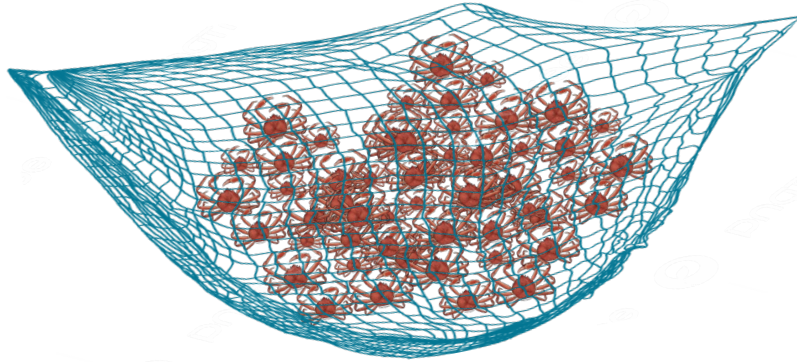




Updated *Chionoecetes* maturity workflow

Emily Ryznar
NMFS-AFSC Kodiak

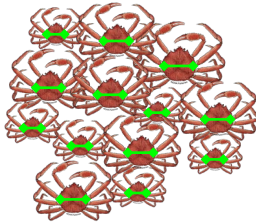
Two-stage sampling designs are advantageous for population metrics that cannot be measured directly



SPECIMEN DATA
(subsample 1)

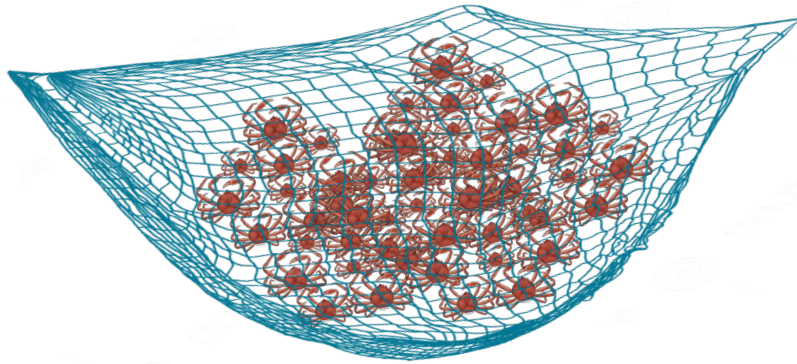
1

Measure
carapace widths
for crab haul
subsample



Subsample 1 ("specimen data"): crab
subsampled for size measurements (or lengths
in fish)

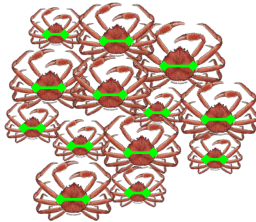
Two-stage sampling designs are advantageous for population metrics that cannot be measured directly



SPECIMEN DATA
(subsample 1)

1

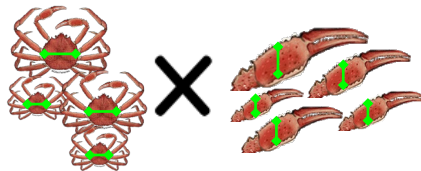
Measure
carapace widths
for crab haul
subsample



CHELA DATA
(subsample 2)

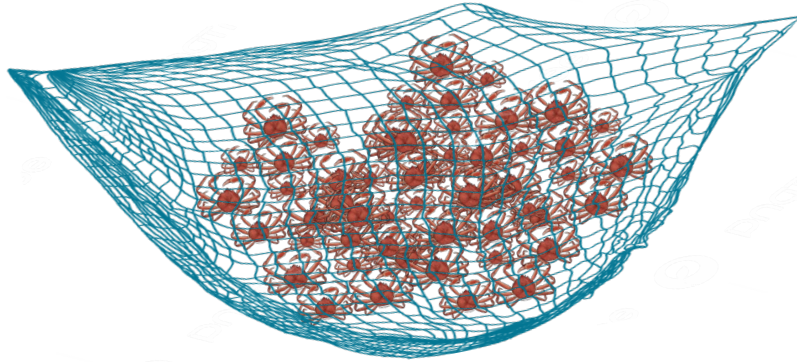
2

Measure chela
heights from
specimen data
subsample



Subsample 2 (“chela data”): crab subsampled from the first subsample for chela maturity measurements (or otoliths in fish for age), with sampling targets

Two-stage sampling designs are advantageous for population metrics that cannot be measured directly

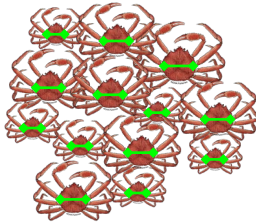


Many approaches do not account for uneven sampling or spatiotemporal variability in this step

SPECIMEN DATA
(subsample 1)

1

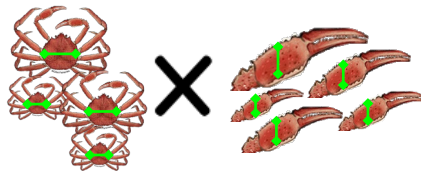
Measure
carapace widths
for crab haul
subsample



CHELA DATA
(subsample 2)

2

Measure chela
heights from
specimen data
subsample



Metric of interest (maturity-at-size, age-at-length) is calculated using subsample 2 data then applied to subsample 1 via age-length-keys, models, etc.

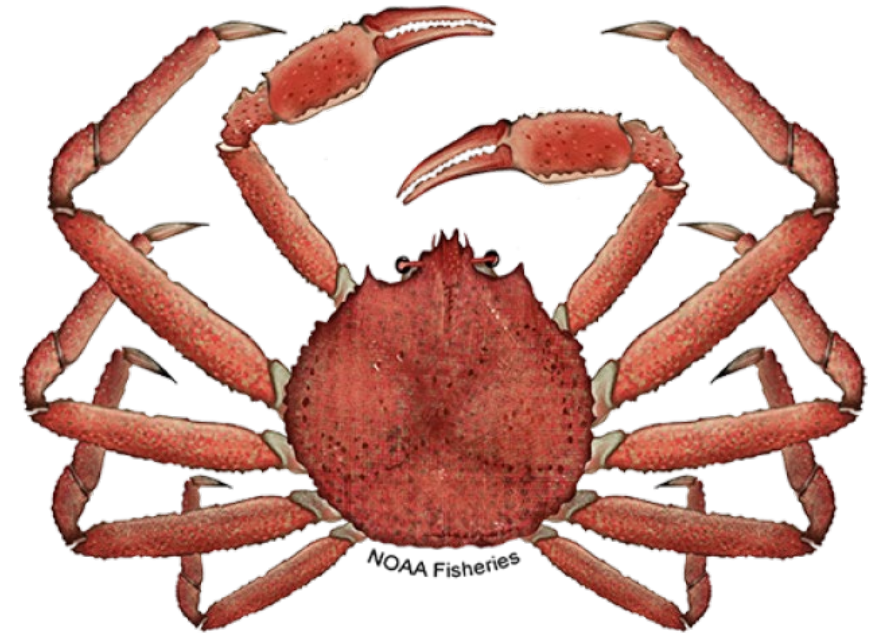
Why is this important for Bering Sea *Chionoecetes*?

- *Chionoecetes* undergo a terminal molt to maturity
- Size-at-maturity (SAM) is an important metric for biological fitness and management
- There is evidence that SAM is declining for both snow crab and Tanner crab in the Bering Sea
- *Chionoecetes* maturity dynamics can exhibit spatiotemporal variation
- Reliable and unbiased maturity estimates are needed that account for spatiotemporal and sampling uncertainty



Goals

1. Evaluate the AFSC Shellfish Assessment Program's legacy workflow for processing *Chionoecetes* maturity data from the EBS bottom trawl survey
2. If necessary, update the workflow to reflect potential spatiotemporal variation in maturity and sampling uncertainty

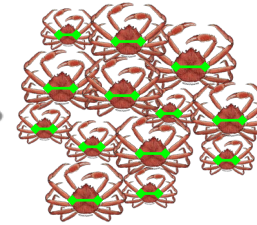
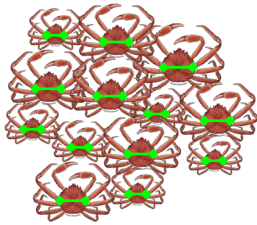


Maturity data workflow

SPECIMEN DATA
(subsample 1)

1

Measure
carapace widths
for crab haul
subsample



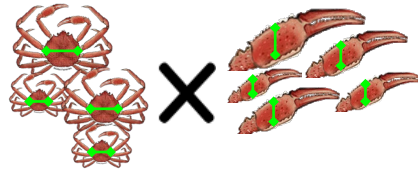
7

Calculate and plot yearly
ogives, size at 50%
maturity, and mature
biomass/abundance

CHELA DATA
(subsample 2)

