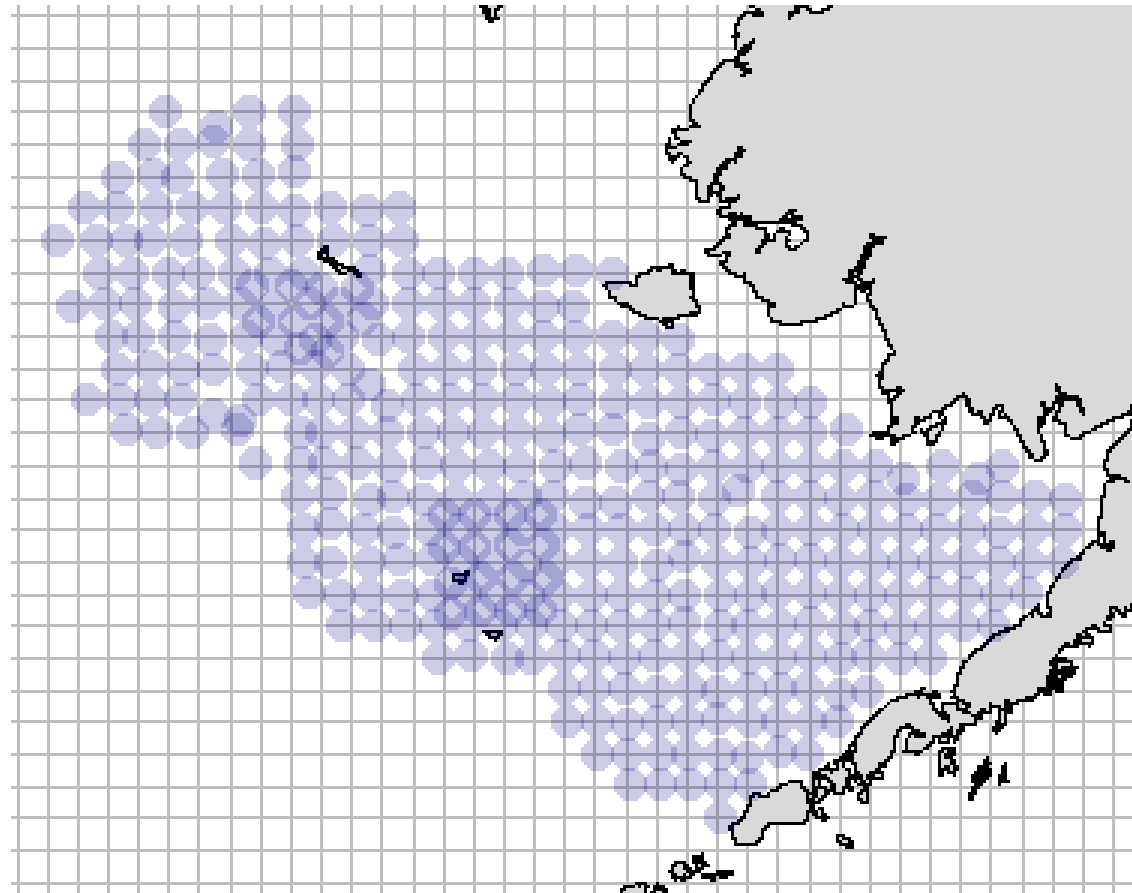
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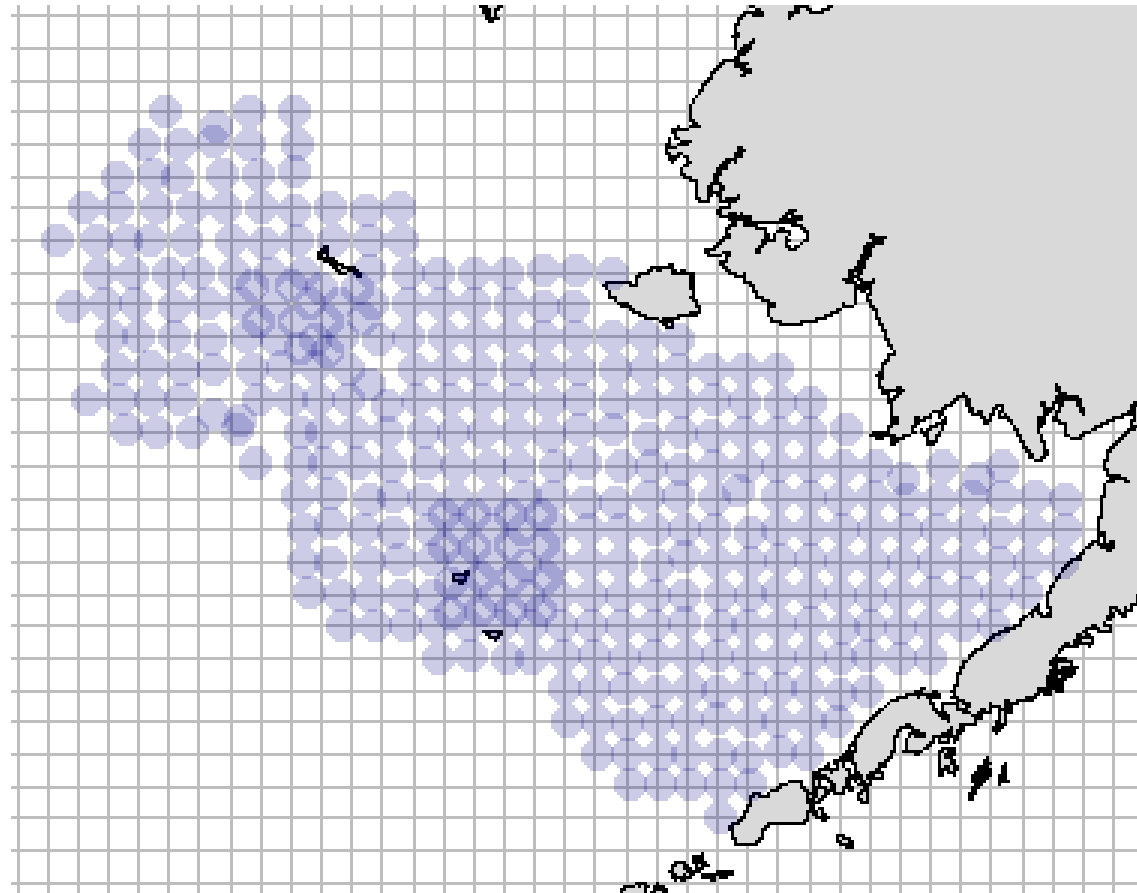
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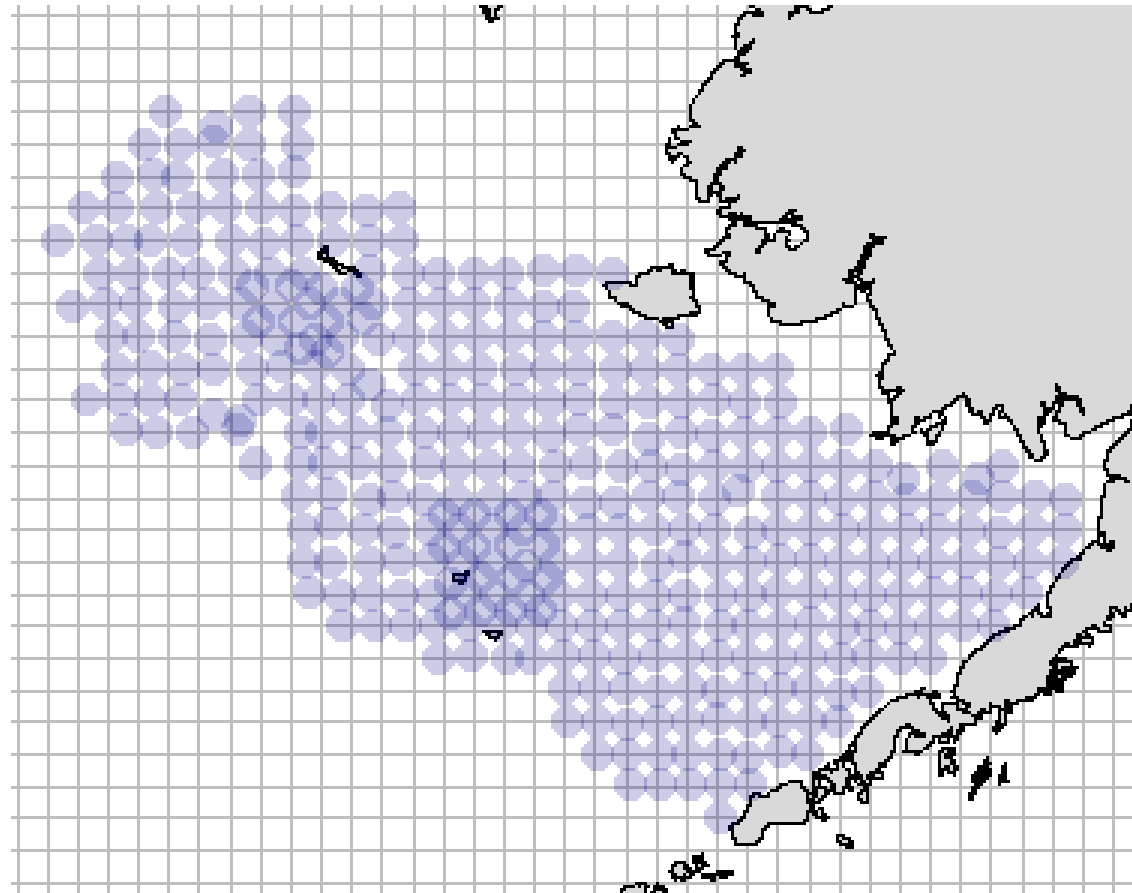
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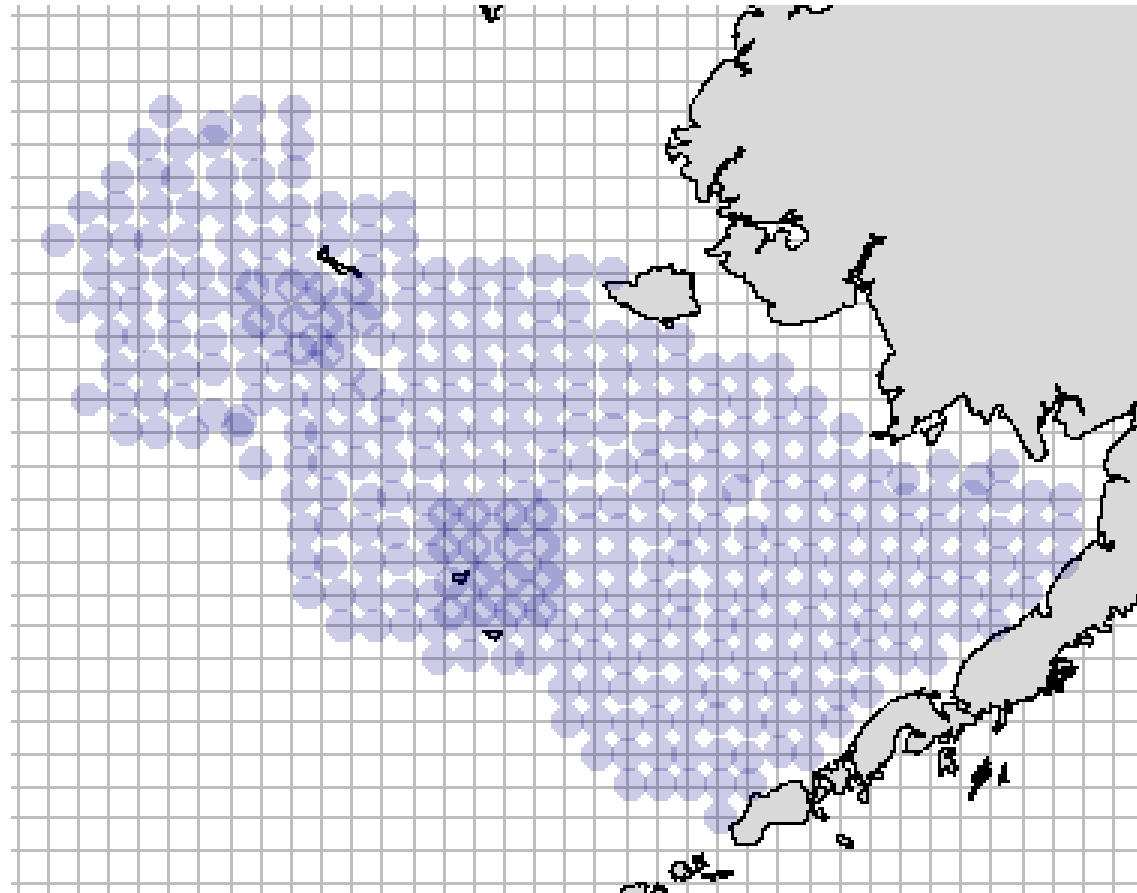
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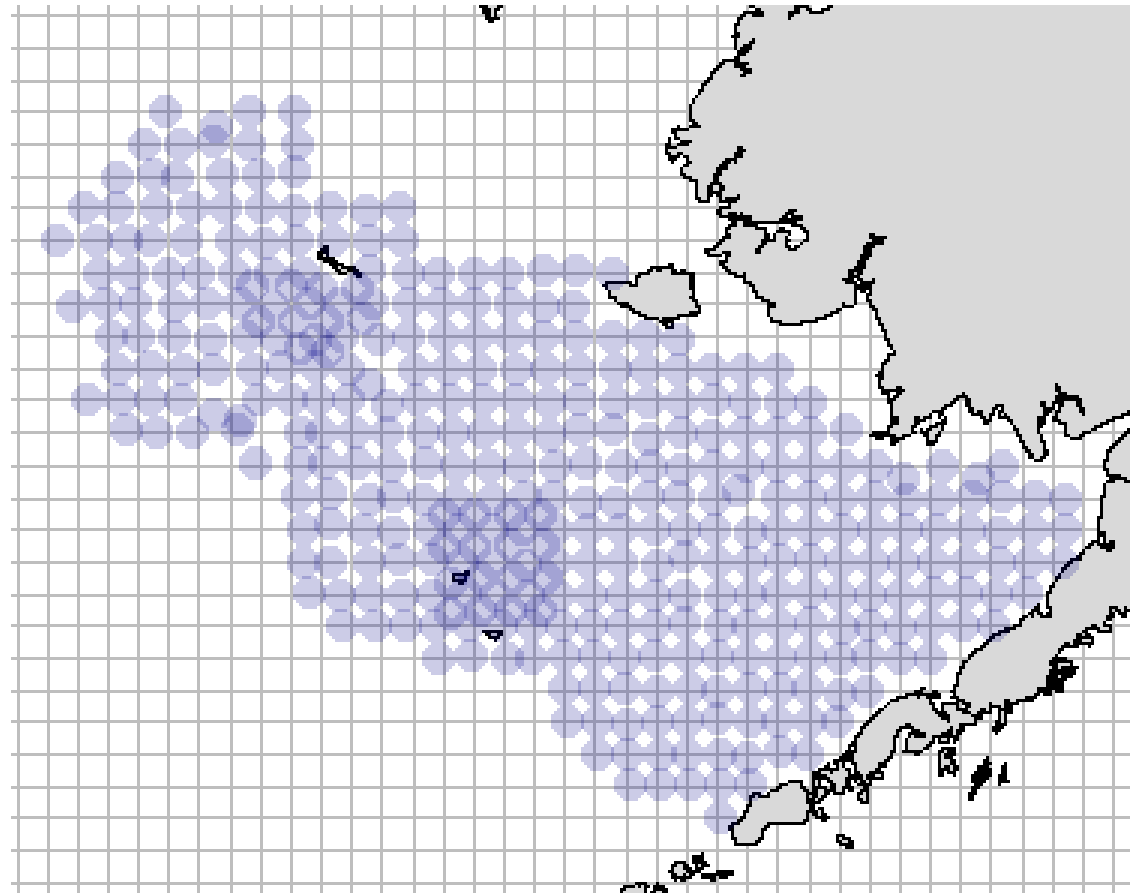
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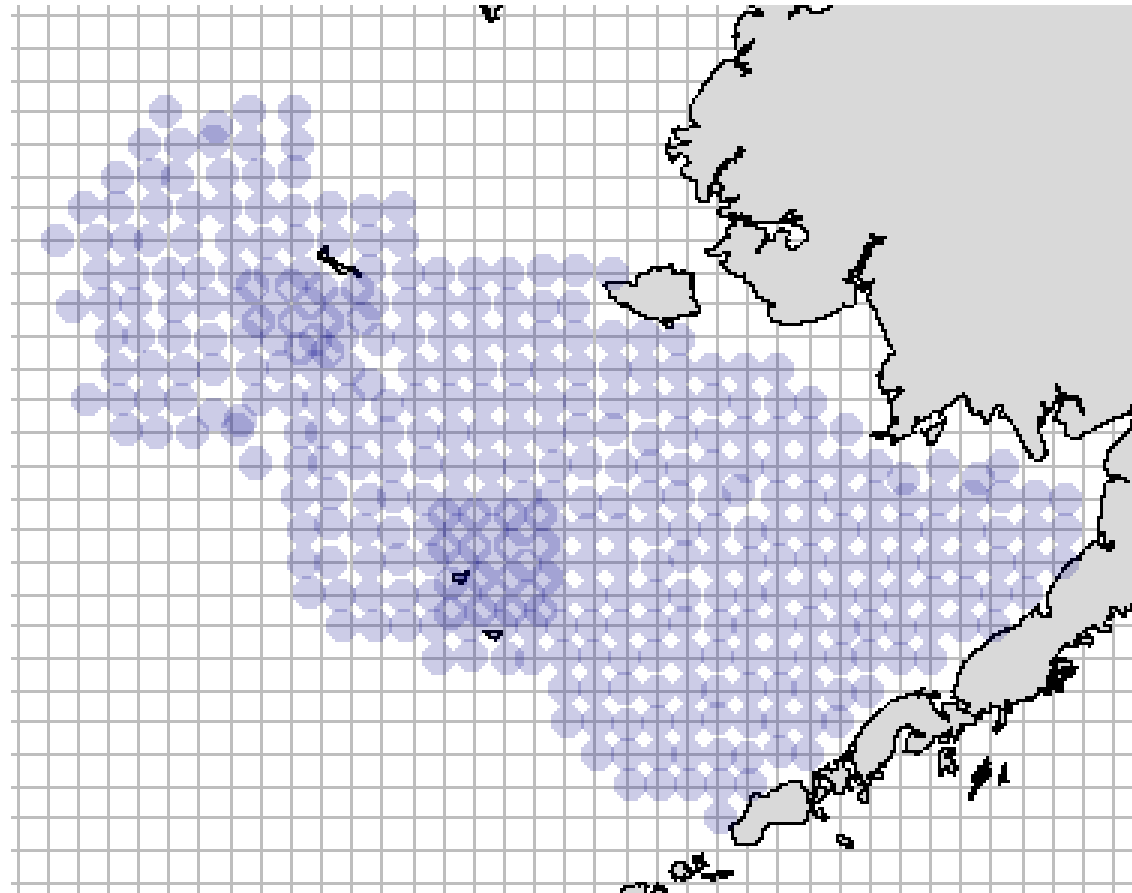
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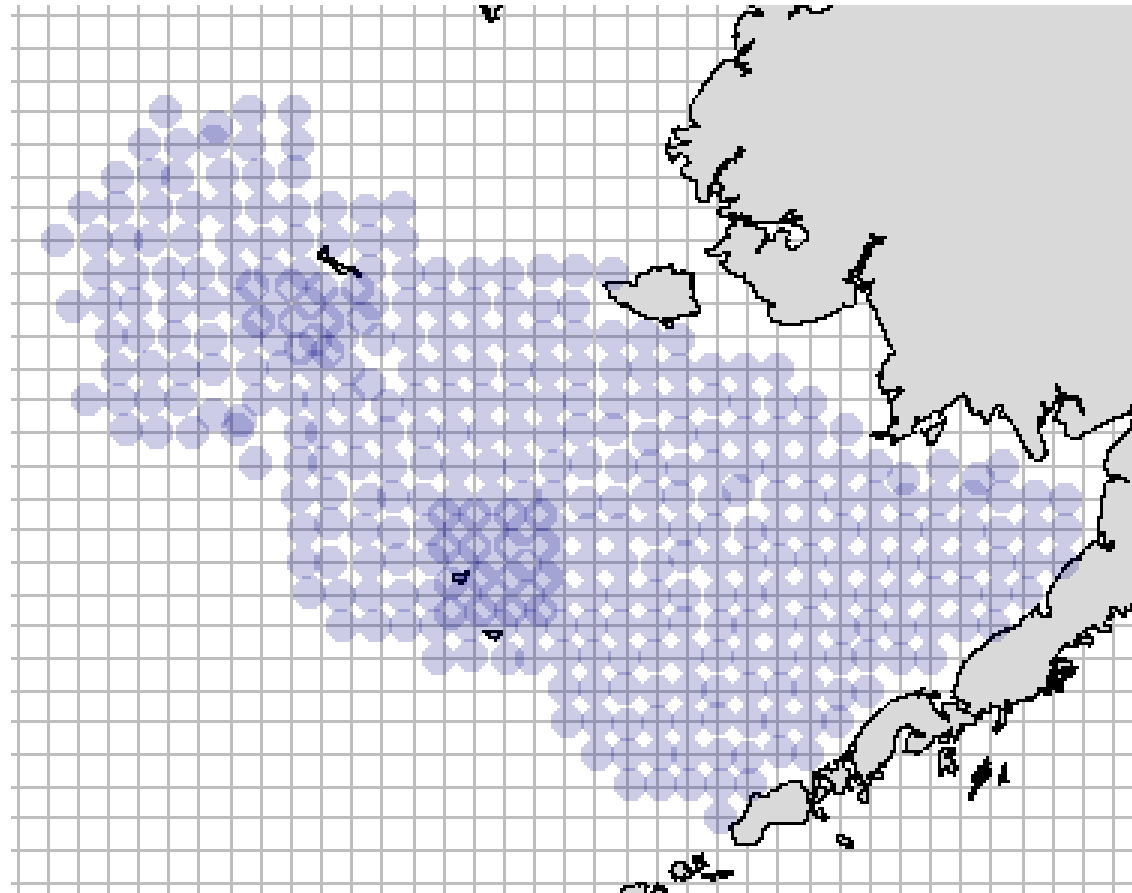
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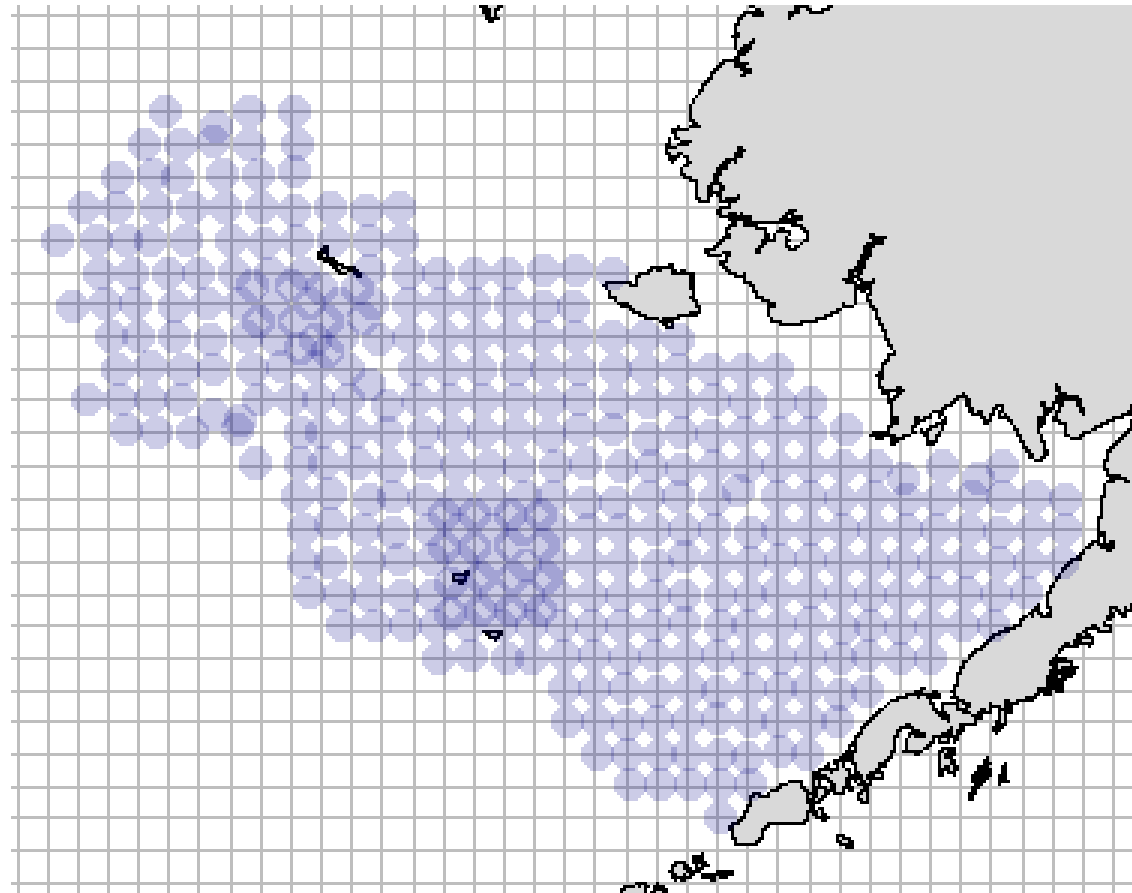
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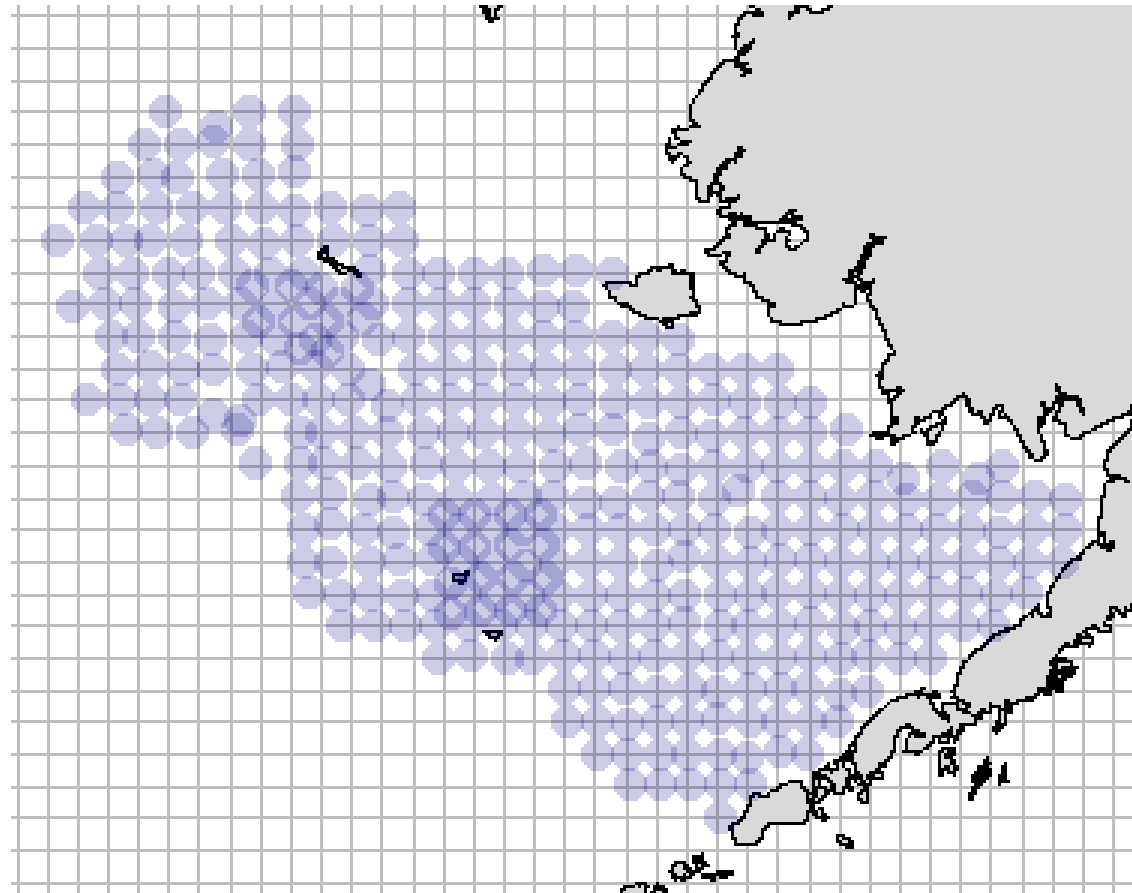
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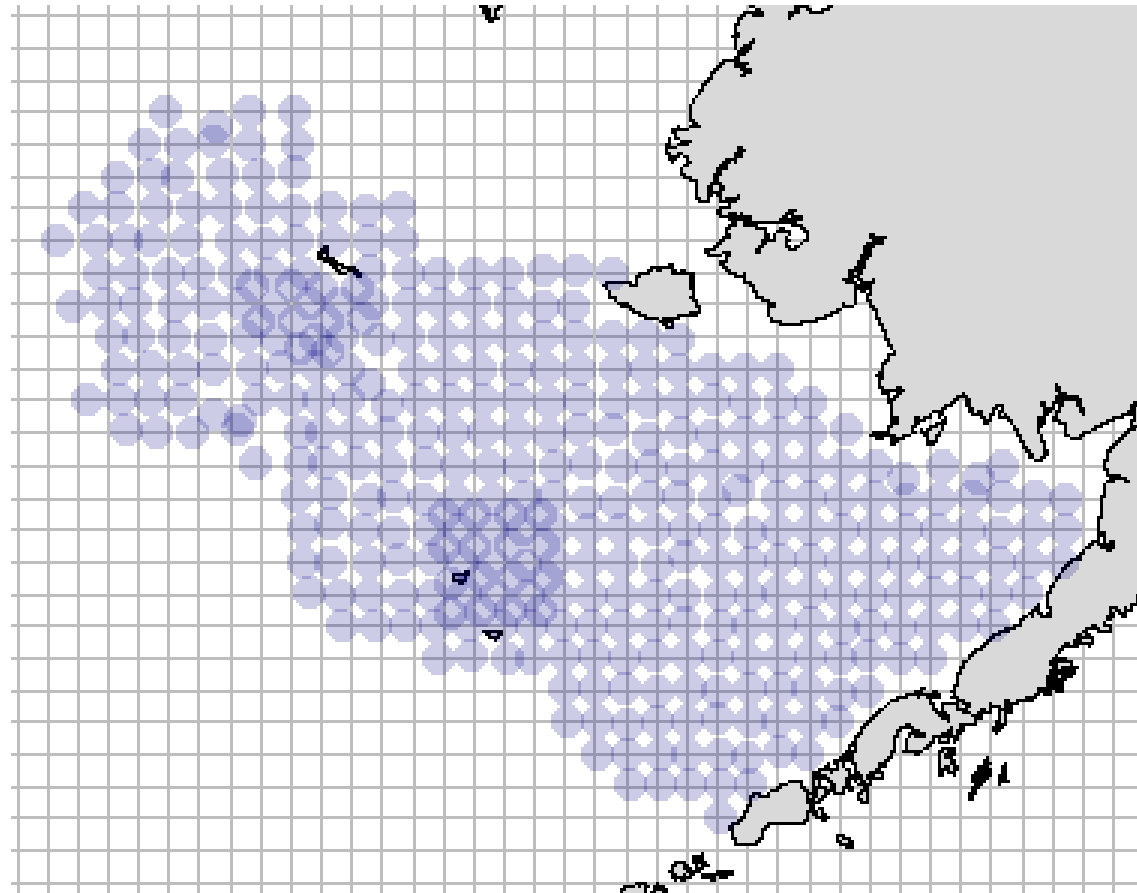
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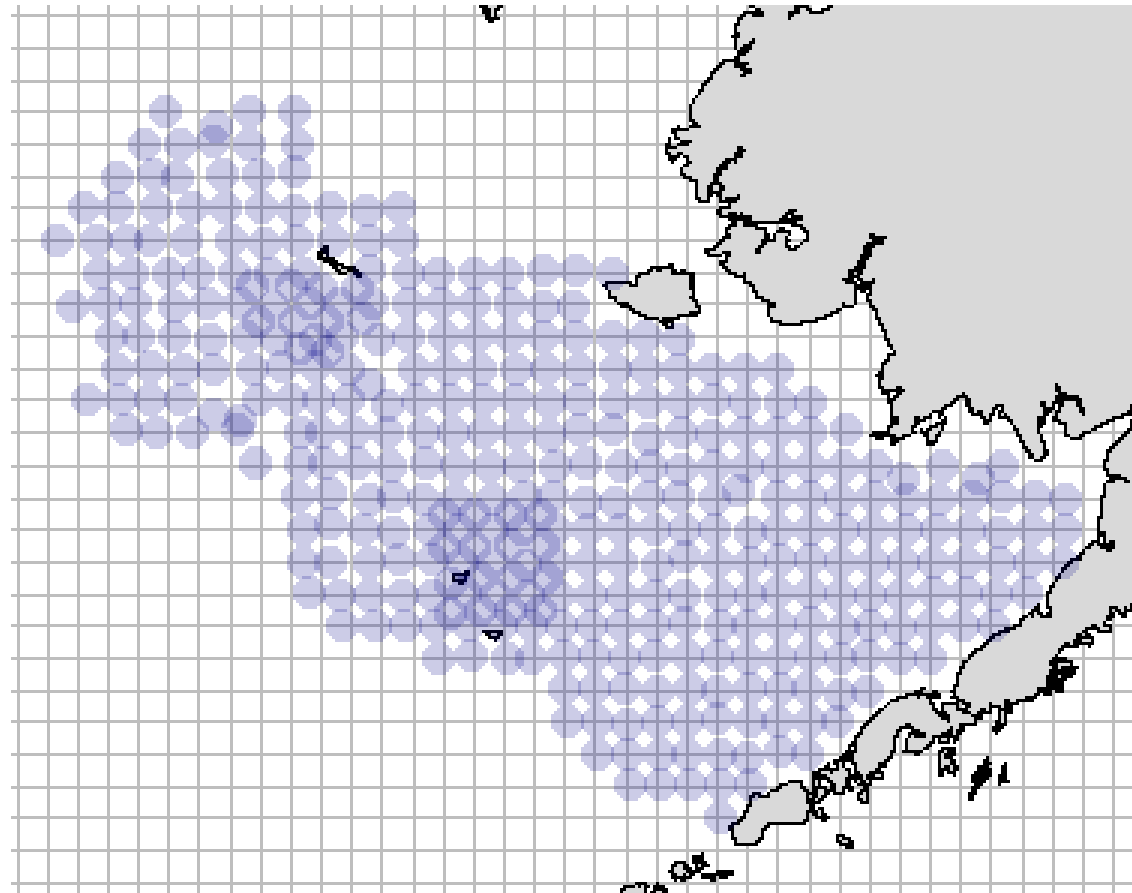
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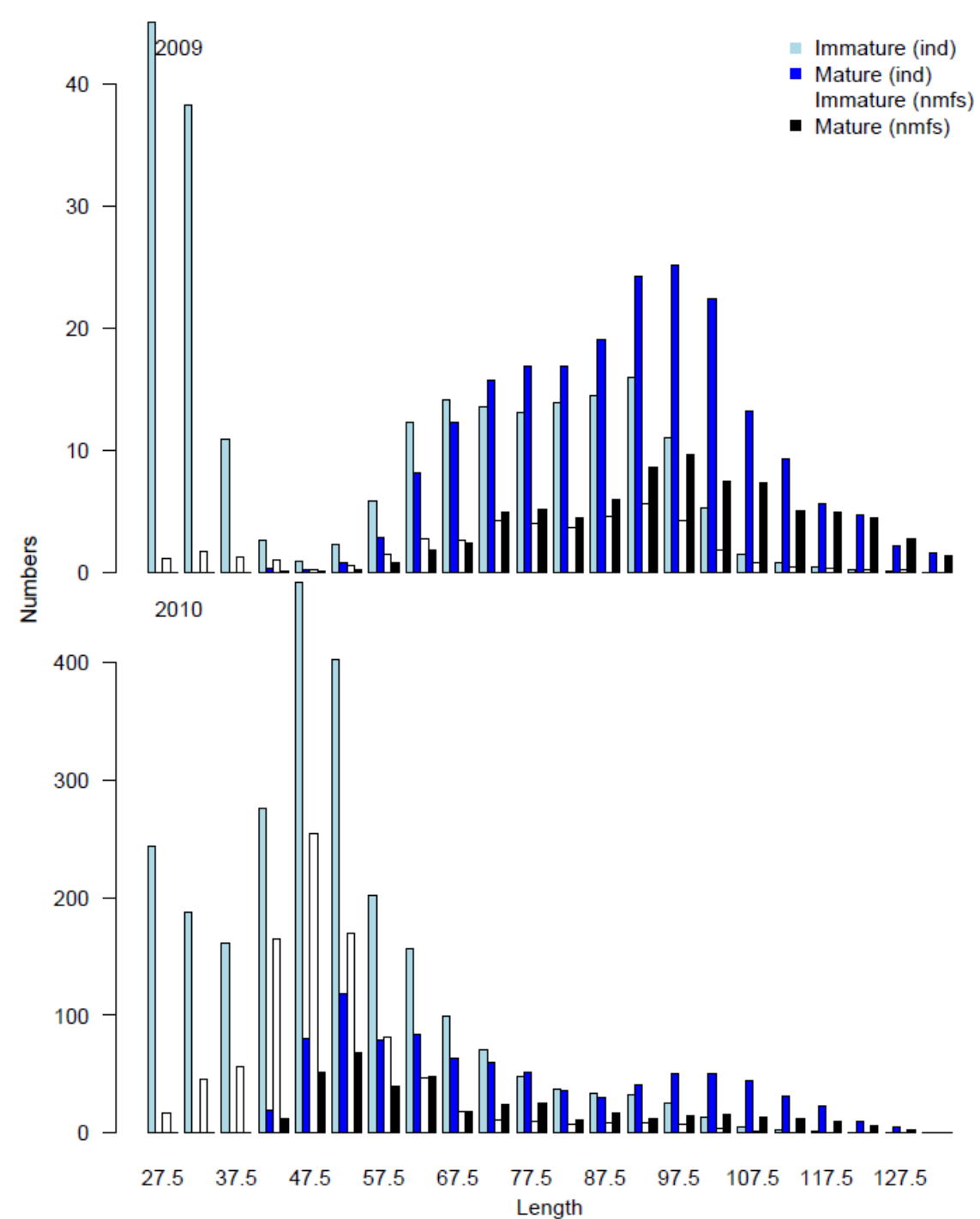
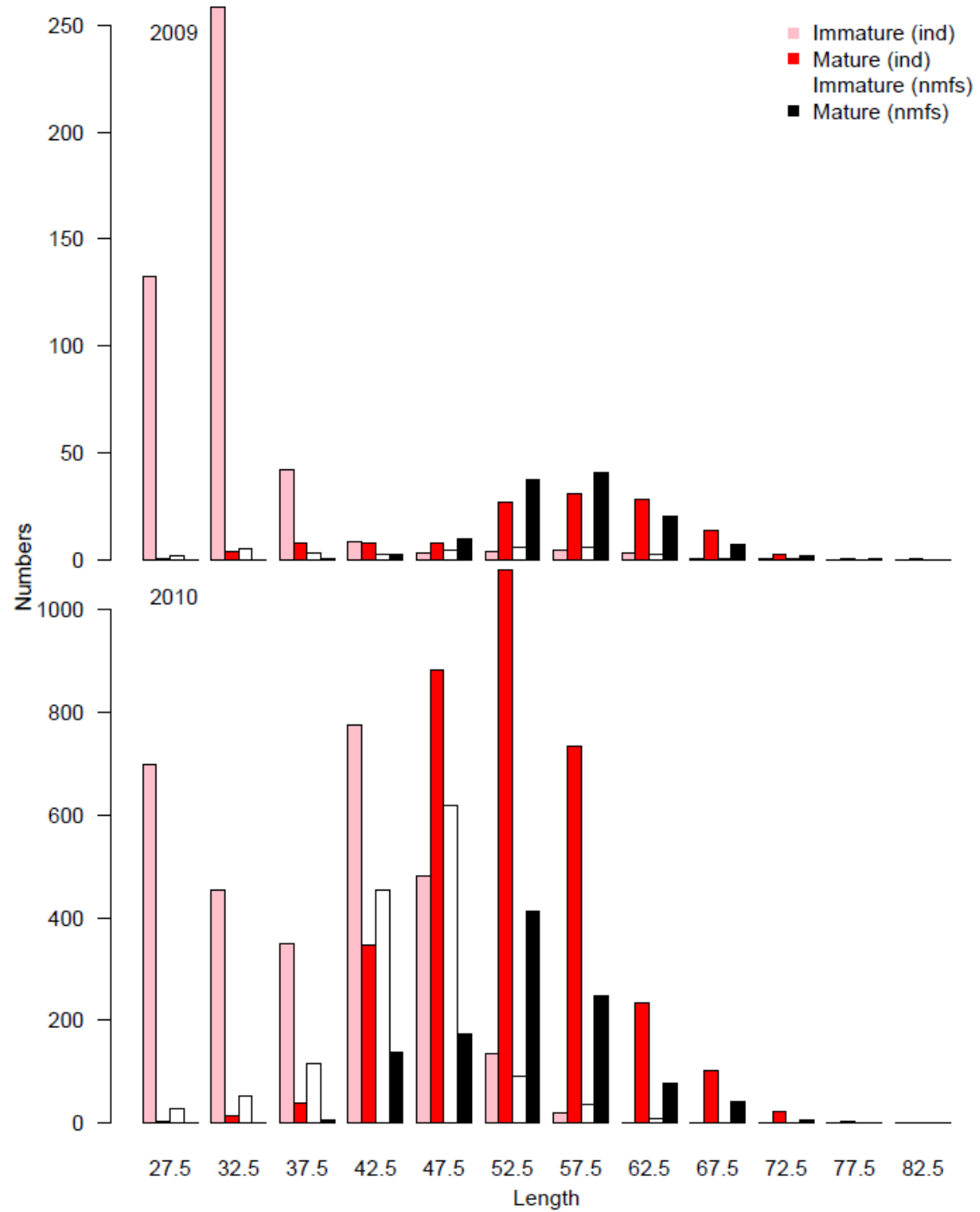