2

Measure chela
heights from
specimen data
subsample

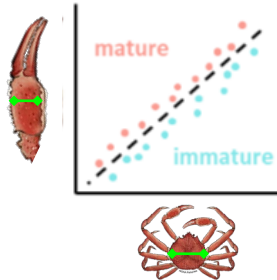


3

Generate $\ln(\text{CH}) \sim$
 $\ln(\text{CW})$ maturity
cutline

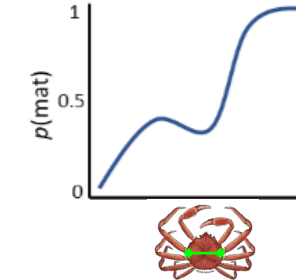
4

Apply cutline to
chela data to assign
crab as mature or
immature



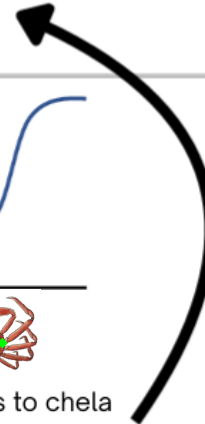
5

Fit models to chela
maturity data to
estimate probability
mature at size

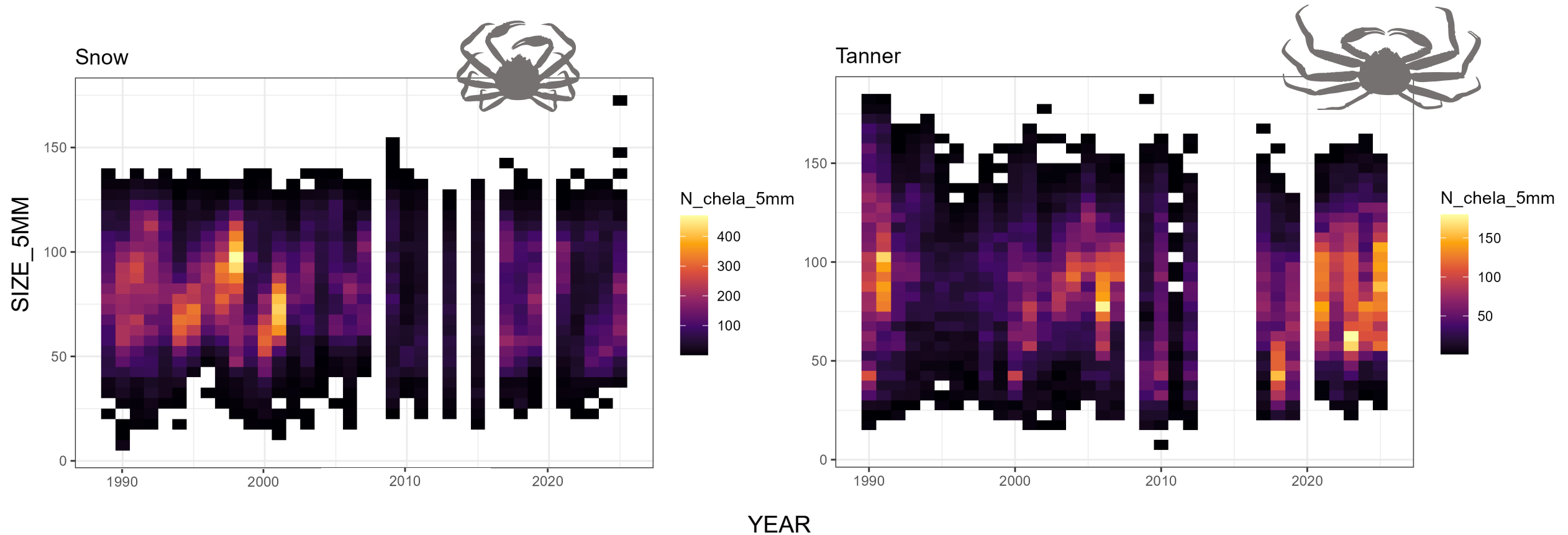


6

Apply maturity models
to specimen data to
estimate maturity at size
for each specimen crab



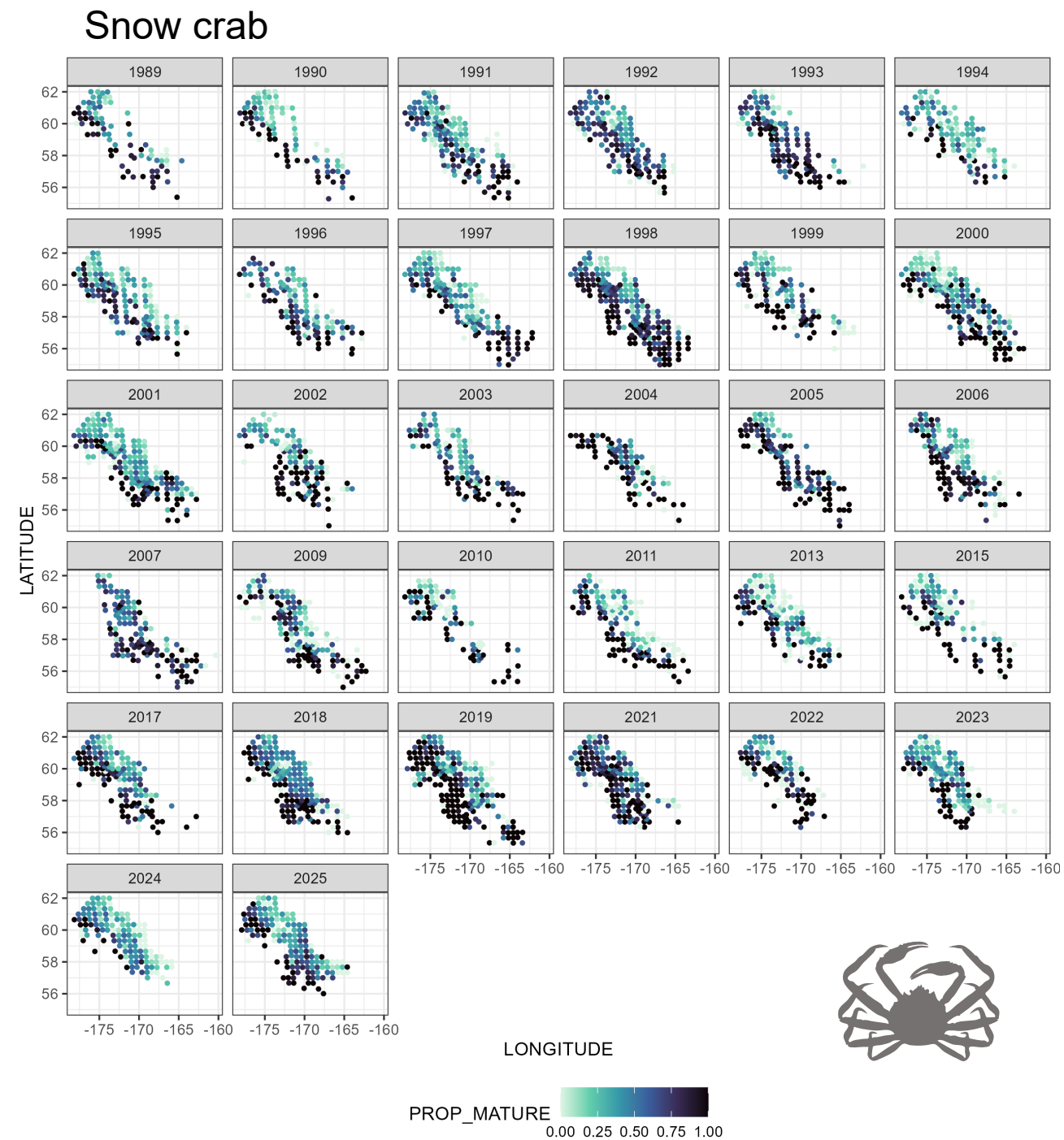
Chela data nuances



→ Sparse/uneven sampling across years and size bins

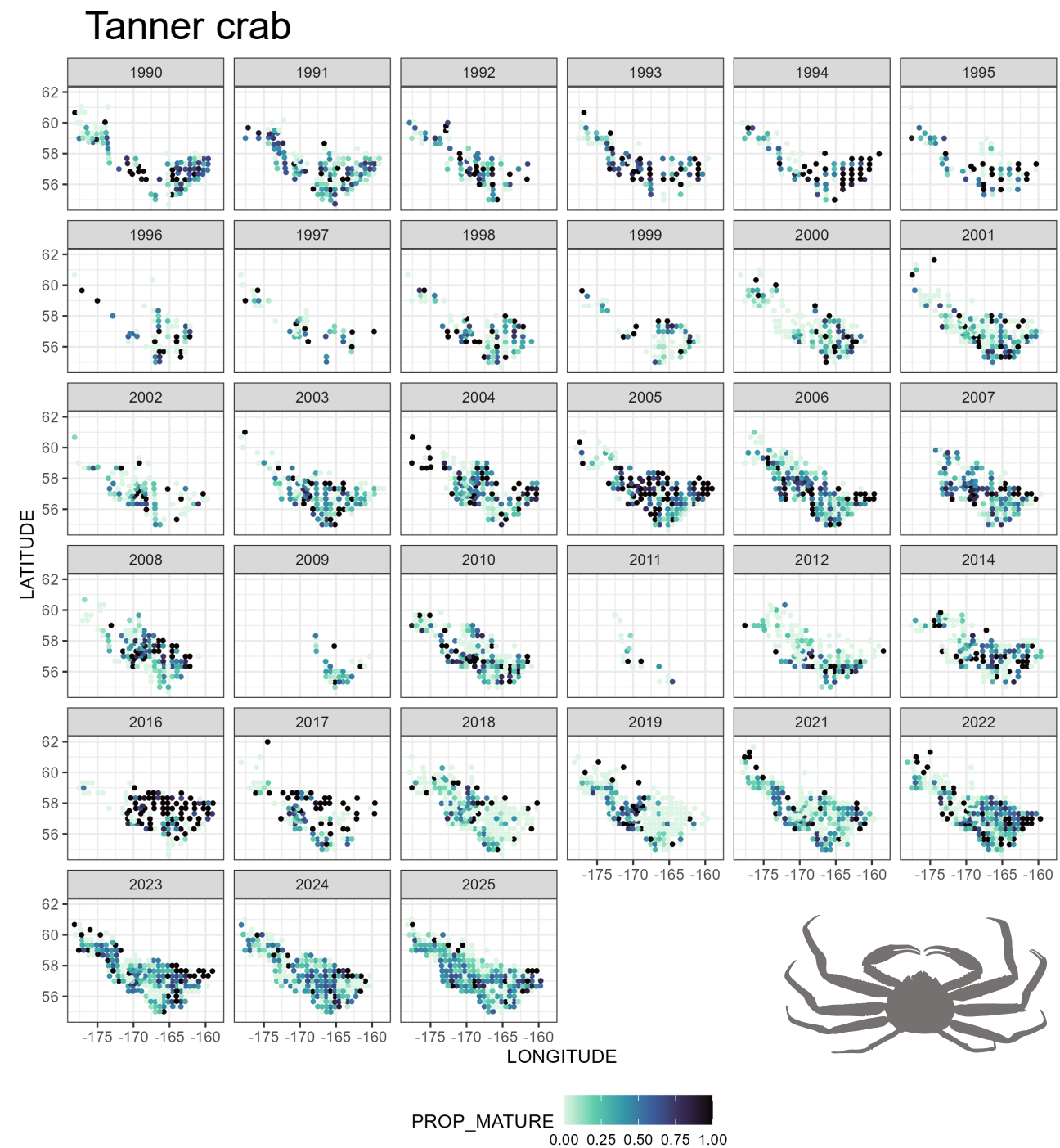
Chela data nuances

- Uneven sampling across space
- Evidence of spatiotemporal variability in maturity