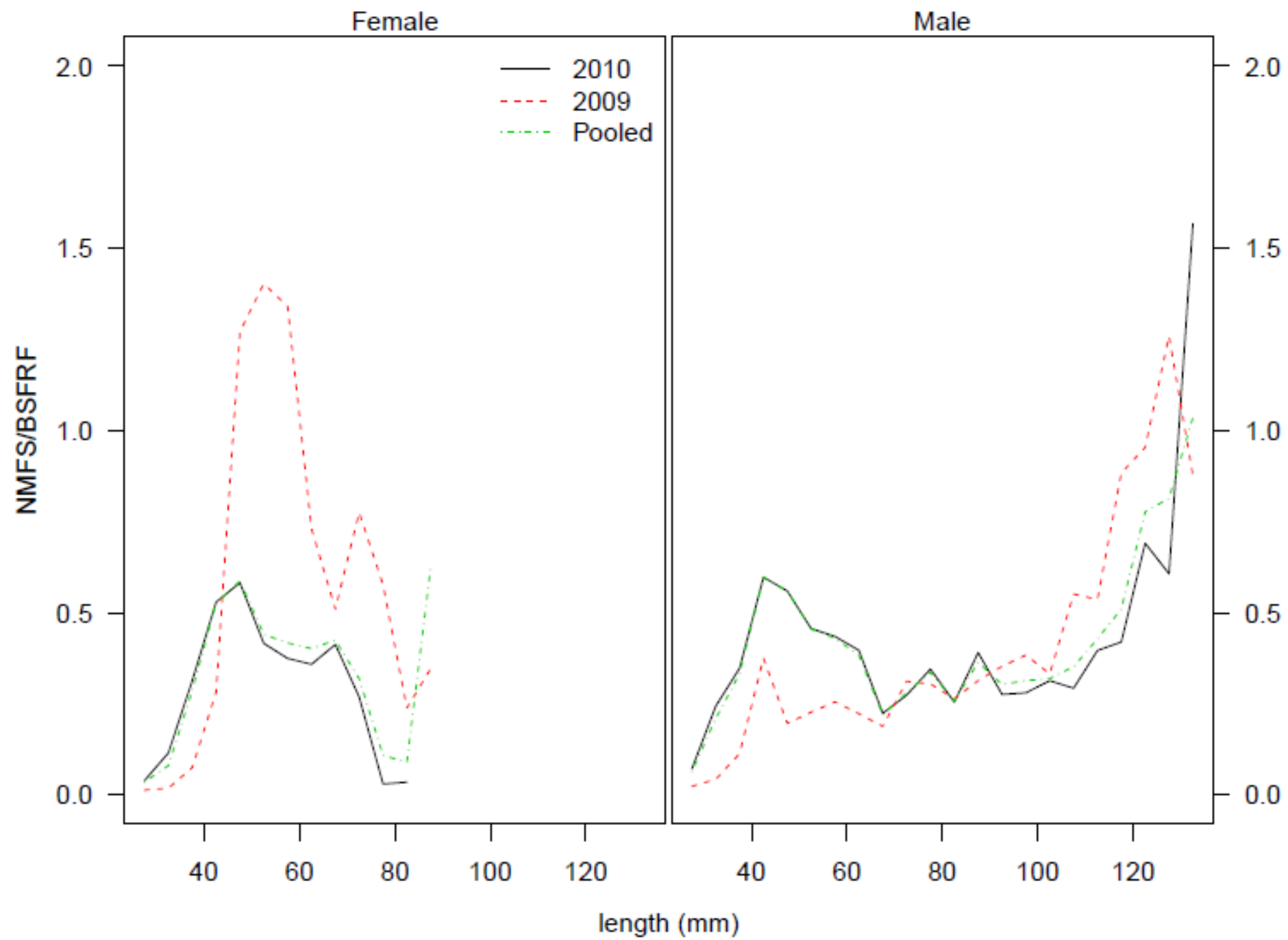
2015



2016

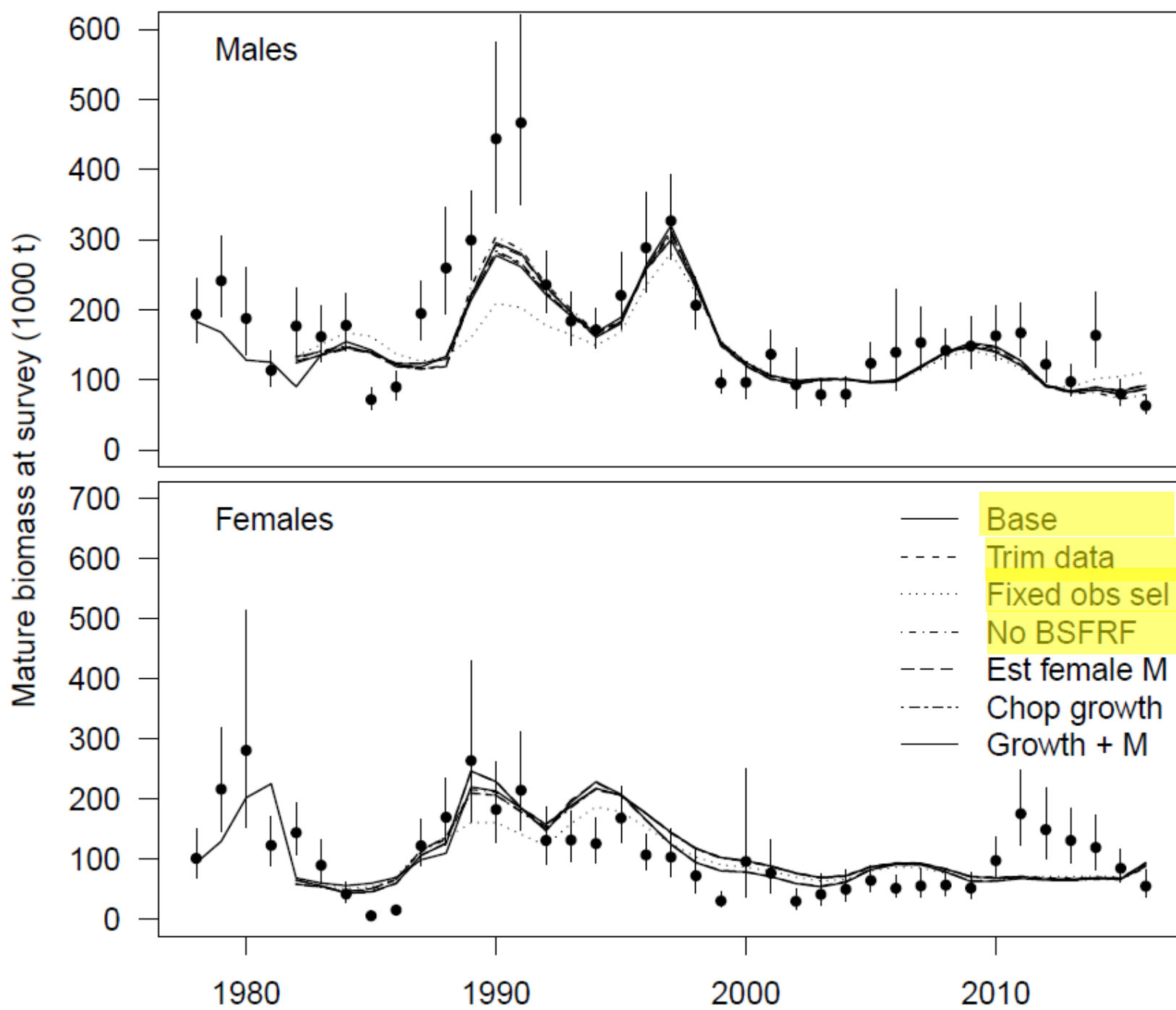






Model runs

- ‘Trim data’
 - Excludes all data from 1978-1981, start model in 1982
 - Explores problem of anchoring of q and bound hitting parameters
- ‘Fixed obs sel’
 - ‘Trim data’ + fixing survey selectivity in era 2 and era 3 to selectivity inferred from BSFRF data
 - Explores implications of BSFRF data
- ‘No BSFRF’
 - ‘Trim data’ + setting the weights for the BSFRF likelihood components to 0
 - Explores the impact of the BSFRF data on model output



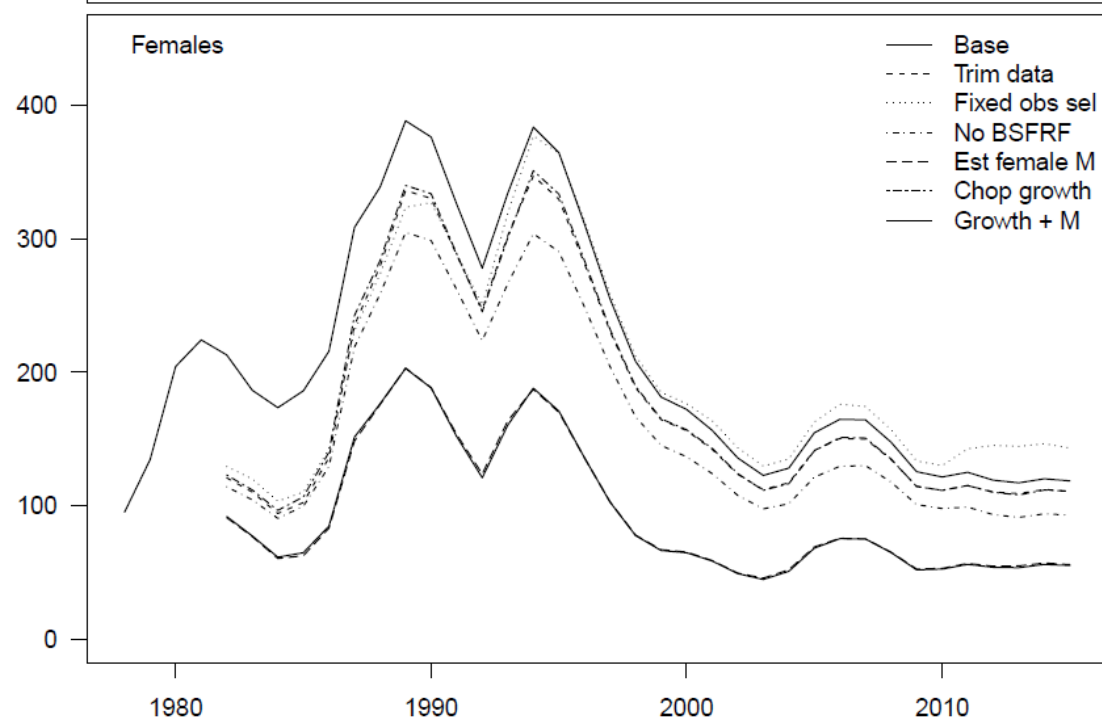
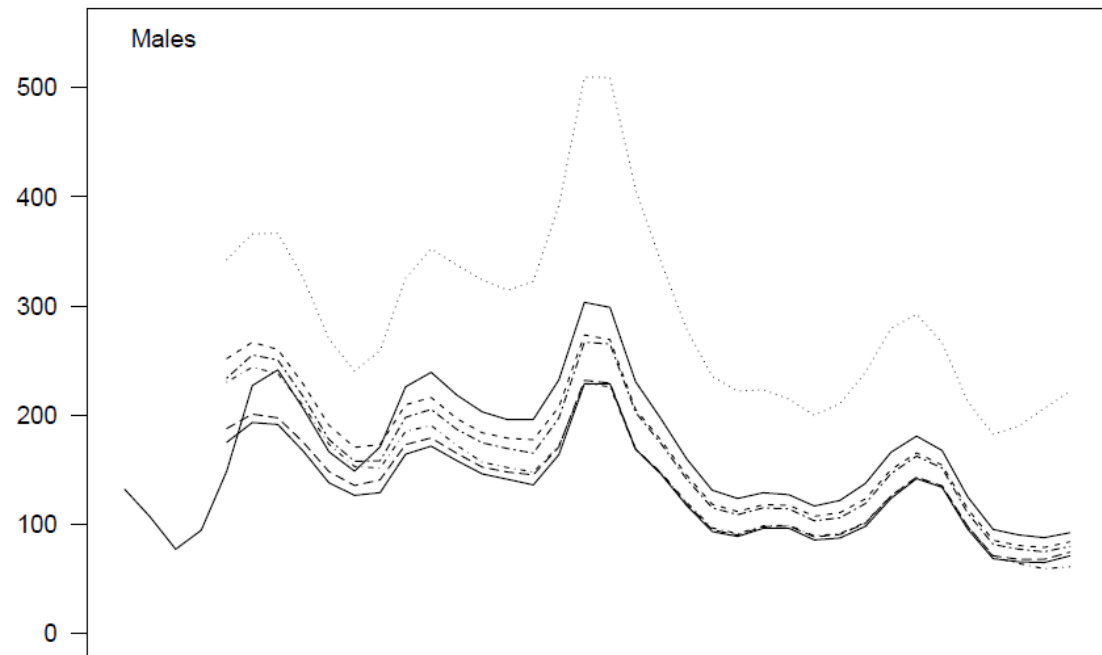
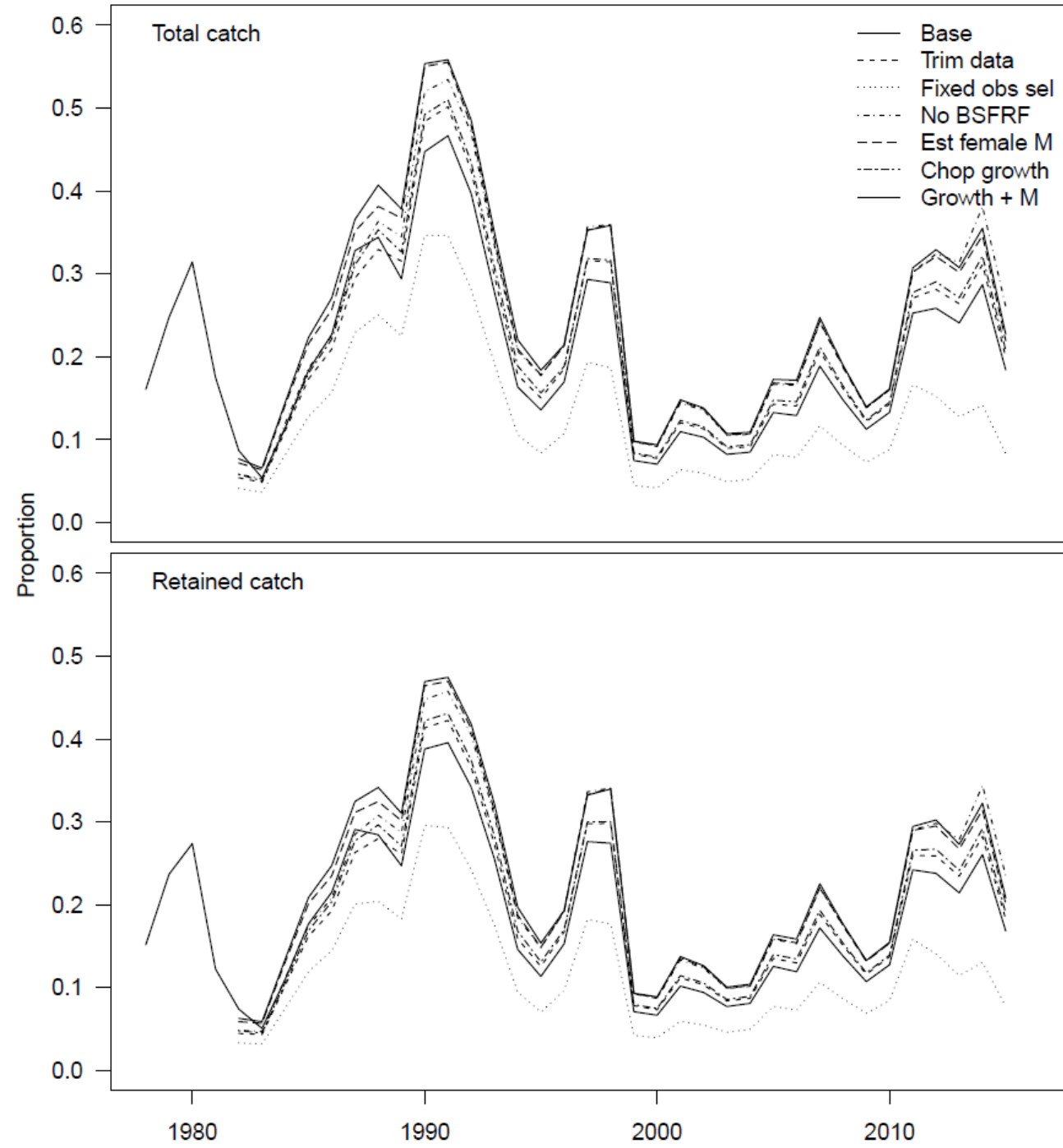
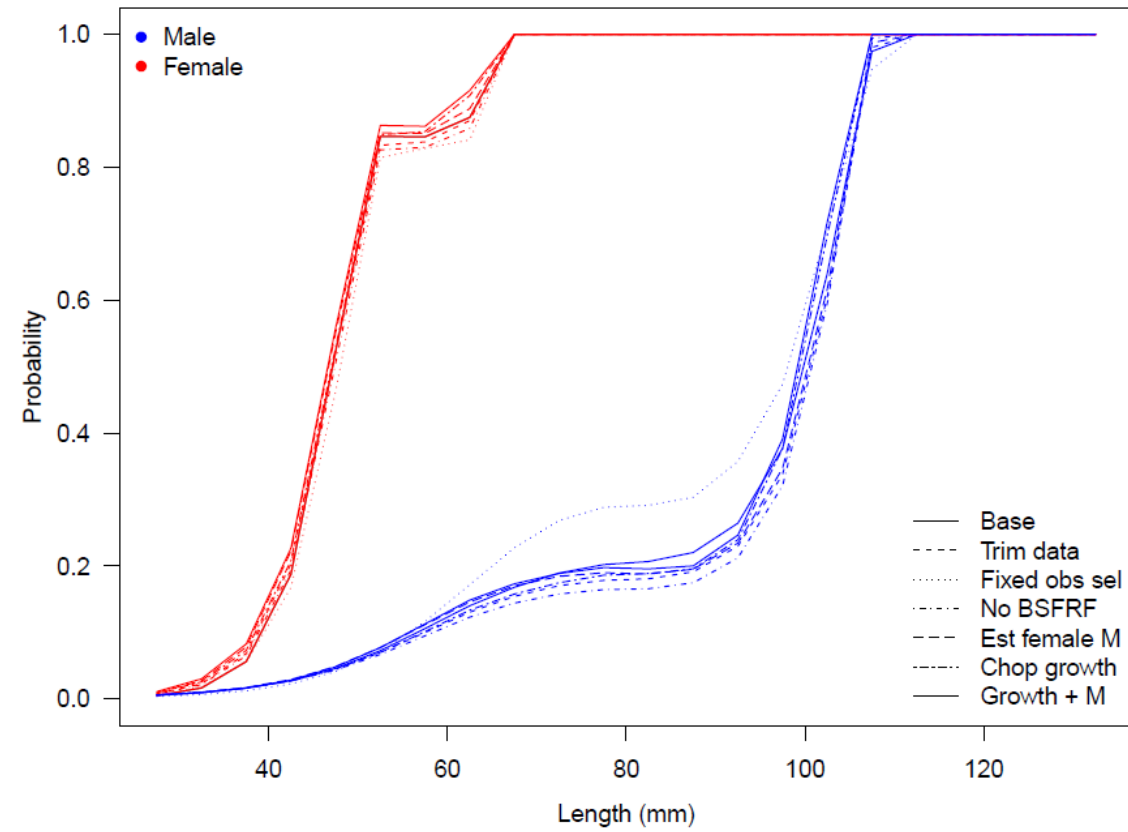
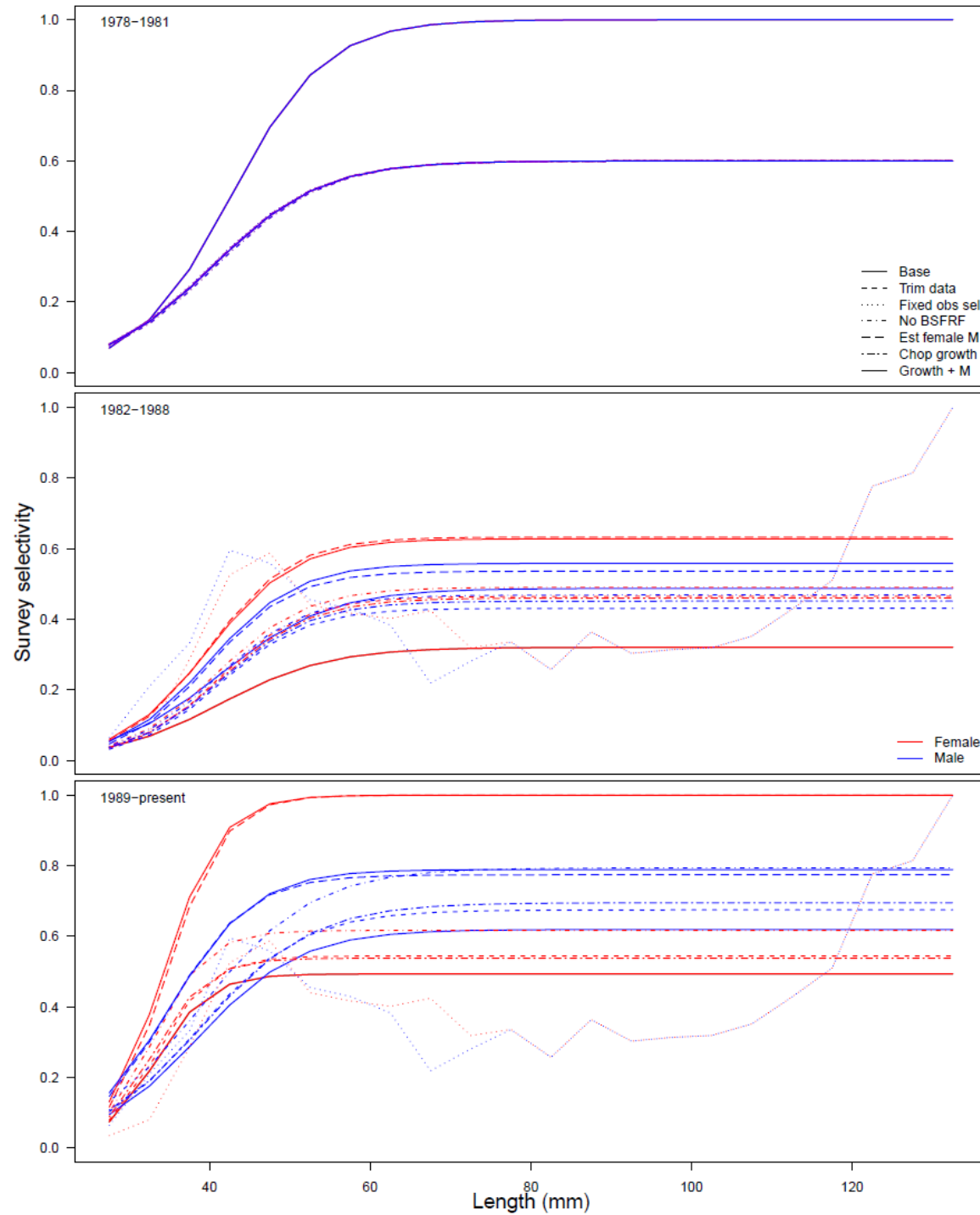


Table 1: Changes in management quantities for each scenario considered. Reported quantities are the MLEs because running MCMC for every model was prohibitively time-consuming. The MLEs for scenarios in which MCMCs were performed are very close to the medians of the posterior distributions.