Chela data nuances

- Uneven sampling across space
- Evidence of spatiotemporal variability in maturity



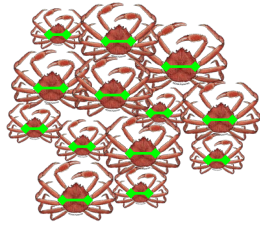
3

Establishing maturity cutlines

SPECIMEN DATA
(subsample 1)

1

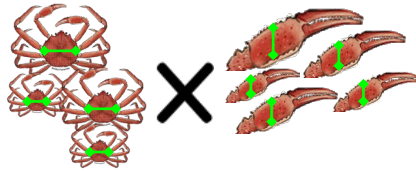
Measure
carapace widths
for crab haul
subsample



CHELA DATA
(subsample 2)

2

Measure chela
heights from
specimen data
subsample

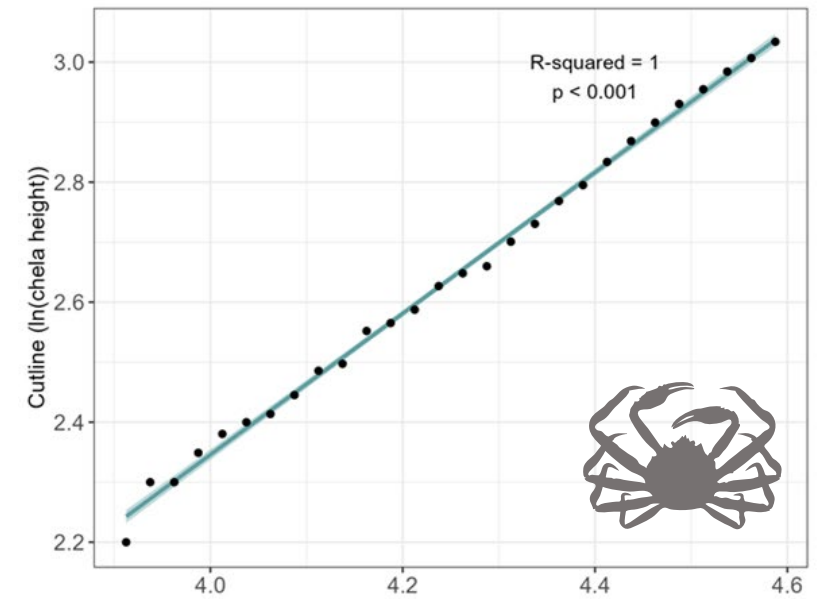


3

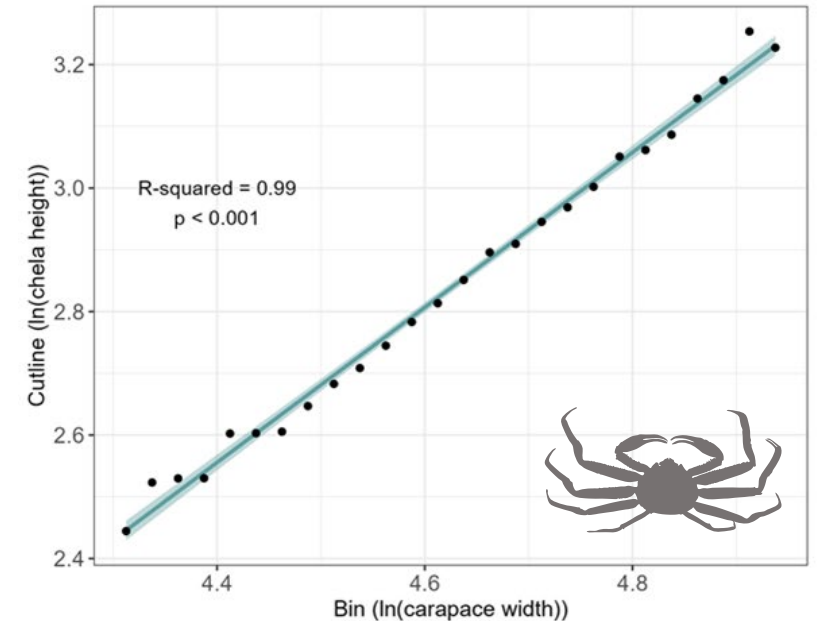
Generate $\ln(\text{CH}) \sim$
 $\ln(\text{CW})$ maturity
cutline

Only
shell 2!

snow cutline



tanner cutline



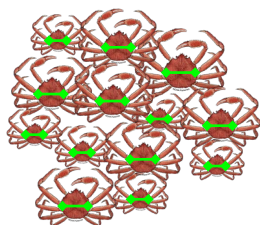
Maturity cutlines established following Richar and Foy 2022

4

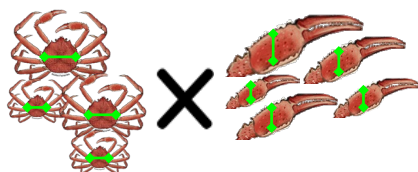
Applying maturity cutlines

SPECIMEN DATA
(subsample 1)

1

Measure
carapace widths
for crab haul
subsampleCHELA DATA
(subsample 2)

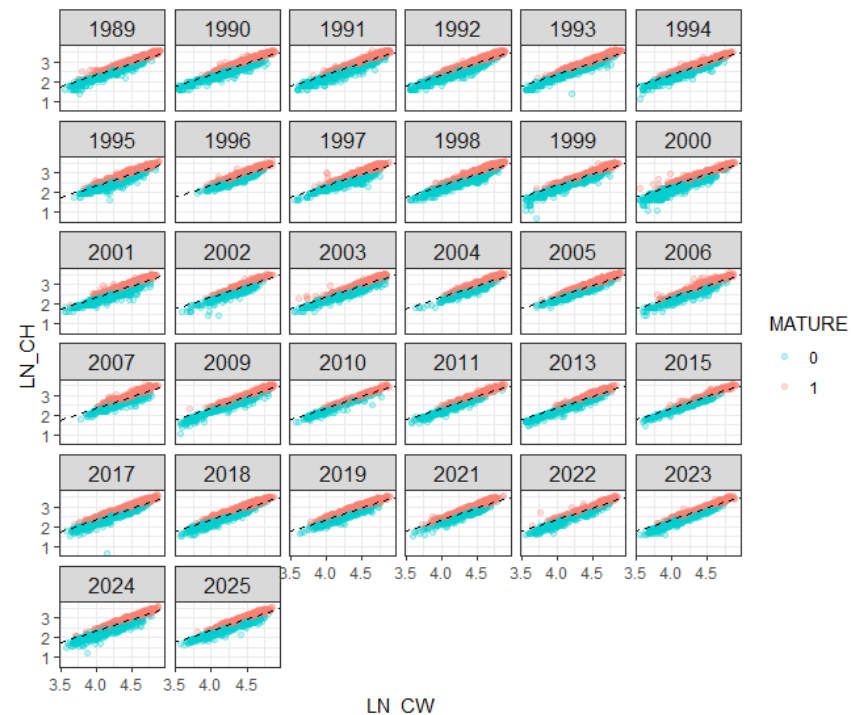
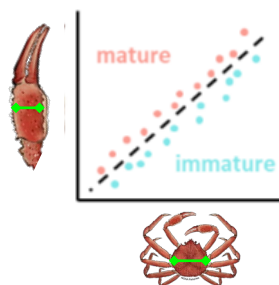
2

Measure chela
heights from
specimen data
subsample

3

Generate $\ln(\text{CH}) \sim \ln(\text{CW})$ maturity
cutline

4

Apply cutline to
chela data to assign
crab as mature or
immature

CHELA_HEIGHT	DATASET	LN_CH	LN_CW	CUTOFF	MATURE
17	CRABPACK	2.833213	4.369448	2.780418	1
24	CRABPACK	3.178054	4.615121	3.069470	1
14	CRABPACK	2.639057	4.219508	2.604001	1
12	CRABPACK	2.484907	4.127134	2.495317	0
18	CRABPACK	2.890372	4.356709	2.765429	1
25	CRABPACK	3.218876	4.615121	3.069470	1
31	CRABPACK	3.433987	4.762174	3.242490	1
24	CRABPACK	3.178054	4.615121	3.069470	1
31	CRABPACK	3.433987	4.770685	3.252504	1
25	CRABPACK	3.218876	4.615121	3.069470	1
23	CRABPACK	3.135494	4.584967	3.033993	1
17	CRABPACK	2.833213	4.317488	2.719283	1
29	CRABPACK	3.367296	4.682131	3.148314	1
23	CRABPACK	3.135494	4.564348	3.009733	1
19	CRABPACK	2.944439	4.369448	2.780418	1
13	CRABPACK	2.564949	4.189655	2.568877	0

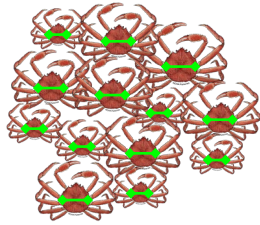
5

Fitting models to chela data to estimate probability mature at size

SPECIMEN DATA
(subsample 1)

1

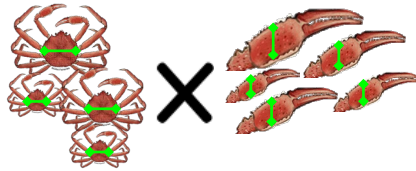
Measure
carapace widths
for crab haul
subsample



CHELA DATA
(subsample 2)

2

Measure chela
heights from
specimen data
subsample



3

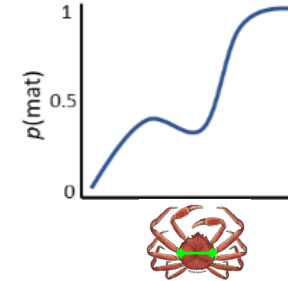
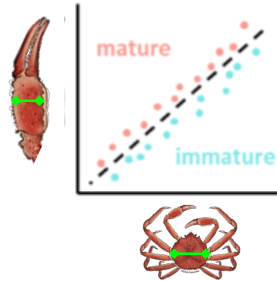
Generate $\ln(\text{CH}) \sim \ln(\text{CW})$ maturity
cutline

4

Apply cutline to
chela data to assign
crab as mature or
immature

5

Fit models to chela
maturity data to
estimate probability
mature at size



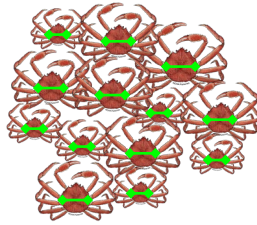
5

Fitting models to chela data to estimate probability mature at size

SPECIMEN DATA
(subsample 1)

1

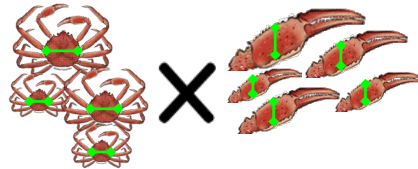
Measure
carapace widths
for crab haul
subsample



CHELA DATA
(subsample 2)

2

Measure chela
heights from
specimen data
subsample

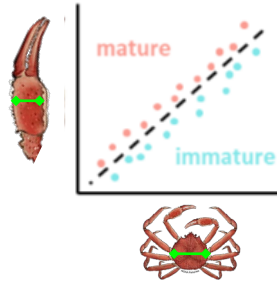


3

Generate $\ln(\text{CH}) \sim \ln(\text{CW})$ maturity
cutline

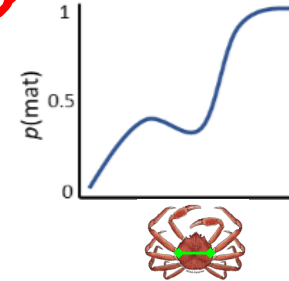
4

Apply cutline to
chela data to assign
crab as mature or
immature



5

Fit models to chela
maturity data to
estimate probability
mature at size



Legacy workflow



Fitting models to chela data to estimate probability mature at size

1. Bin chela data into 10mm bins
2. Calculate proportion mature within each bin using sampling factor

5

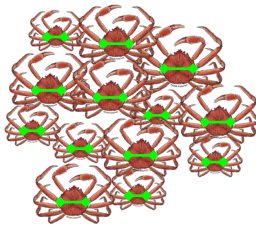
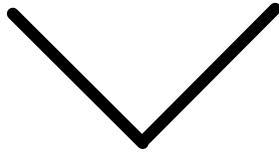
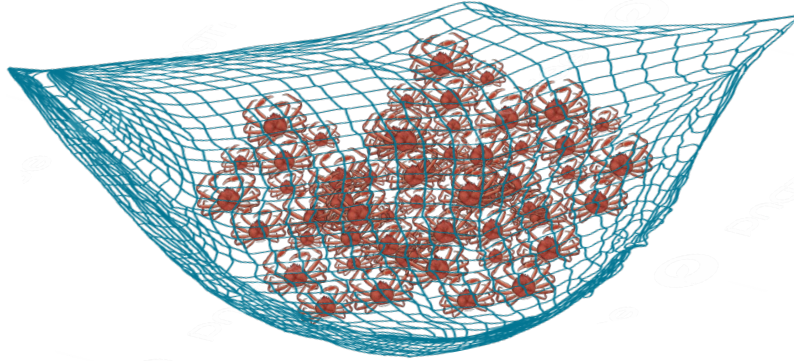
Fitting models to chela data to estimate probability mature at size

1. Bin chela data into 10mm bins
2. Calculate proportion mature within each bin using sampling factor



5

Fitting models to chela data to estimate probability mature at size



SPECIMEN DATA
(subsample 1)

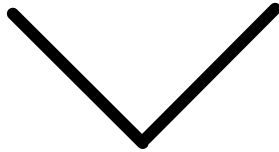
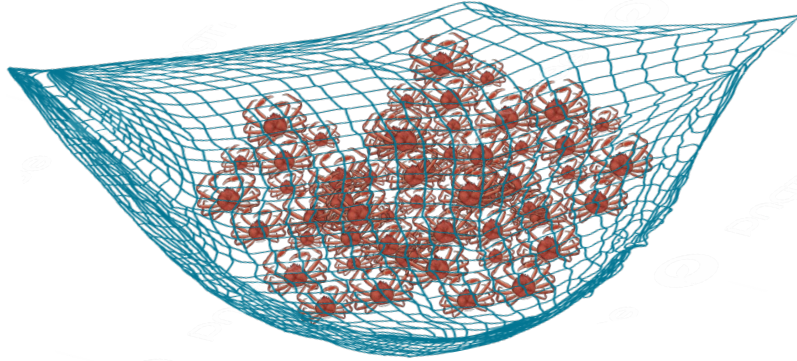
1

Measure
carapace widths
for crab haul
subsample

Sampling factor = abundance at size in
subsample 1 after accounting for
subsampling intensity for subsample 1

5

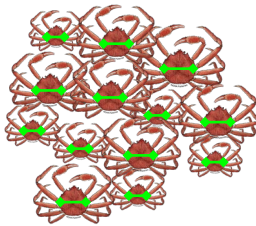
Fitting models to chela data to estimate probability mature at size



SPECIMEN DATA
(subsample 1)

1

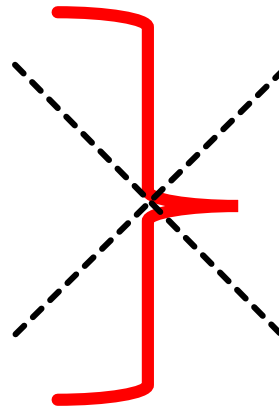
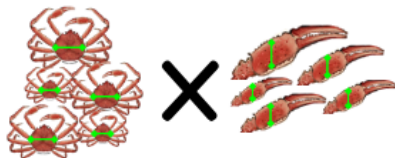
Measure
carapace widths
for crab haul
subsample



CHELA DATA
(subsample 2)

2

Measure chela
heights from
specimen data
subsample



Sampling factor does not apply to
subsampling for chela (subsample 2)

5

Fitting models to chela data to estimate probability mature at size

1. Bin chela data into 10mm bins
2. Calculate proportion mature within each bin using sampling factor
3. Fit logistic models to proportion mature by 10mm bin, separate by year

```
mod <- nls(PROP_MATURE ~ (1/(1 + exp(-a*(SIZE_BIN - b)))),
  data = dat,
  start = list(a = 0.10, b = 60.0),
  na.action = na.omit, nls.control(maxiter = 5000))
```

YEAR	SIZE_BIN	A_EST	A_SE	B_EST	B_SE	PROP_MATURE
1989	75	0.1069941	0.01022512	90.65492	1.014503	0.2232185
1989	85	0.1069941	0.01022512	90.65492	1.014503	0.2423178
1989	105	0.1069941	0.01022512	90.65492	1.014503	0.7893232
1989	85	0.1069941	0.01022512	90.65492	1.014503	0.2837318
1989	105	0.1069941	0.01022512	90.65492	1.014503	0.7515437
1989	75	0.1069941	0.01022512	90.65492	1.014503	0.1725031

5

Fitting models to chela data to estimate probability mature at size

1. Bin chela data into 10mm bins
2. Calculate proportion mature within each bin using sampling factor
3. Fit logistic models to proportion mature by 10mm bin, separate by year
 - Does not account for uncertainty due to bin sample sizes
 - Does not account for spatiotemporal variability

```
mod <- nls(PROP_MATURE ~ (1/(1 + exp(-a*(SIZE_BIN - b)))),
  data = dat,
  start = list(a = 0.10, b = 60.0),
  na.action = na.omit, nls.control(maxiter = 5000))
```

YEAR	SIZE_BIN	A_EST	A_SE	B_EST	B_SE	PROP_MATURE
1989	75	0.1069941	0.01022512	90.65492	1.014503	0.2232185
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1989	105	0.1069941	0.01022512	90.65492	1.014503	0.7893232
1989	85	0.1069941	0.01022512	90.65492	1.014503	0.2837318
1989	105	0.1069941	0.01022512	90.65492	1.014503	0.7515437
1989	75	0.1069941	0.01022512	90.65492	1.014503	0.1725031

6

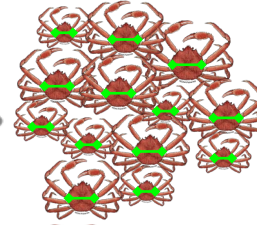
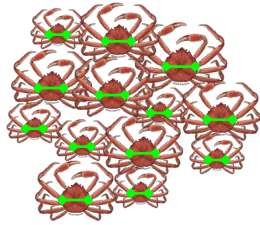
Use models to predict probability maturity at size for all specimen crab

YEAR	SIZE_BIN	A_EST	A_SE	B_EST	B_SE	PROP_MATURE
1989	75	0.1069941	0.01022512	90.65492	1.014503	0.2232185
1989	85	0.1069941	0.01022512	90.65492	1.014503	0.2423178
1989	105	0.1069941	0.01022512	90.65492	1.014503	0.7893232
1989	85	0.1069941	0.01022512	90.65492	1.014503	0.2837318
1989	105	0.1069941	0.01022512	90.65492	1.014503	0.7515437
1989	75	0.1069941	0.01022512	90.65492	1.014503	0.1725031

SPECIMEN DATA
(subsample 1)

1

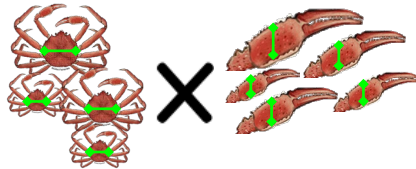
Measure
carapace widths
for crab haul
subsample



CHELA DATA
(subsample 2)

2

Measure chela
heights from
specimen data
subsample

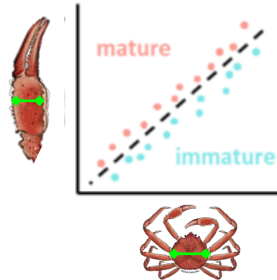


3

Generate $\ln(\text{CH}) \sim \ln(\text{CW})$ maturity
cutline

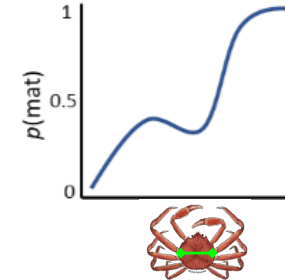
4

Apply cutline to
chela data to assign
crab as mature or
immature



5

Fit models to chela
maturity data to
estimate probability
mature at size



6

Apply maturity models
to specimen data to
estimate maturity at size
for each specimen crab