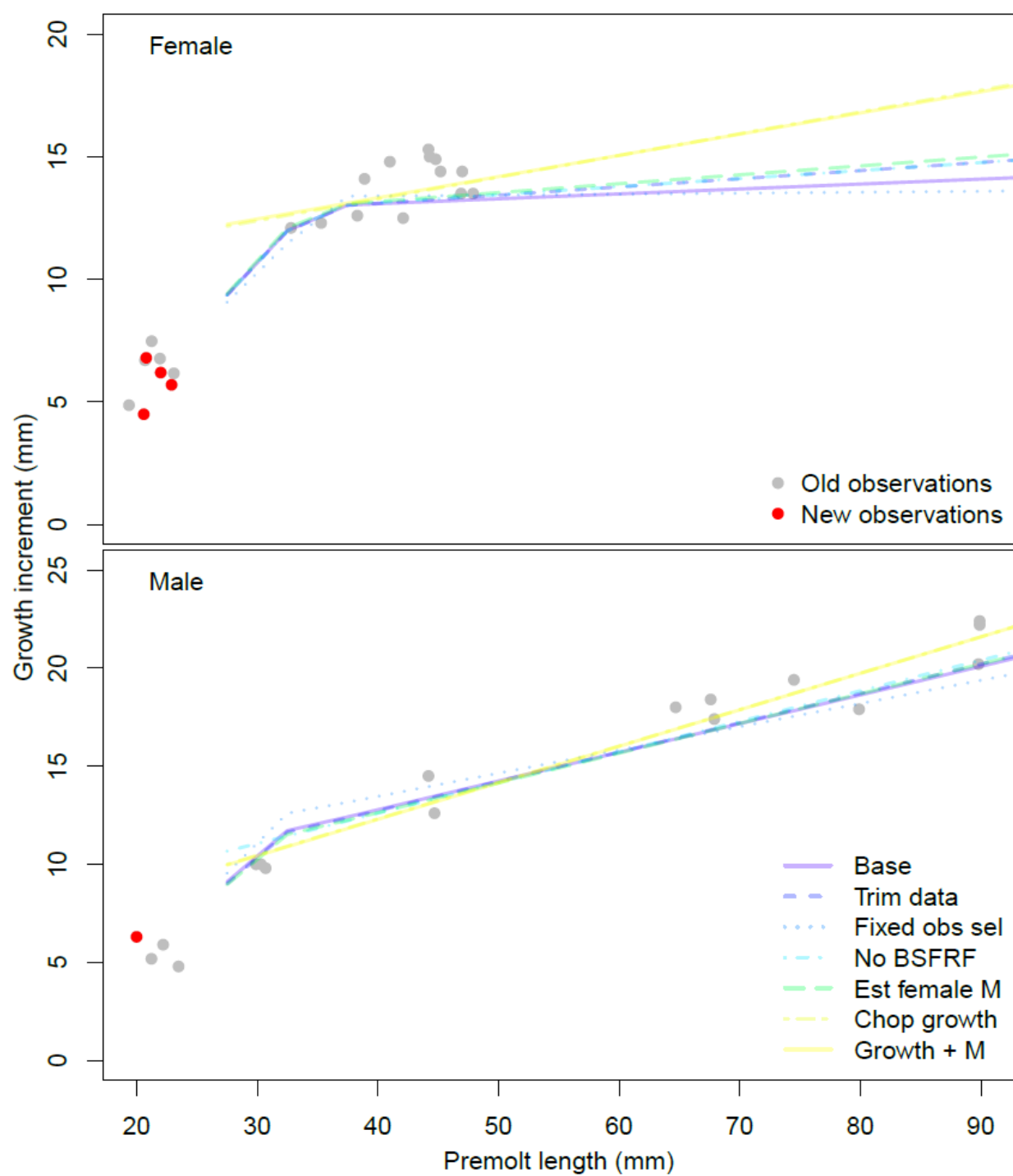
Model	MMB	B35	F35	FOFL	OFL
Base	92.09	152.3	1.91	1.14	24.59
Trim data	83.8	152.3	1.42	0.81	19.97
Fixed obs sel	221.6	215.3	3.49	2.62	82.68
No BSFRF	60.86	142.3	1.17	0.56	11.5
Est female M	74.29	139.6	1.21	0.68	18.38
Chop growth	79.57	149.8	1.34	0.75	18.66
Growth + M	70.89	137.4	1.17	0.64	17.35



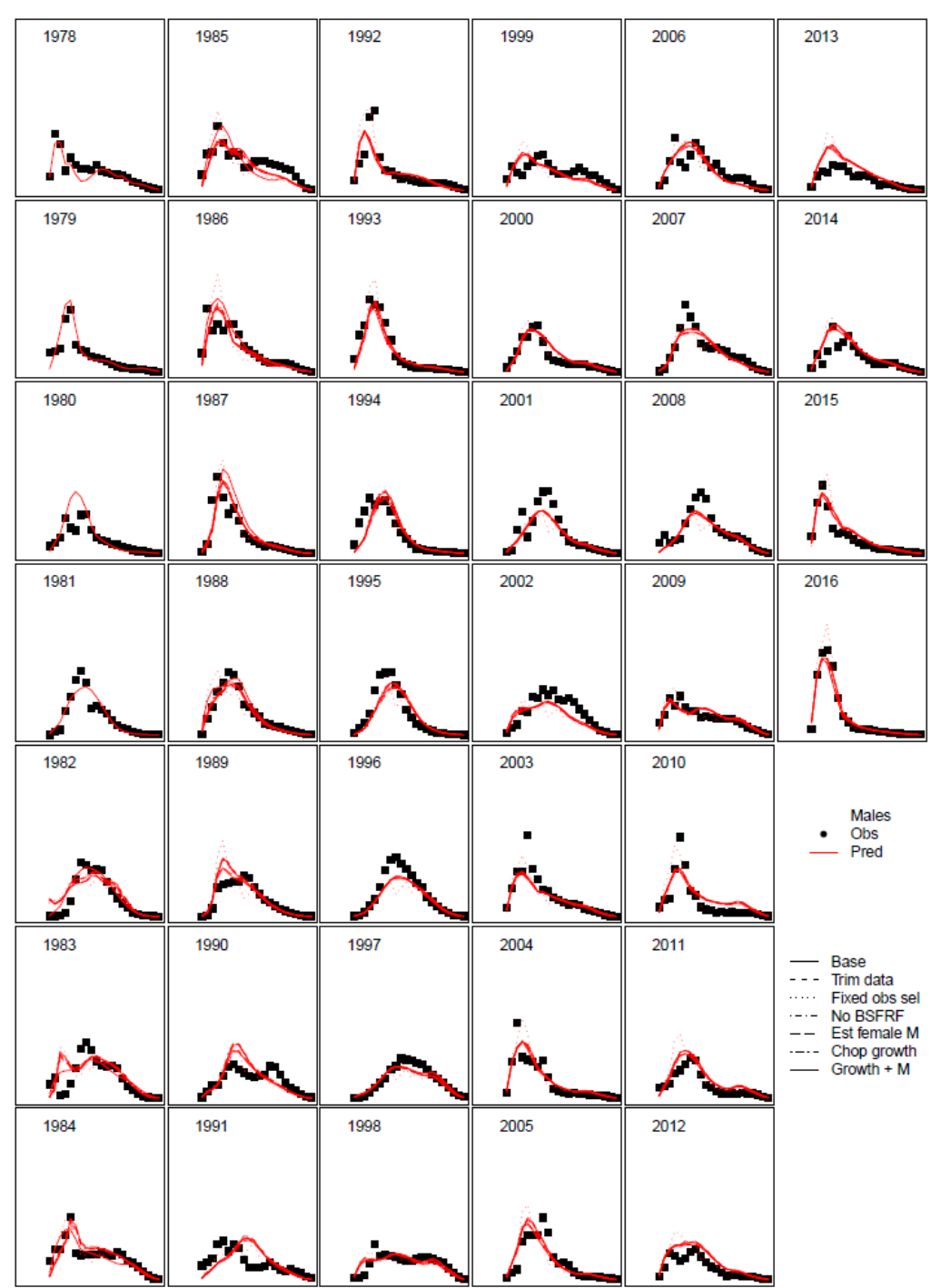
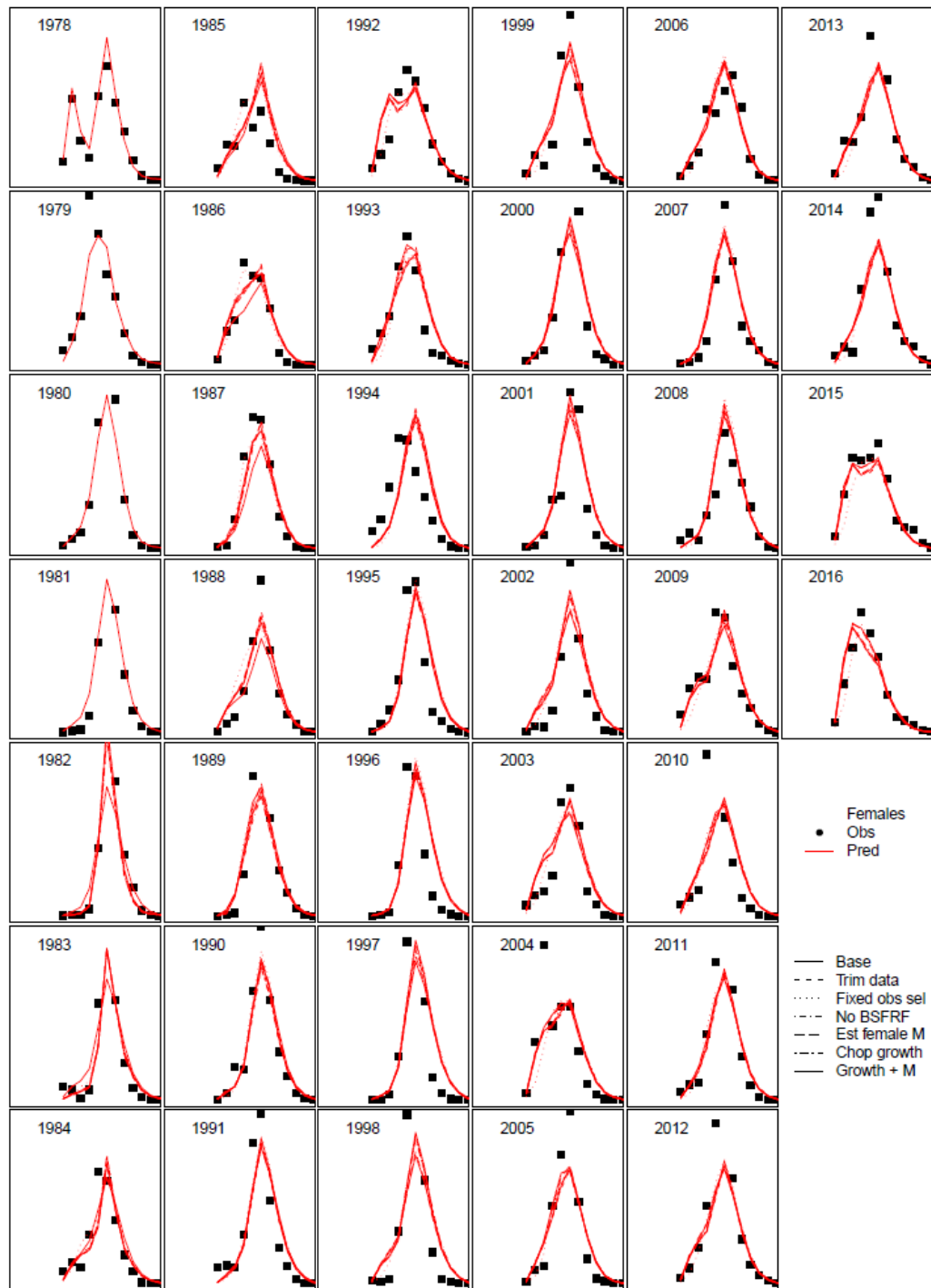


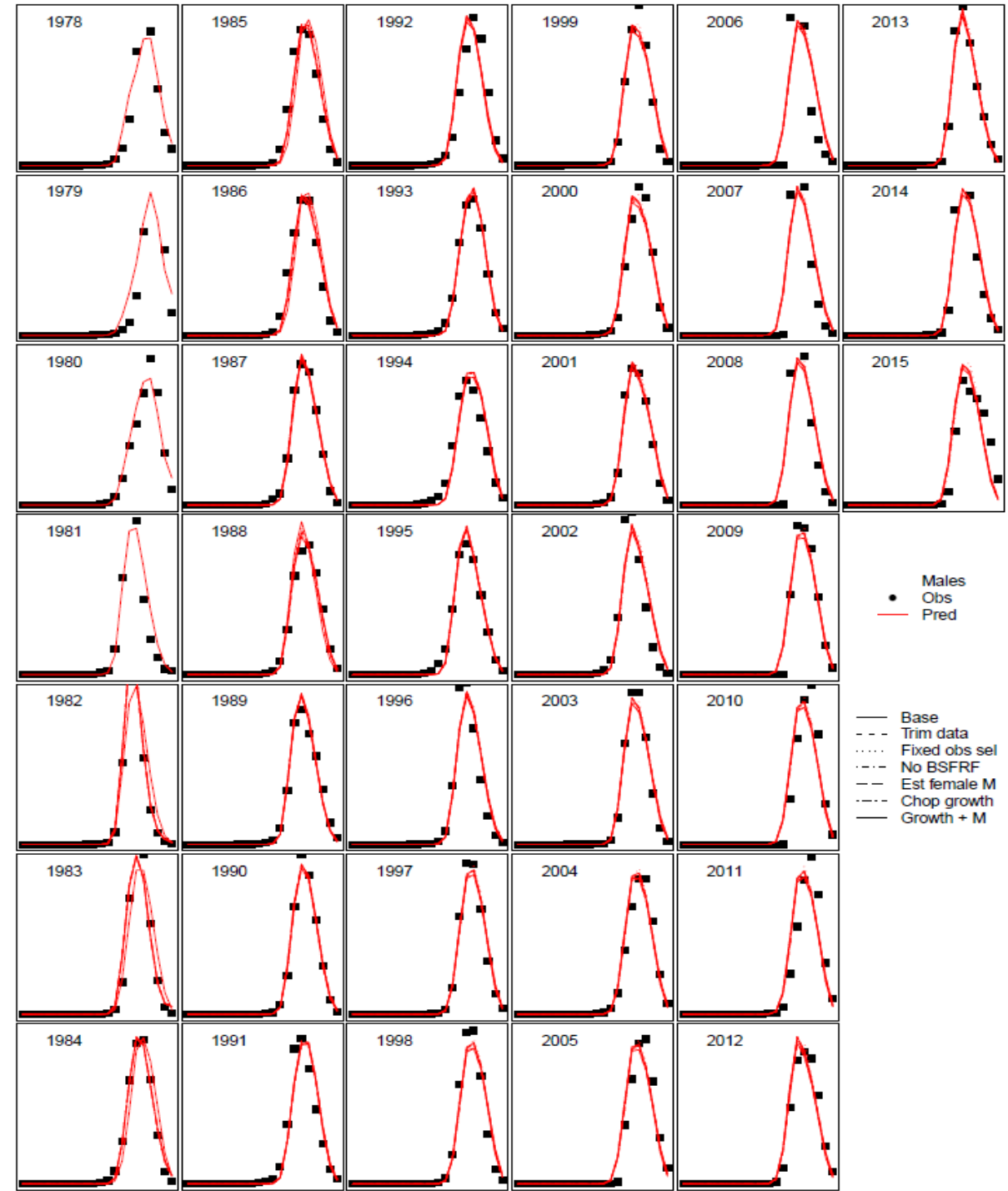
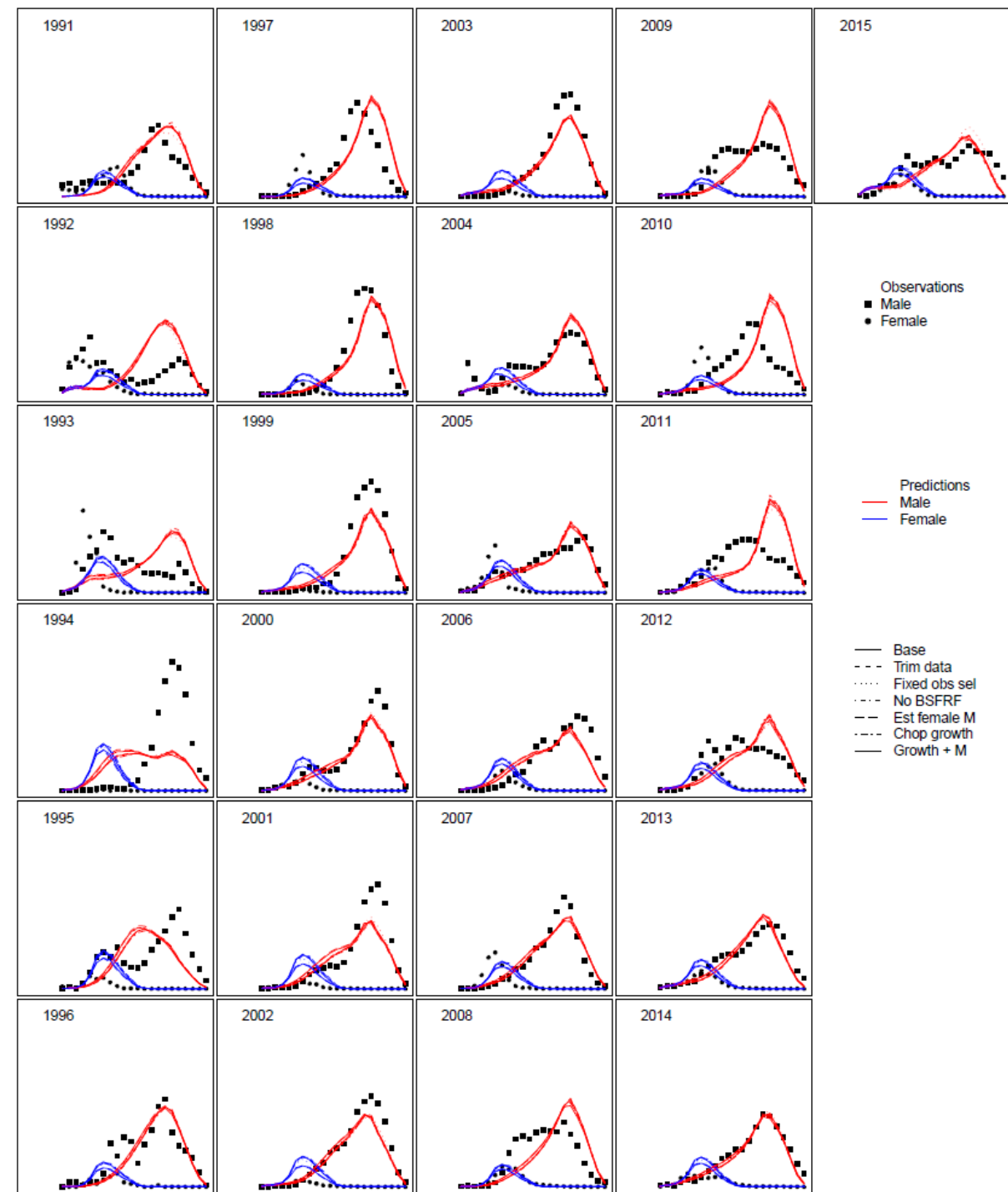
Parameter	Base	Trim data	Fixed obs sel	No BSFRF	Est female M	Chop growth	Growth + M
srv1_q	1	0.6	0.6	0.6	0.6	0.6	0.6
srv1_q_f	1	0.6	0.6	0.6	0.6	0.6	0.6
srv1_sel95	59.89	60.19	60	60.74	60.21	60.34	60.35
srv1_sel50	42.66	40.18	40	40.69	40.2	40.32	40.33
srv2_q	0.49	0.43	0.6	0.47	0.54	0.45	0.56
srv2_q_f	0.32	0.46	0.6	0.49	0.63	0.46	0.63
srv2_sel95	61.3	57.05	105	57.32	55.24	58.05	56.01
srv2_sel50	41.32	41.18	40	40.84	39.82	41.35	39.86
srv3_q	0.62	0.68	0.6	0.79	0.77	0.7	0.79
srv3_sel95	57.24	57.63	120	59.43	49.53	59.37	50.62
srv3_sel50	38.42	38.59	57.5	38.78	34.78	39.15	34.94
srv3_q_f	0.49	0.54	0.6	0.62	1	0.54	1
srv3_sel95_f	43.09	43.42	95	42.85	45.23	42.84	44.8
srv3_sel50_f	33.27	33.47	45	32.97	34.73	32.94	34.27