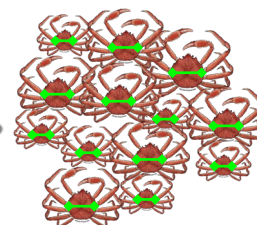
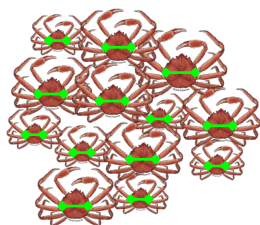
7

Calculate ogives, SAM, and mature biomass/abundance

SPECIMEN DATA
(subsample 1)

1

Measure carapace widths for crab haul subsample



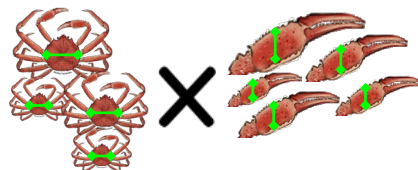
7

Calculate and plot yearly ogives, size at 50% maturity, and mature biomass/abundance

CHELA DATA
(subsample 2)

2

Measure chela heights from specimen data subsample

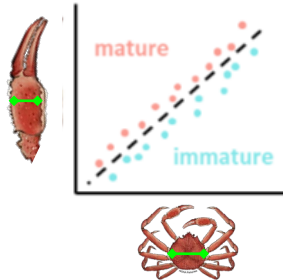


3

Generate $\ln(\text{CH}) \sim \ln(\text{CW})$ maturity cutline

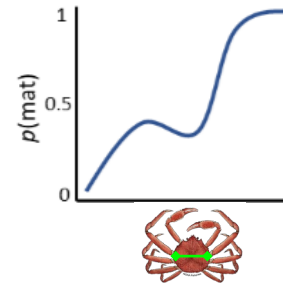
4

Apply cutline to chela data to assign crab as mature or immature



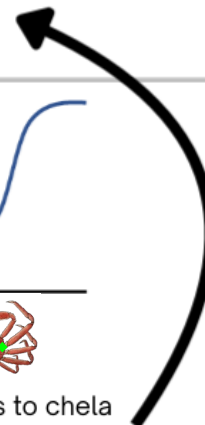
5

Fit models to chela maturity data to estimate probability mature at size



6

Apply maturity models to specimen data to estimate maturity at size for each specimen crab

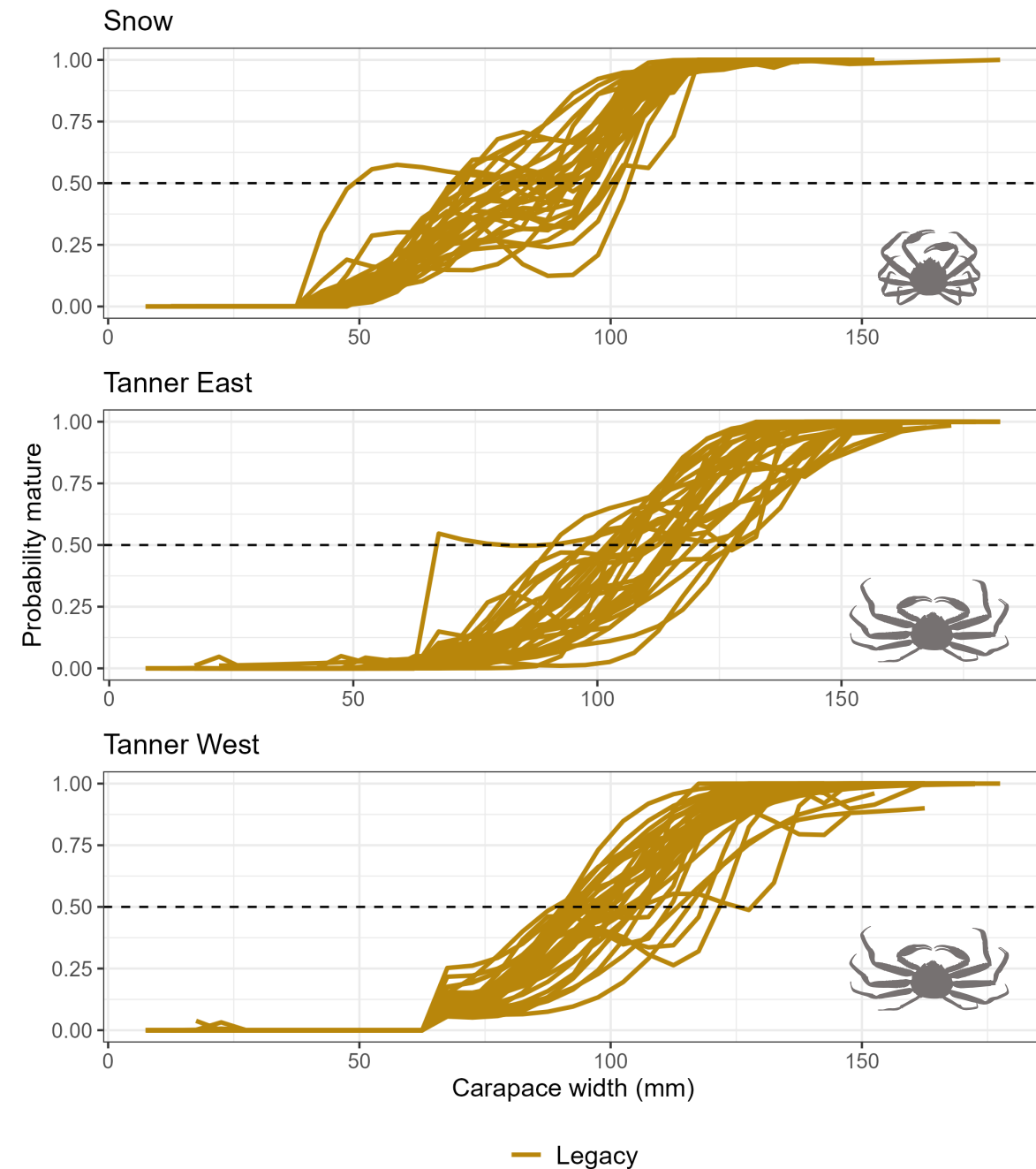


7

Calculate ogives, SAM, and mature biomass/abundance

Ogives calculated by:

1. Computing the mean probability mature by 10mm size bin each year, interpolated to 5mm bins for comparison with updated workflow

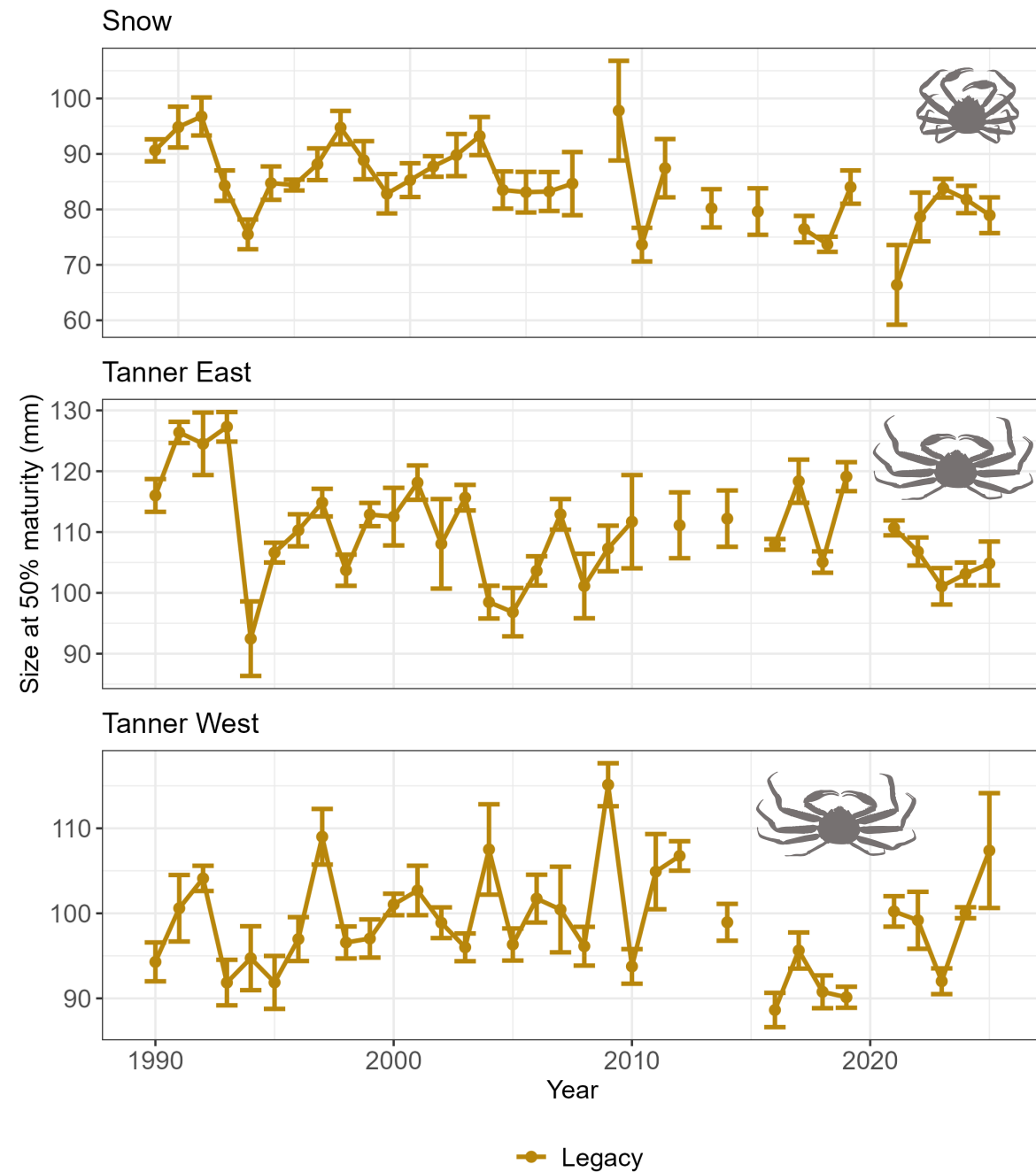


7

Calculate ogives, SAM, and mature biomass/abundance

Size-at-50% maturity (SAM) calculated by:

1. Using yearly SAM parameter estimates from the models
2. Using yearly SAM standard error estimates from the models for uncertainty

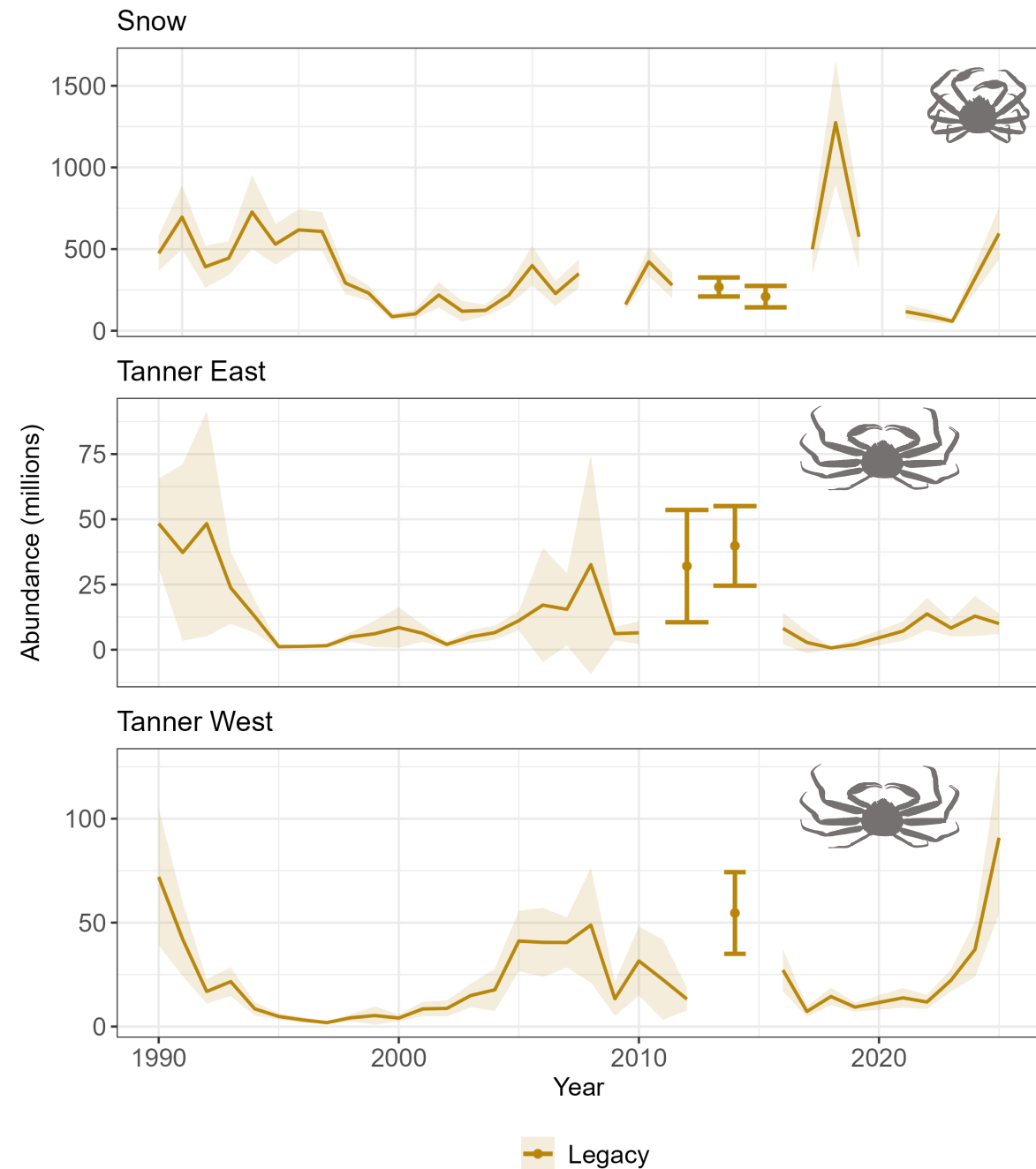


7

Calculate ogives, SAM, and mature biomass/abundance

Mature abundance/biomass calculated by:

1. Multiplying probability mature at size and abundance at size (sampling factor) to get mature abundance/biomass at size
2. Mature abundance/biomass at size is then expanded via standard design-based methods



Legacy workflow	Proposed workflow
Uses 10mm bins	Uses 5mm bins
Fits nls logistic models to chela data	Fits sdmTMB models to chela data
Uses proportion mature as the response, calculated using sampling factor	Uses binomial (mature/immature) as response

Legacy workflow	Proposed workflow
Uses 10mm bins	Uses 5mm bins
Fits nls logistic models to chela data	Fits sdmTMB models to chela data
Uses proportion mature as the response, calculated using sampling factor	Uses binomial (mature/immature) as response
Assumes logistic maturity-at-size ogive shape	Flexibly models maturity-at-size via gam-style smooths

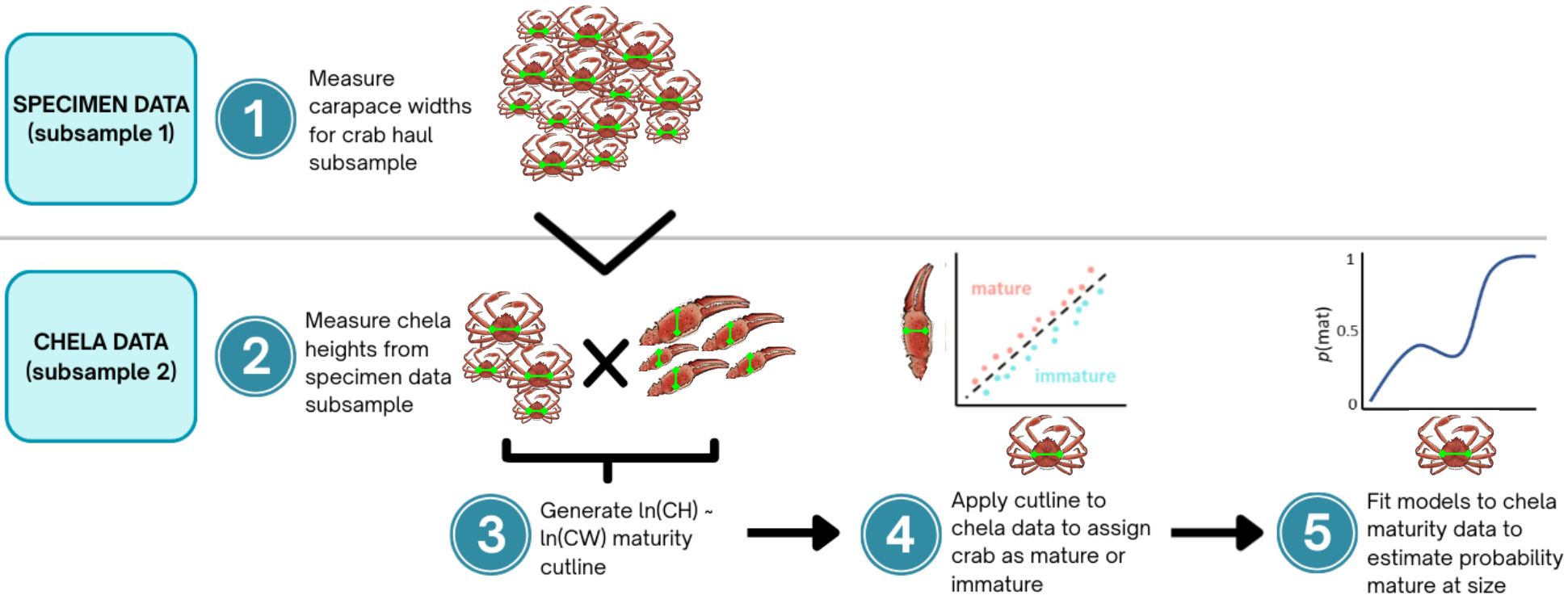
Legacy workflow	Proposed workflow
Uses 10mm bins	Uses 5mm bins
Fits nls logistic models to chela data	Fits sdmTMB models to chela data
Uses proportion mature as the response, calculated using sampling factor	Uses binomial (mature/immature) as response
Assumes logistic maturity-at-size ogive shape	Flexibly models maturity-at-size via gam-style smooths
Does not account for uncertainty in maturity due to uneven sampling across space, time, and size bins	Robust to spatiotemporal gaps and variability in maturity through random fields; uncertainty is also tied to sample sizes via binomial structure and propagated across all workflow steps

Legacy workflow	Proposed workflow
Uses 10mm bins	Uses 5mm bins
Fits nls logistic models to chela data	Fits sdmTMB models to chela data
Uses proportion mature as the response, calculated using sampling factor	Uses binomial (mature/immature) as response
Assumes logistic maturity-at-size ogive shape	Flexibly models maturity-at-size via gam-style smooths
Does not account for uncertainty in maturity due to uneven sampling across space, time, and size bins	Robust to spatiotemporal gaps and variability in maturity through random fields; uncertainty is also tied to sample sizes via binomial structure and propagated across all workflow steps
Models not vetted through diagnostics(?)	Models vetted through diagnostics

Legacy workflow	Proposed workflow
Uses 10mm bins	Uses 5mm bins
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Assumes logistic maturity-at-size ogive shape	Flexibly models maturity-at-size via gam-style smooths
Does not account for uncertainty in maturity due to uneven sampling across space, time, and size bins	Robust to spatiotemporal gaps and variability in maturity through random fields; uncertainty is also tied to sample sizes via binomial structure and propagated across all workflow steps
Models not vetted through diagnostics(?)	Models vetted through diagnostics
SAM and ogives do not account for population size	SAM and ogives are weighted by abundance to account for population size

Proposed workflow

Steps 1-4 the same as the legacy workflow



5

Fitting models to chela data to estimate probability mature at size

1. Bin chela data into 5mm bins
2. Fit sdmTMB models to binomial (mature/immature) individual crab data by 5mm size bin
 - Binomial: bins with more samples carry more weight in the likelihood
 - Spatial = "on": captures persistent space-only deviations
 - Spatiotemporal = "iid": captures year-specific spatial deviations, though no correlation across years ("ar1")
 - Uneven sampling accounted for in random fields
 - Anisotropy in spatial deviations
 - Also `spatial_varying()` and `time_varying()` arguments
3. Evaluate various model parameterizations using `sanity()`, k-fold cv, and DHARMA residuals