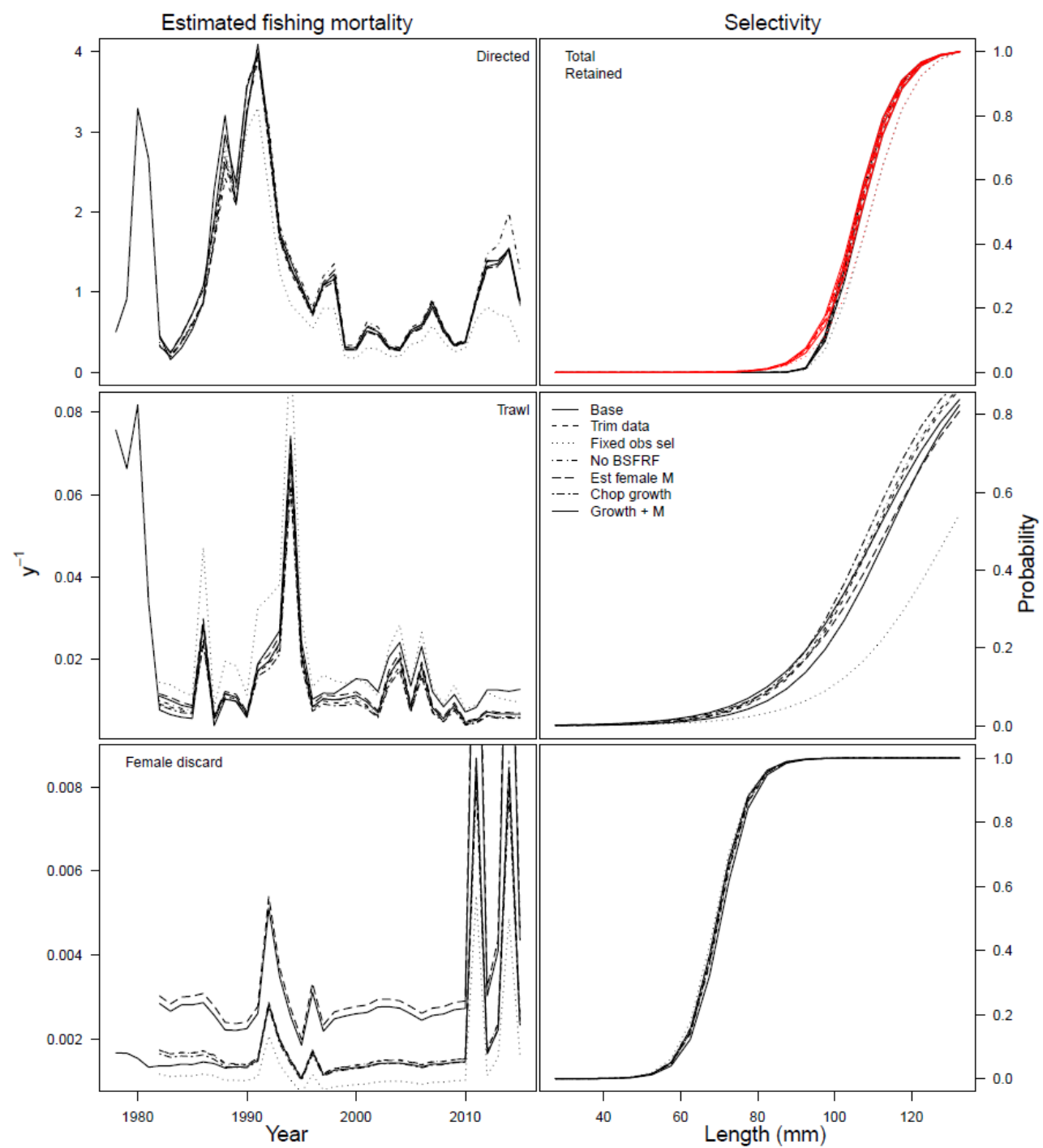
Parameter	Base	Trim data	Fixed obs sel	No BSFRF	Est female M	Chop growth	Growth + M
Mmult_imat	1.8	1.81	1.22	1.74	1.28	1.81	1.27
Mmult	1.13	1.08	1.13	1.06	1.15	1.09	1.16
Mmultf	1	1	1	1	1.41	1	1.42

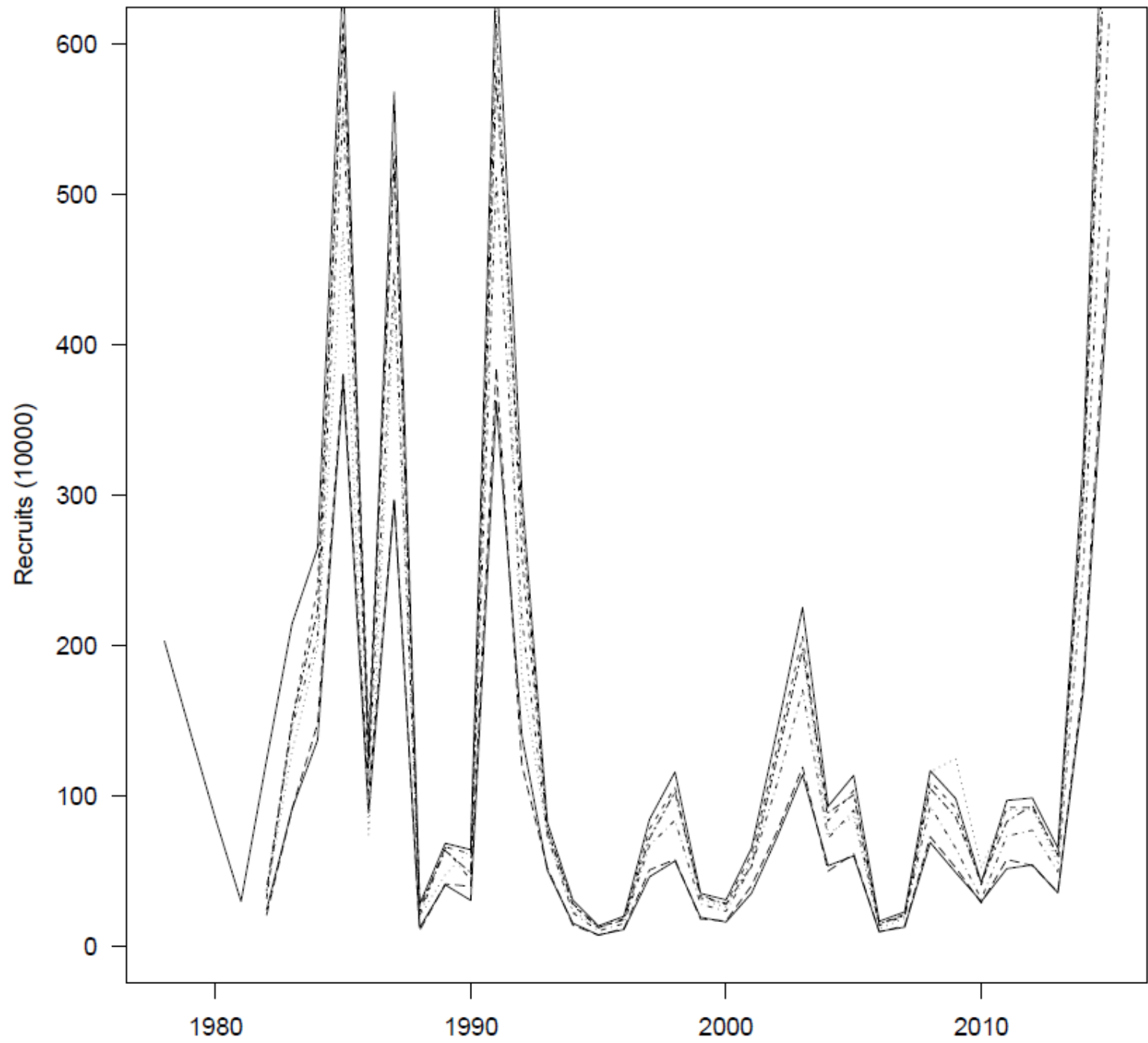


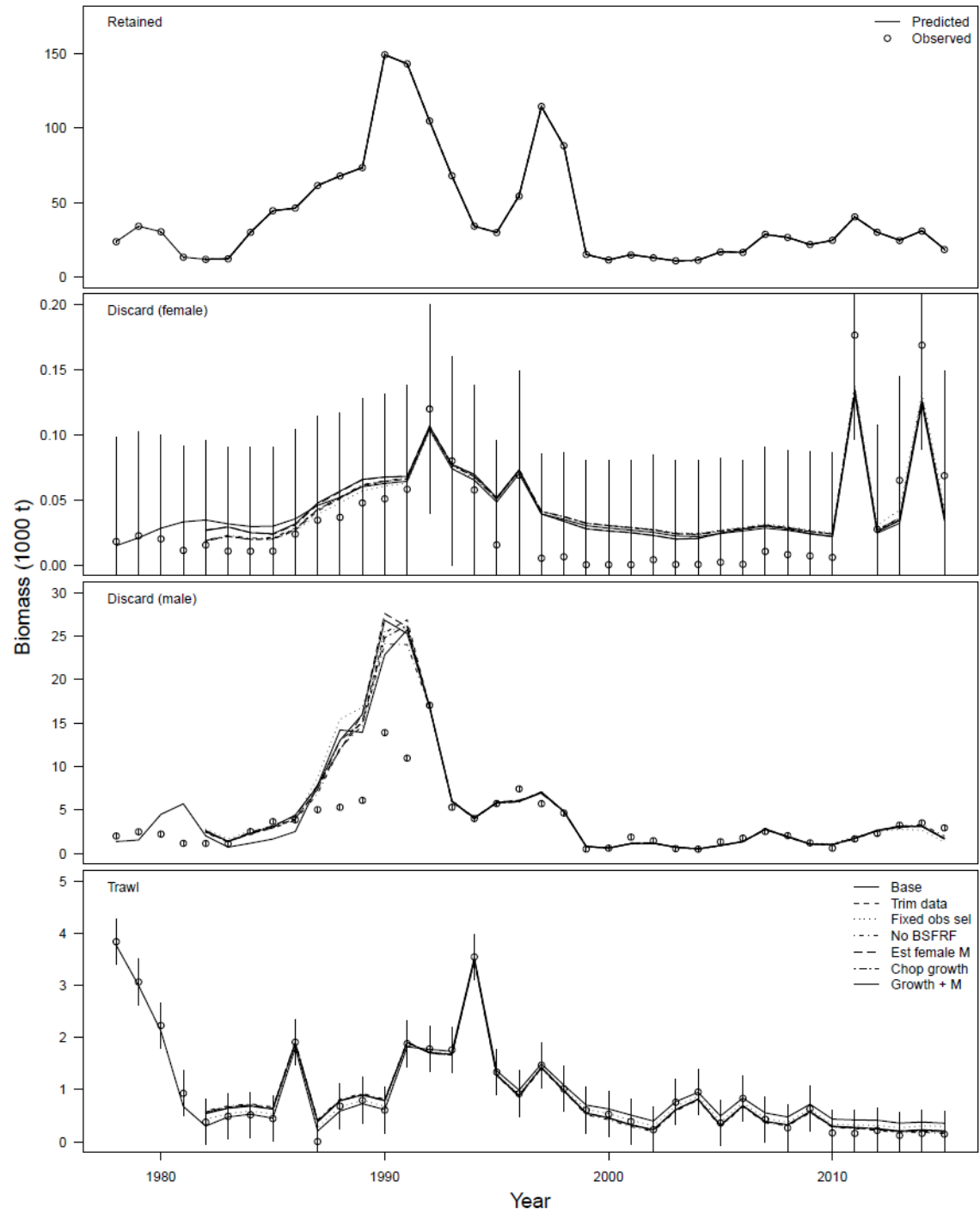
Parameter	Base	Trim data	Fixed obs sel	No BSFRF	Est female M	Chop growth	Growth + M
af	-5.08	-5.06	-4.1	-5.08	-5.29	9.72	9.87
am	-5.74	-5.83	-7.48	-12.2	-5.61	4.89	4.84
bf	1.53	1.52	1.48	1.53	1.53	1.09	1.09
bm	1.54	1.54	1.62	1.83	1.53	1.19	1.19
b1	1.15	1.15	1.12	1.16	1.15	1.25	1.25
bf1	1.02	1.03	1	1.03	1.04	1.5	1.5
deltam	32.2	32.25	32.37	27.47	32.19	30	30
deltaf	34.37	34.29	36.51	34.33	34.13	27.5	27.5











Model results

- ‘Trim data’
 - OFL decreased compared to ‘Base’, primarily because q in era 3 increased
 - Decrease in estimated probability of maturing and natural mortality for brought down F35%
- ‘Fixed obs sel’
 - OFL increased (a lot) compared to ‘Base’ from a decrease in q , probability of maturing, and growth
 - Much worse fits to survey MMB, survey selectivity much lower than any of the estimated scenarios
- ‘No BSFRF’
 - OFL decreased compared to ‘Base’, primarily because q in era 3 increased
 - Shifts breakpoint in growth
 - F35% decreases relative to ‘Base’ due to decreases in natural mortality and probability of maturing

Table 1: Changes in management quantities for each scenario considered. Reported quantities are the MLEs because running MCMC for every model was prohibitively time-consuming. The MLEs for scenarios in which MCMCs were performed are very close to the medians of the posterior distributions.