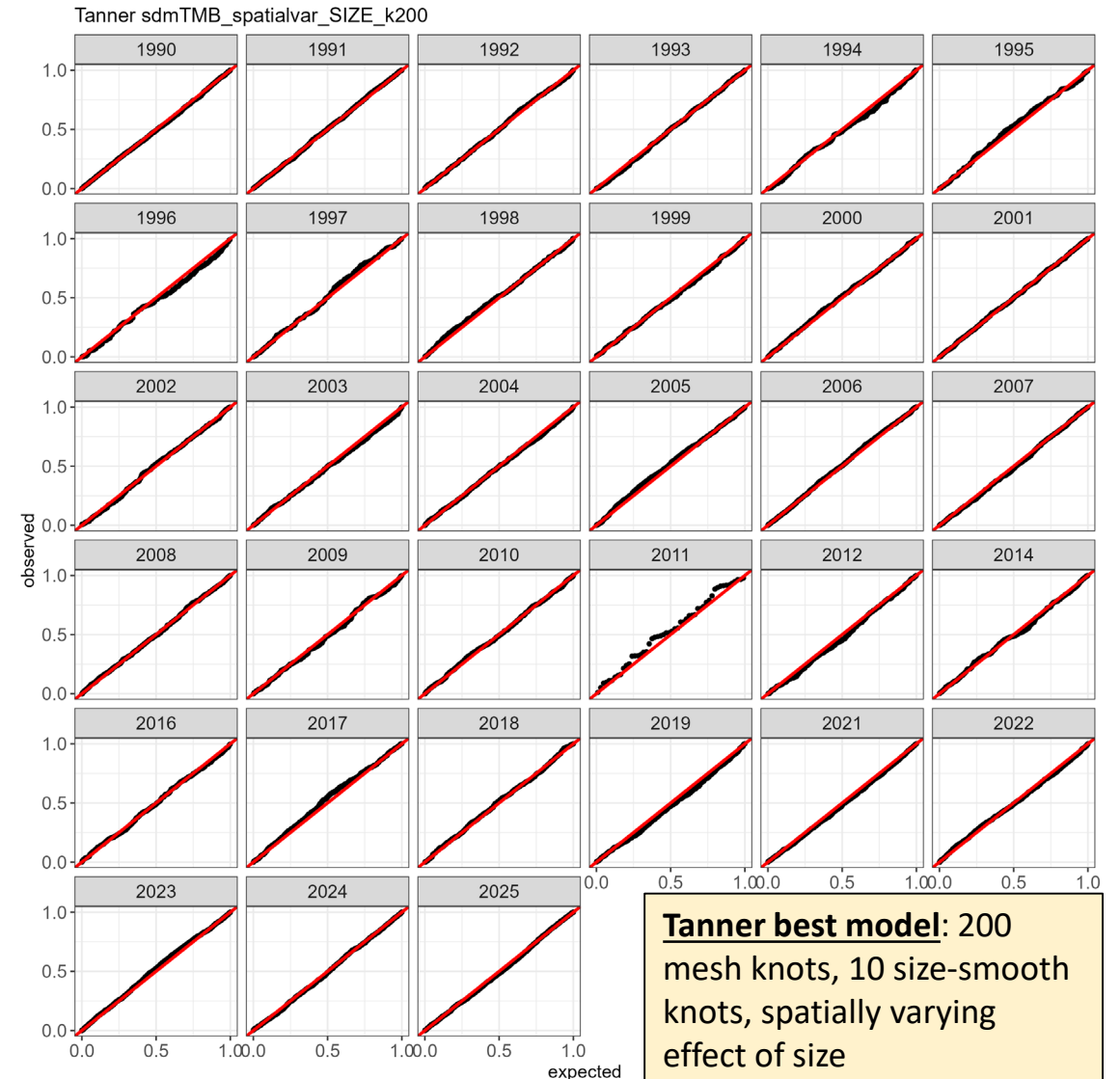
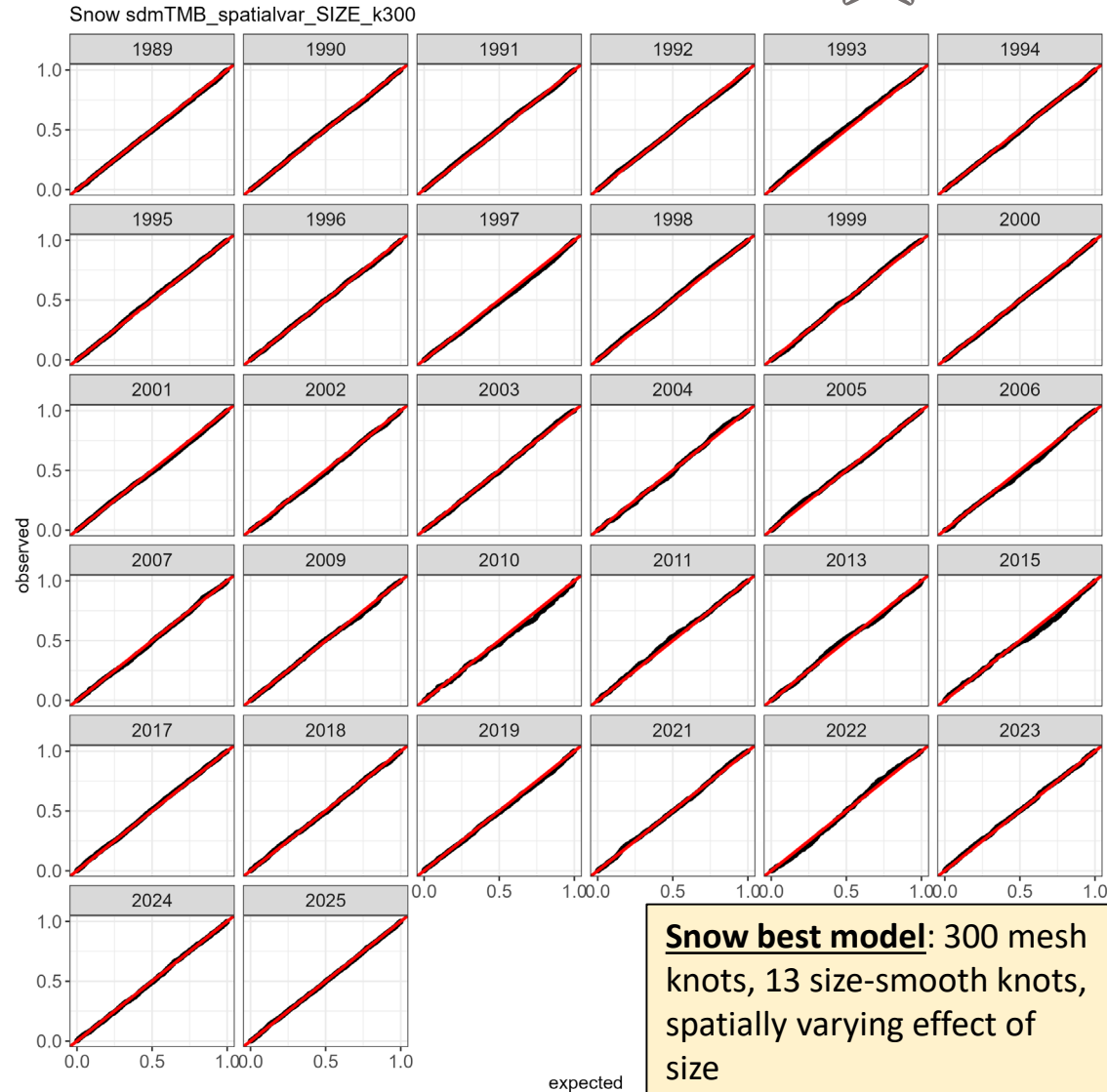
```
mod.1 <- sdmTMB(  
  MATURE ~ s(SIZE_5MM, k = 10) + YEAR_F,  
  spatial = "on",  
  spatiotemporal = "iid",  
  mesh = mat.msh,  
  family = binomial(),  
  time = "YEAR",  
  extra_time = xtra.time,  
  anisotropy = TRUE,  
  data = tanner.chela  
)
```

5

Fitting models to chela data to estimate probability mature at size



*see document for more diagnostics



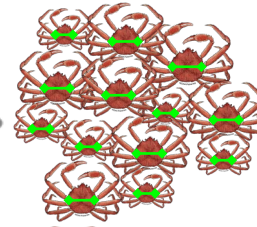
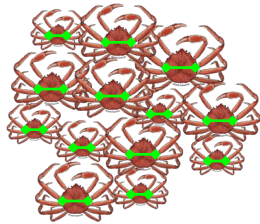
6

Use models to predict probability maturity at size for all specimen crab

SPECIMEN DATA
(subsample 1)

1

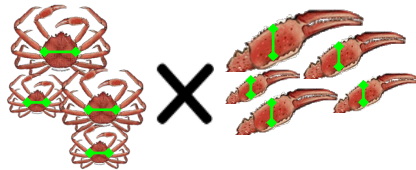
Measure
carapace widths
for crab haul
subsample



CHELA DATA
(subsample 2)

2

Measure chela
heights from
specimen data
subsample

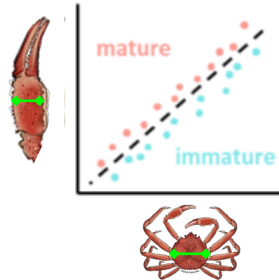


3

Generate $\ln(\text{CH}) \sim \ln(\text{CW})$ maturity
cutline

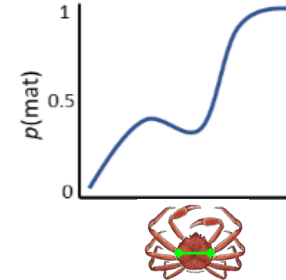
4

Apply cutline to
chela data to assign
crab as mature or
immature



5

Fit models to chela
maturity data to
estimate probability
mature at size



6

Apply maturity models
to specimen data to
estimate maturity at size
for each specimen crab