Model	MMB	B35	F35	FOFL	OFL
Base	92.09	152.3	1.91	1.14	24.59
Trim data	83.8	152.3	1.42	0.81	19.97
Fixed obs sel	221.6	215.3	3.49	2.62	82.68
No BSFRF	60.86	142.3	1.17	0.56	11.5
Est female M	74.29	139.6	1.21	0.68	18.38
Chop growth	79.57	149.8	1.34	0.75	18.66
Growth + M	70.89	137.4	1.17	0.64	17.35

Recommendations

- ‘Trim data’
 - Adopt exclusion of all data from 1978-1981, start model in 1982
 - Rationale: Including this era artificially anchors catchability at 1. Given the uncertainties around expected changes under different survey gear and the potential for catch to be missing in the early years, the risks outweigh the benefits
 - Era 3 should start in 1988 instead of 1989
- ‘Fixed obs sel’ & “No BSFRF”
 - Neither of these should be adopted, but were used illustratively
 - Think harder about how to do incorporate extra survey
 - Issues:
 - problems with variables hitting bounds
 - Large disconnect between ‘observed’ selectivity and estimated
 - Stock is at it’s lowest, in spite of an assumption of a higher q than implied by the industry surveys—changing this assumption to the ‘observed’ would have exacerbated the decline in MMB

Natural mortality

- Current:
 - Immature M (male and female):
 - 0.41 (estimated)
 - Prior = $N(0.23, 0.154)$
 - Mature female M:
 - 0.23 (fixed)
 - Mature male M:
 - 0.26 (estimated)
 - Prior = $N(0.23, 0.054)$
- Issues
 - Mature male M was higher than female, which was biologically questionable
 - No natural mortality specific data (e.g. tagging data)
 - Has a large impact on reference points
 - Poorly documented rationale

Model runs

- 'Est female M'
 - 'Trim data' + estimating mature female M + setting the prior for immature crab equal to prior for mature crab
 - Potentially corrects for flip-flop of M between sexes and corrects the prior to conform to the rationale of M being based on longevity

Model results

- 'Trim data'
 - Immature M (male and female):
 - 0.29 (estimated, decreased from 0.41)
 - Prior = $N(0.23, 0.054)$ [sd decreased from 0.154]
 - Mature female M:
 - 0.32 (estimated, increased from 0.23)
 - Prior = $N(0.23, 0.054)$
 - Mature male M:
 - 0.26 (estimated; did not change)
 - Prior = $N(0.23, 0.054)$
 - Survey catchability is pegged at 1 for females when estimating mature M
 - OFL decreased compared to 'Base', primarily because q in era 3 increased
 - Decrease in estimated probability of maturing for brought down F35%

Parameter	Base	Trim data	Fixed obs sel	No BSFRF	Est female M	Chop growth	Growth + M
srv1_q	1	0.6	0.6	0.6	0.6	0.6	0.6
srv1_q_f	1	0.6	0.6	0.6	0.6	0.6	0.6
srv1_sel95	59.89	60.19	60	60.74	60.21	60.34	60.35
srv1_sel50	42.66	40.18	40	40.69	40.2	40.32	40.33
srv2_q	0.49	0.43	0.6	0.47	0.54	0.45	0.56
srv2_q_f	0.32	0.46	0.6	0.49	0.63	0.46	0.63
srv2_sel95	61.3	57.05	105	57.32	55.24	58.05	56.01
srv2_sel50	41.32	41.18	40	40.84	39.82	41.35	39.86
srv3_q	0.62	0.68	0.6	0.79	0.77	0.7	0.79
srv3_sel95	57.24	57.63	120	59.43	49.53	59.37	50.62
srv3_sel50	38.42	38.59	57.5	38.78	34.78	39.15	34.94
srv3_q_f	0.49	0.54	0.6	0.62	1	0.54	1
srv3_sel95_f	43.09	43.42	95	42.85	45.23	42.84	44.8
srv3_sel50_f	33.27	33.47	45	32.97	34.73	32.94	34.27

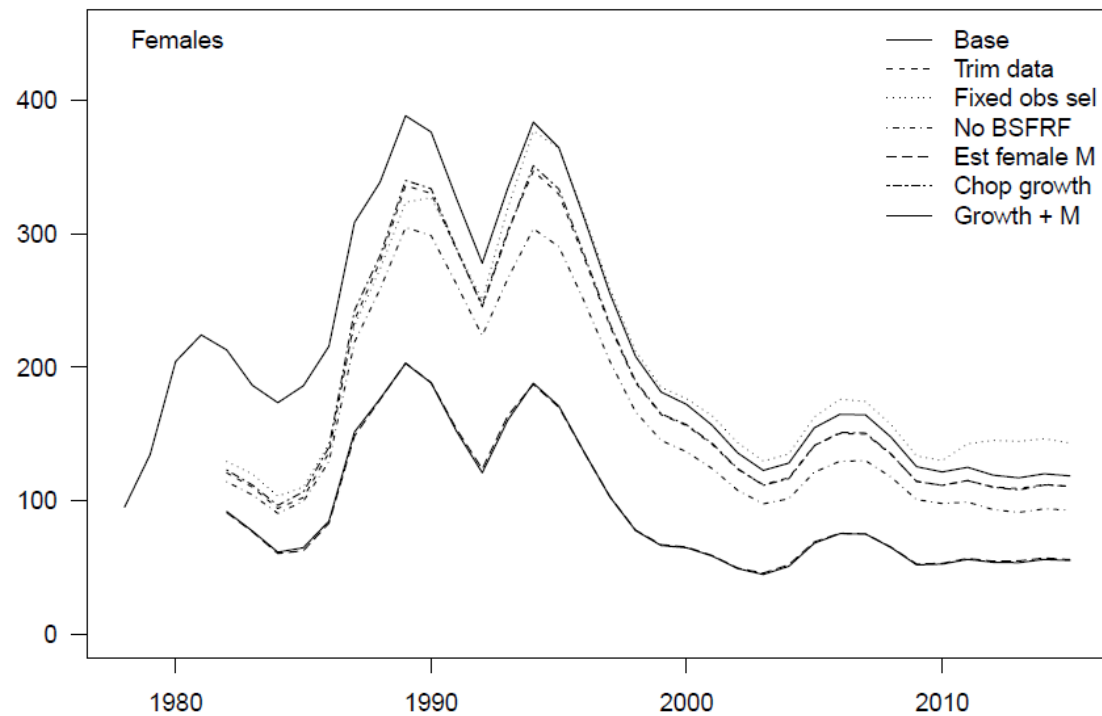
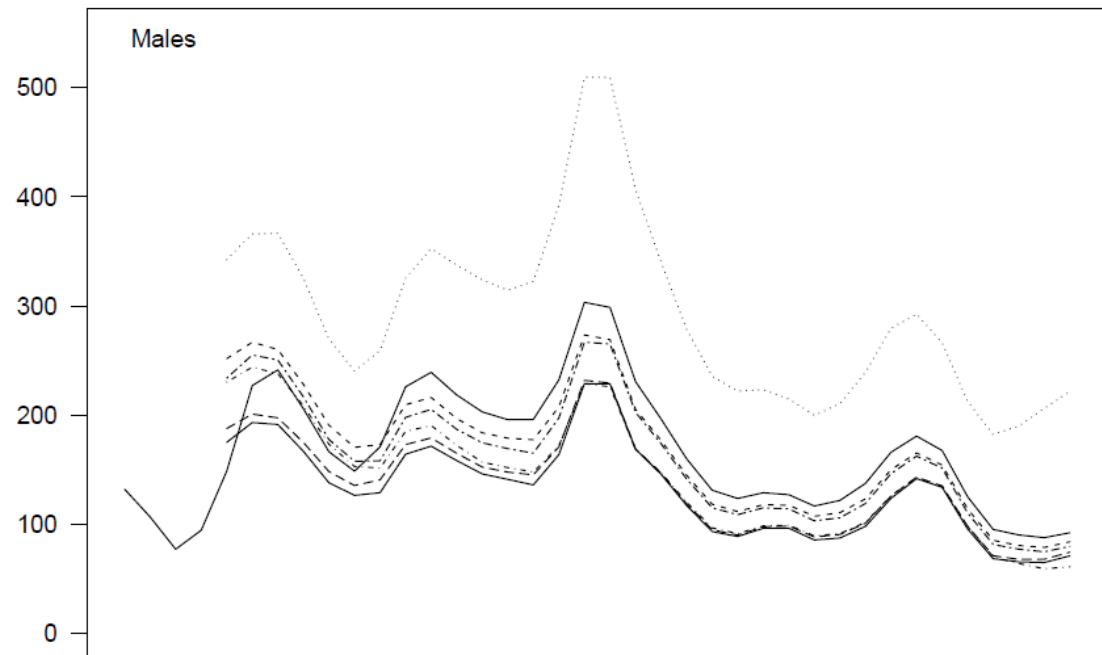


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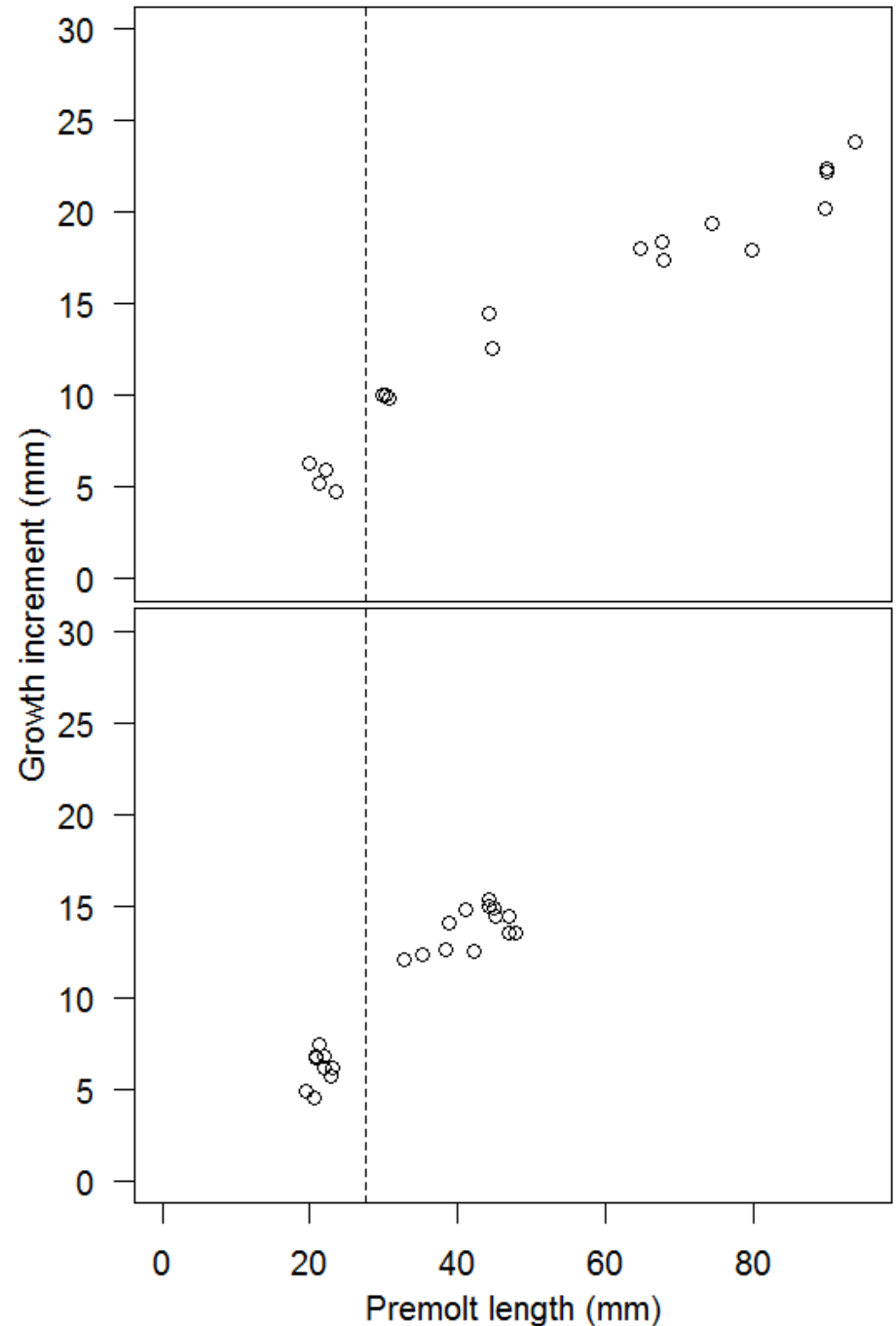
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Recommendations

- It makes sense to estimate mature female natural mortality and corrects the relationship between mature male and mature female M , but now survey q in era 3 for females hits its bound of 1.
- Immature natural mortality is now flipped, but this is a result of placing the same prior on immature M that is placed on mature M .

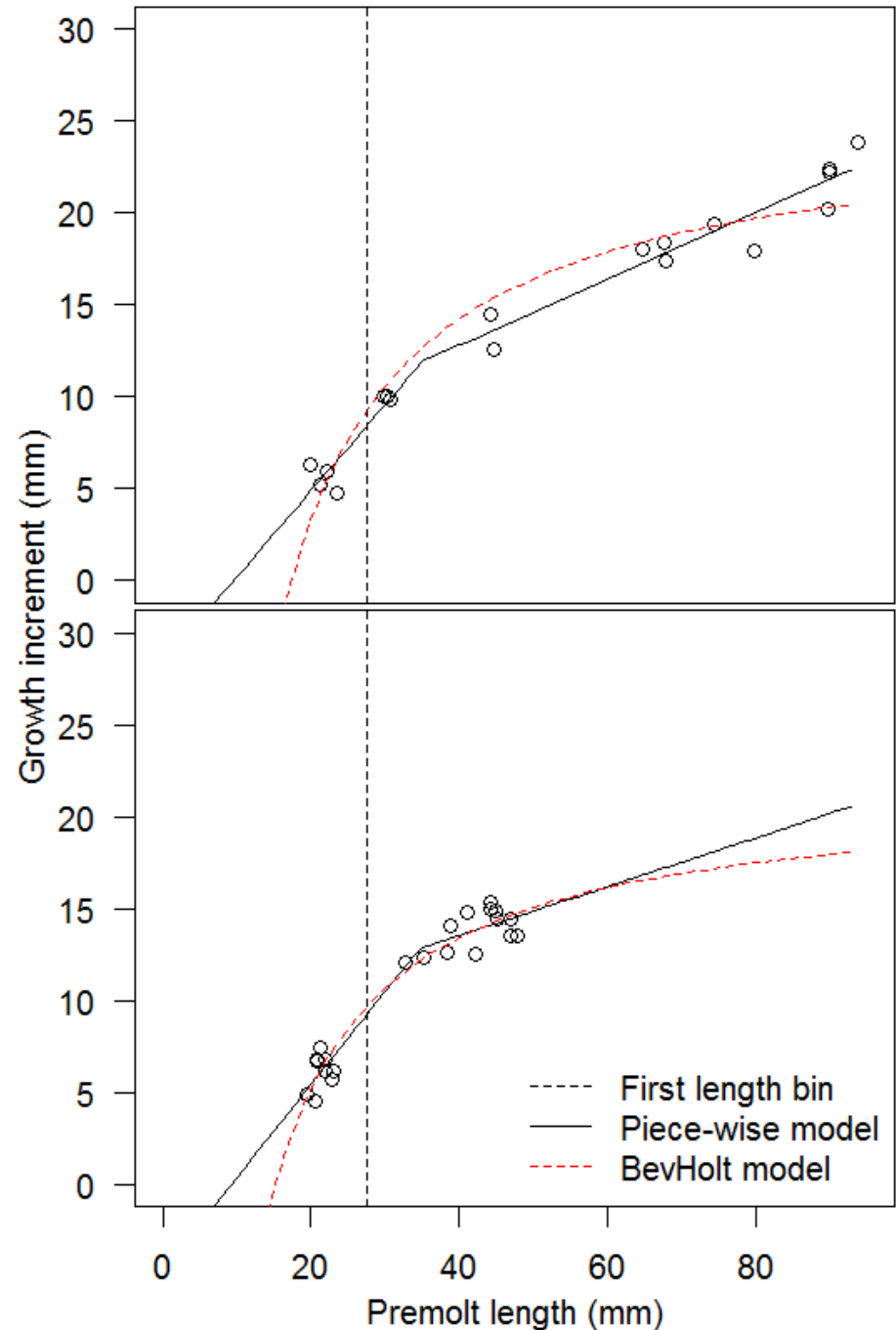
Growth model and available data

- Current: Piece-wise linear model
- 8 estimated parameters
- 40 data points
- Issues
 - No data where the breakpoint, resulting in poor estimation
 - Data beneath the breakpoint impacts the model little
 - Growth parameters hit bounds and are generally poorly behaved
- What model should be used for growth?



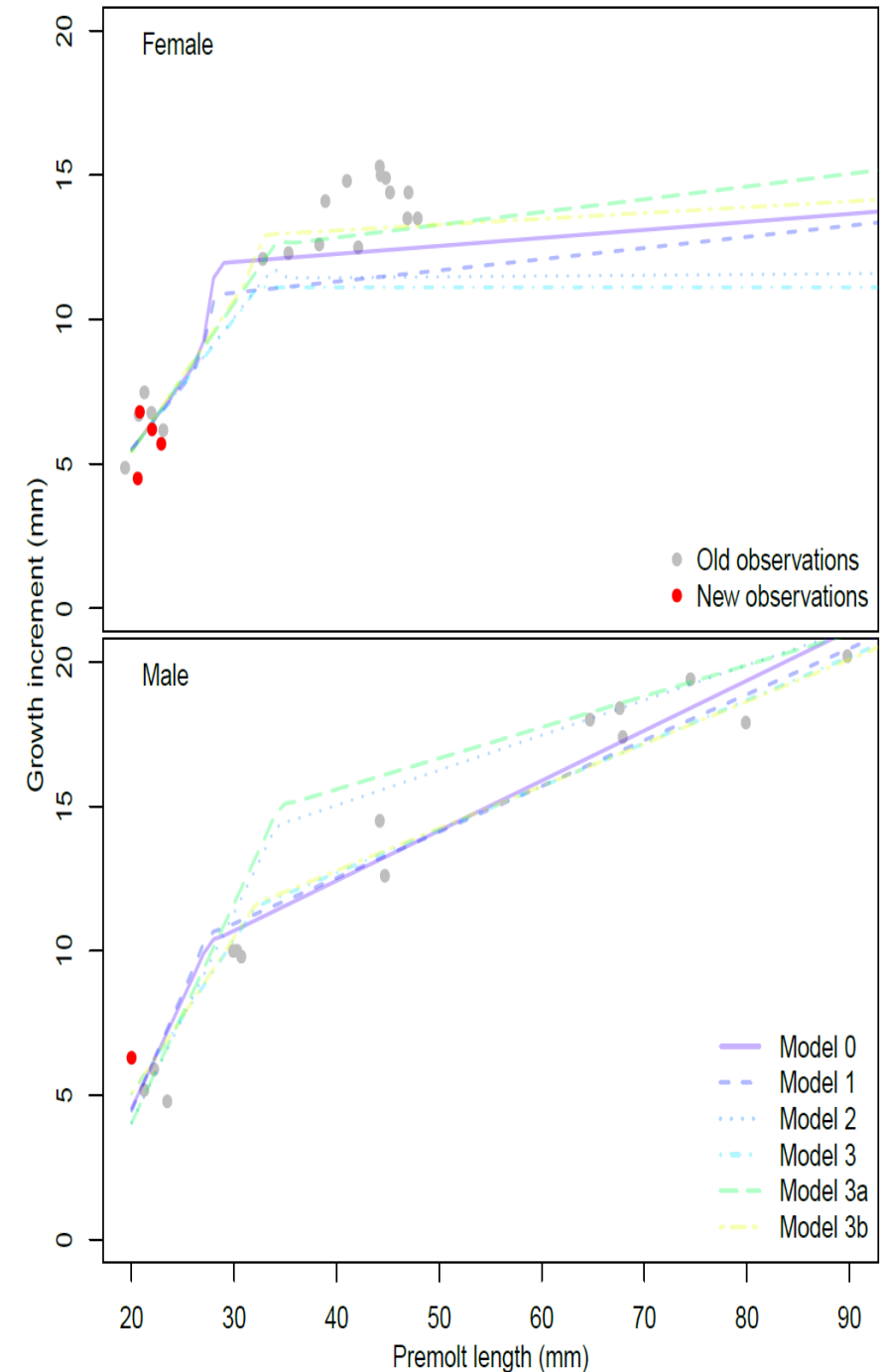
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 - Growth parameters hit bounds and are generally poorly behaved
- What model should be used for growth?



Model runs

- ‘Chop growth’
 - “Trim data” + excludes all growth data with a premolt size of <27.5 mm, then estimates only a linear model for both males and females
 - Explores problem of bound hitting and poorly estimated growth parameters
- ‘Growth + M’
 - ‘Chop growth’ + estimating mature female M
 - Growth and natural mortality are somewhat confounded

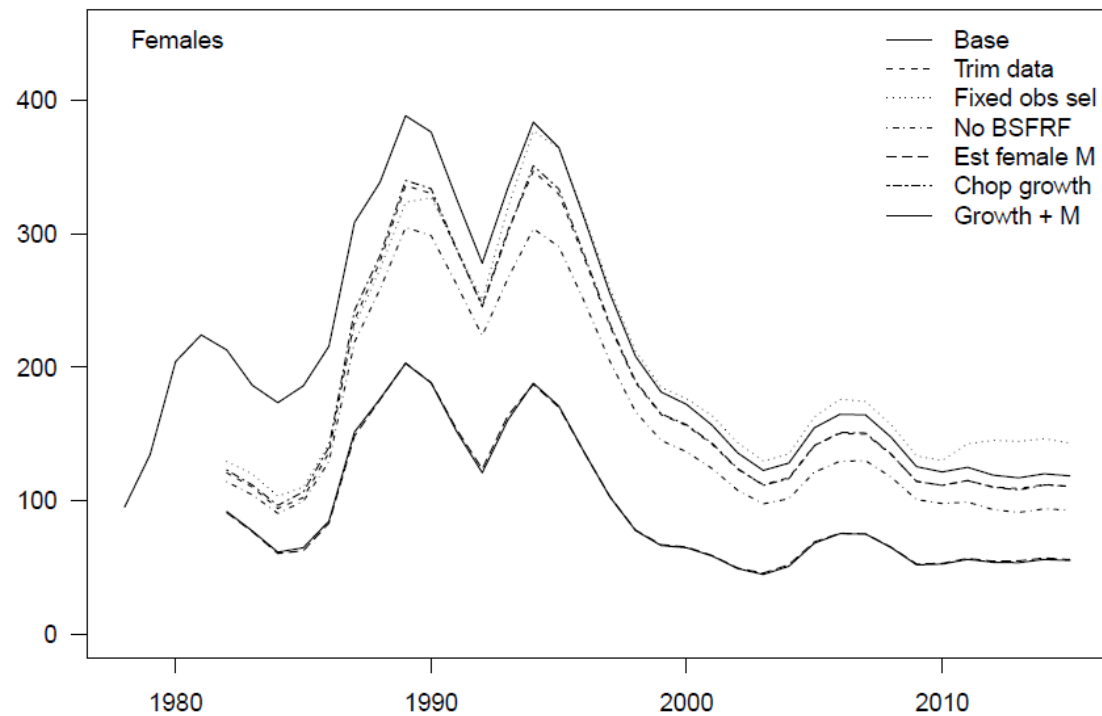
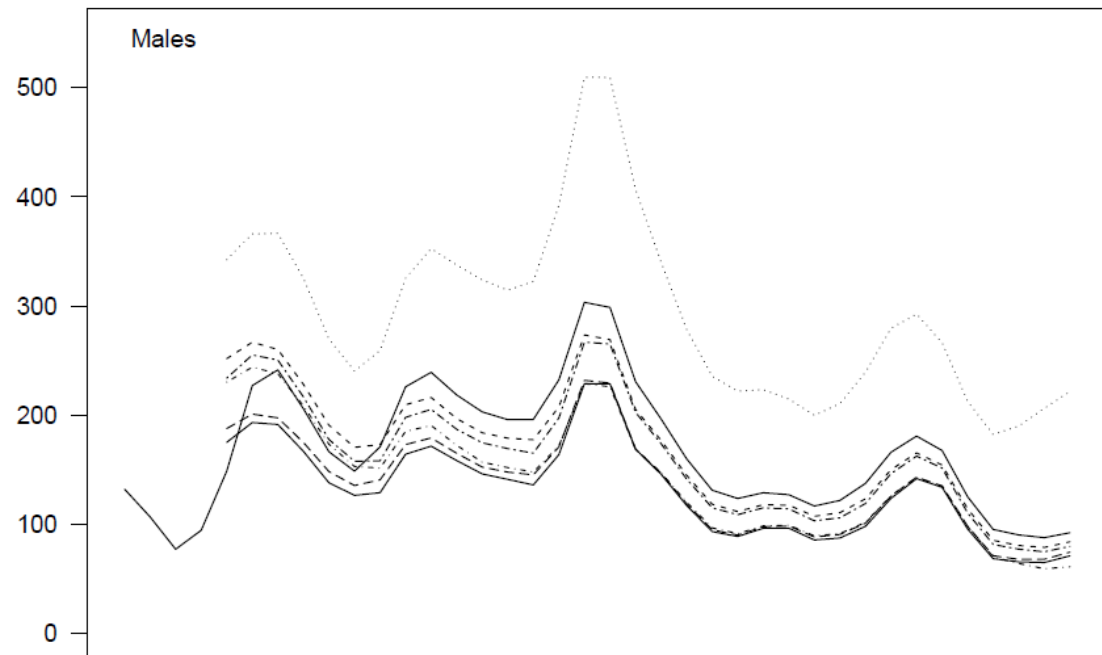
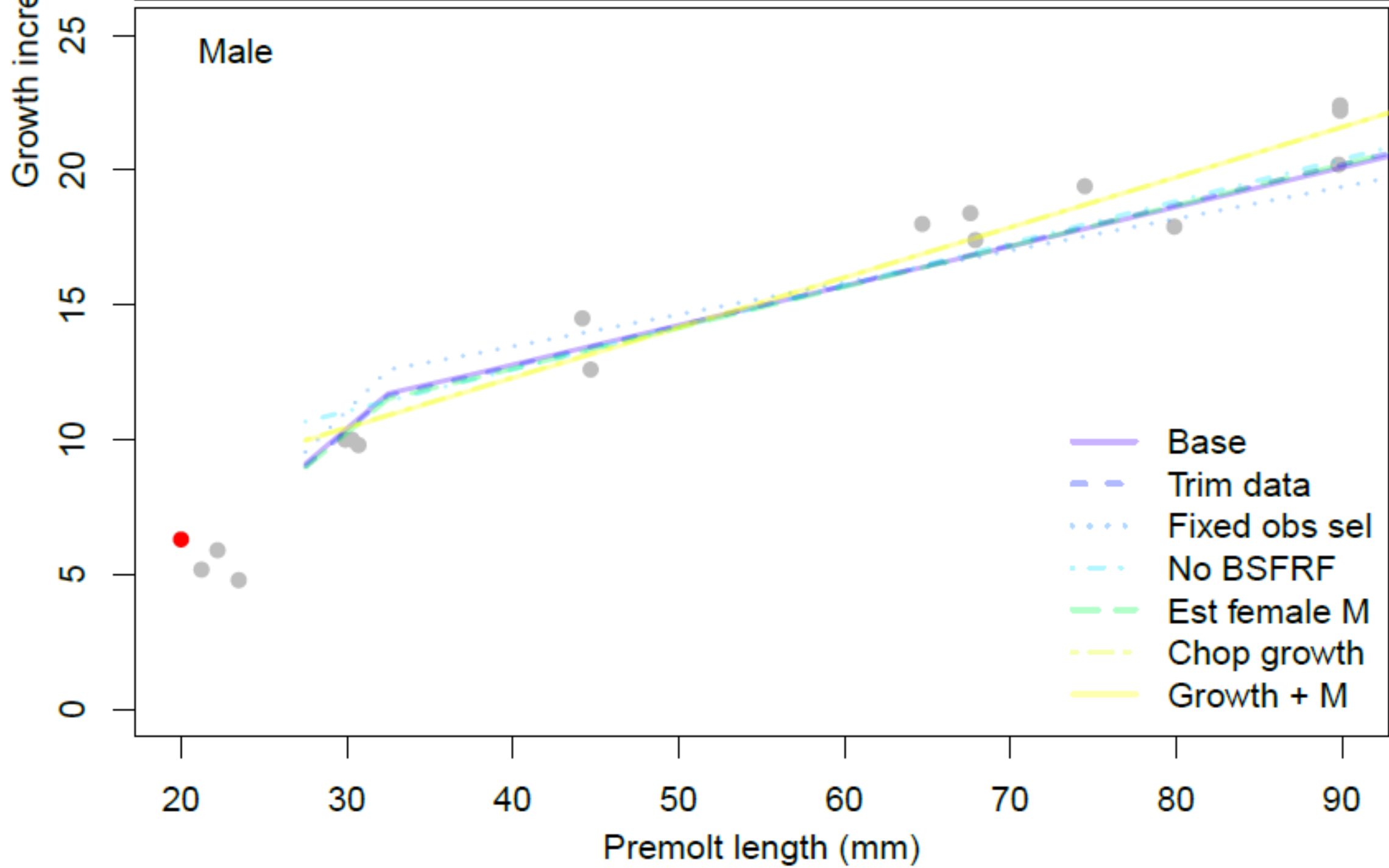
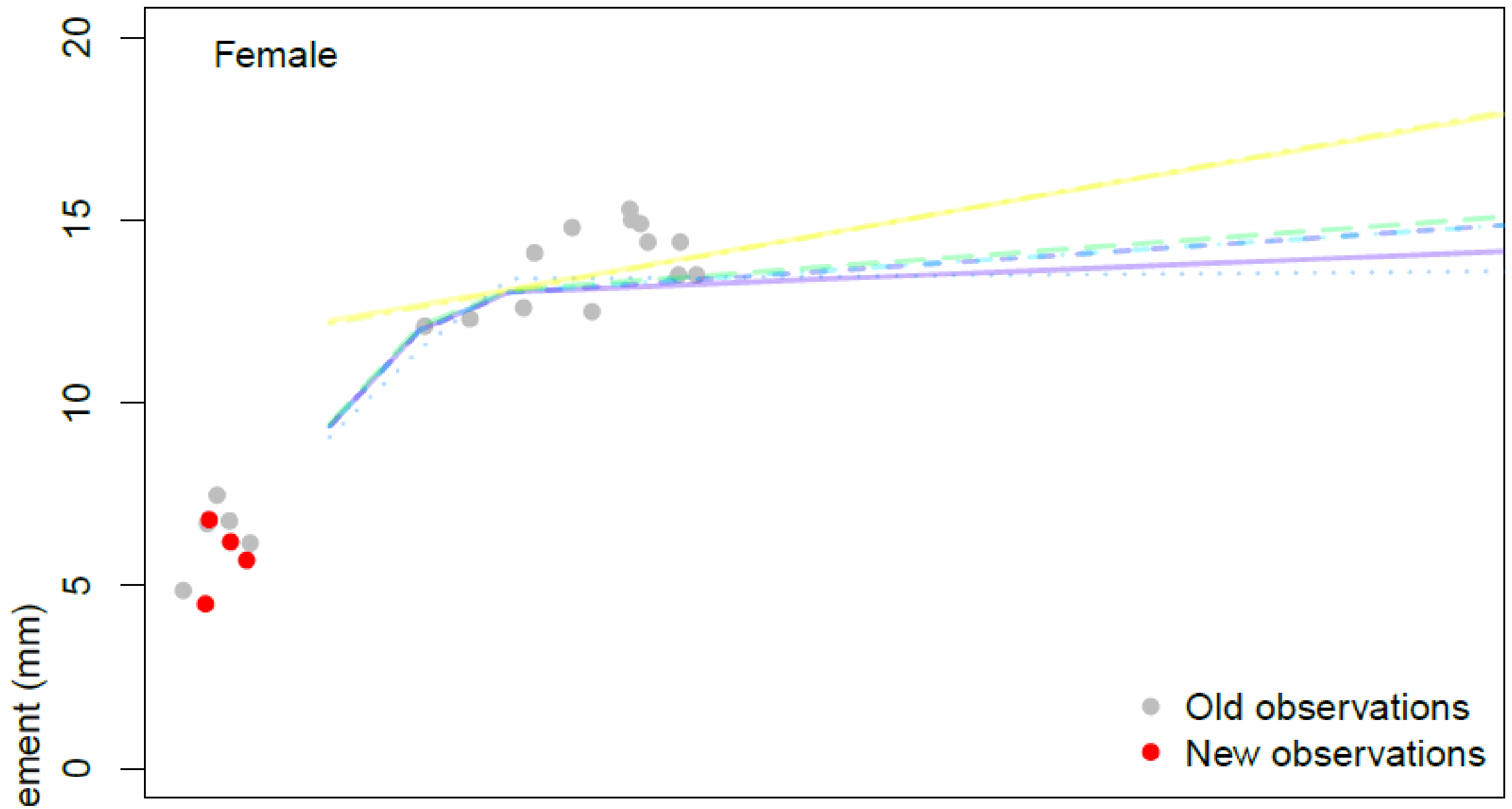


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Parameter	Base	Trim data	Fixed obs sel	No BSFRF	Est female M	Chop growth	Growth + M
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srv1_q_f	1	0.6	0.6	0.6	0.6	0.6	0.6
srv1_sel95	59.89	60.19	60	60.74	60.21	60.34	60.35
srv1_sel50	42.66	40.18	40	40.69	40.2	40.32	40.33
srv2_q	0.49	0.43	0.6	0.47	0.54	0.45	0.56
srv2_q_f	0.32	0.46	0.6	0.49	0.63	0.46	0.63
srv2_sel95	61.3	57.05	105	57.32	55.24	58.05	56.01
srv2_sel50	41.32	41.18	40	40.84	39.82	41.35	39.86
srv3_q	0.62	0.68	0.6	0.79	0.77	0.7	0.79
srv3_sel95	57.24	57.63	120	59.43	49.53	59.37	50.62
srv3_sel50	38.42	38.59	57.5	38.78	34.78	39.15	34.94
srv3_q_f	0.49	0.54	0.6	0.62	1	0.54	1
srv3_sel95_f	43.09	43.42	95	42.85	45.23	42.84	44.8
srv3_sel50_f	33.27	33.47	45	32.97	34.73	32.94	34.27





Model results

- ‘Growth + M’
 - ‘Growth + M’ is the ‘synthesis’ of all the changes—excludes 1978-1981 data, estimates mature female M, eliminates problem parameters from growth
 - BUT, new problems arise:
 - Survey q (females era 3) is now estimated at 1
 - Survey q (males era 3) is now estimated at 0.79, which is a large increase over the ‘Base’

Recommendations summary

- Select a method for computing a distribution of the OFL based on uncertainty in the data and parameter estimates
- Drop 1978-1981 data
- Start era 3 in 1988
- Use a model selection approach to identify a model other than the piece-wise linear models for growth?
- Estimate mature female M , but whack-a-mole era 3 survey q ?