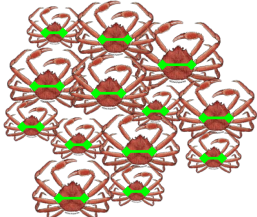
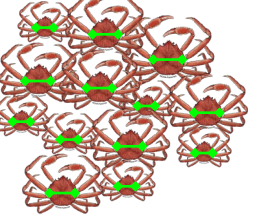
7

Calculate ogives, SAM, and mature biomass/abundance

SPECIMEN DATA
(subsample 1)

1

Measure carapace widths for crab haul subsample



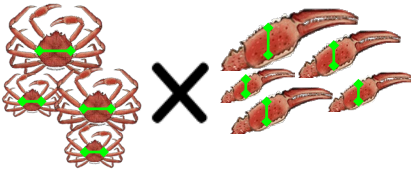
7

Calculate and plot yearly ogives, size at 50% maturity, and mature biomass/abundance

CHELA DATA
(subsample 2)

2

Measure chela heights from specimen data subsample

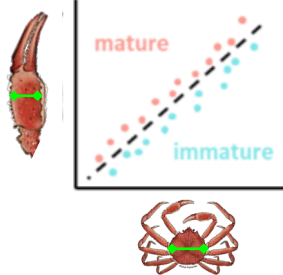


3

Generate $\ln(\text{CH}) \sim \ln(\text{CW})$ maturity cutline

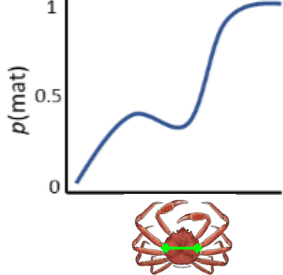
4

Apply cutline to chela data to assign crab as mature or immature



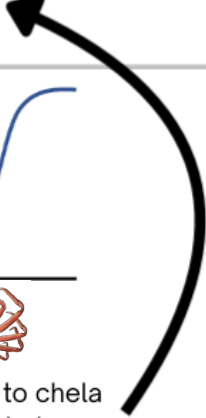
5

Fit models to chela maturity data to estimate probability mature at size



6

Apply maturity models to specimen data to estimate maturity at size for each specimen crab

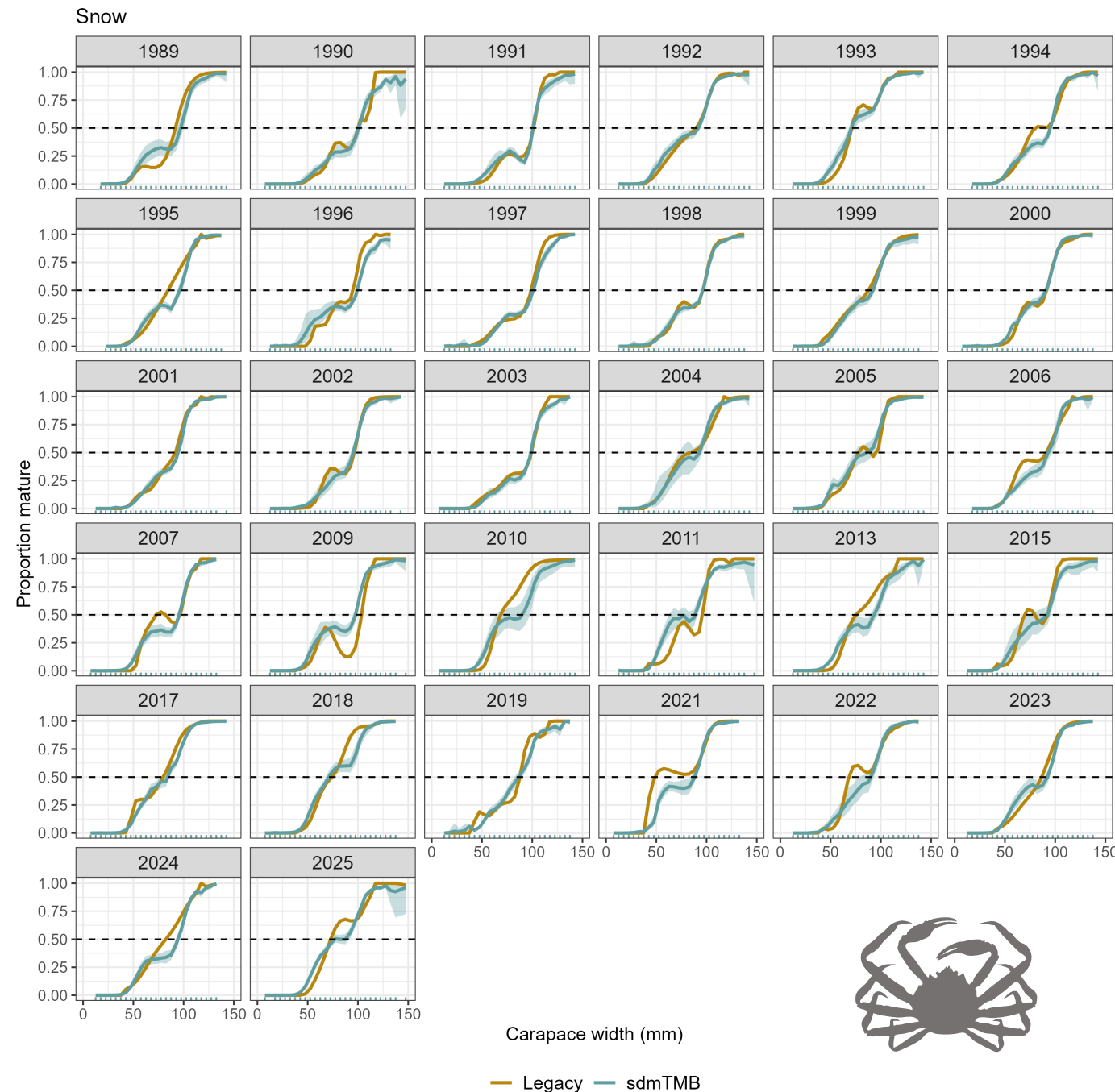


7

Calculate ogives, SAM, and mature biomass/abundance

Ogives calculated by:

1. Simulating 500 draws from each model's joint precision matrix
2. Computing the mean probability mature at size across draws each year, weighted by abundance at size
3. Quantifying uncertainty by summarizing ogive variation across draws

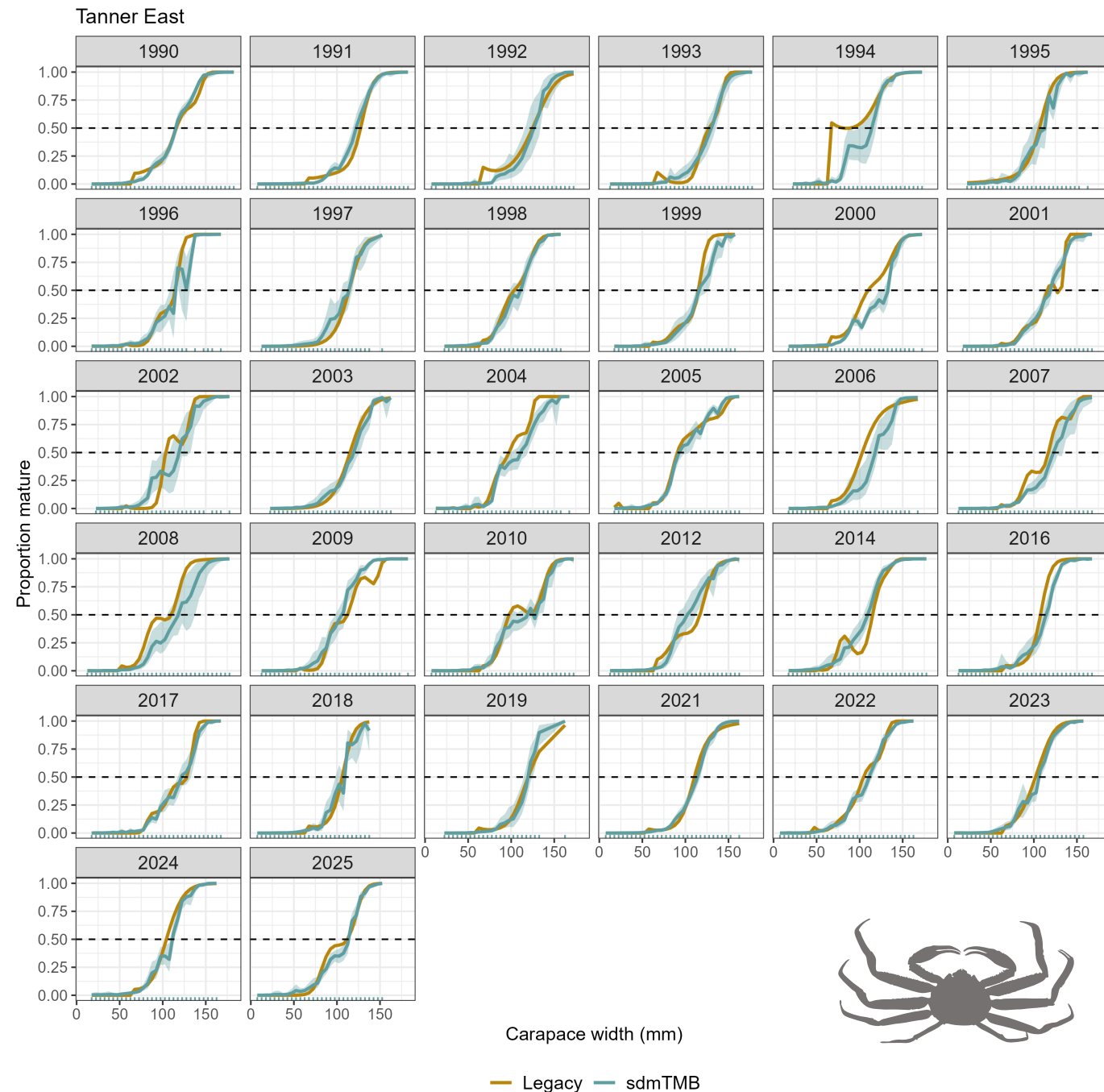


7

Calculate ogives, SAM, and mature biomass/abundance

Ogives calculated by:

1. Simulating 500 draws from each model's joint precision matrix
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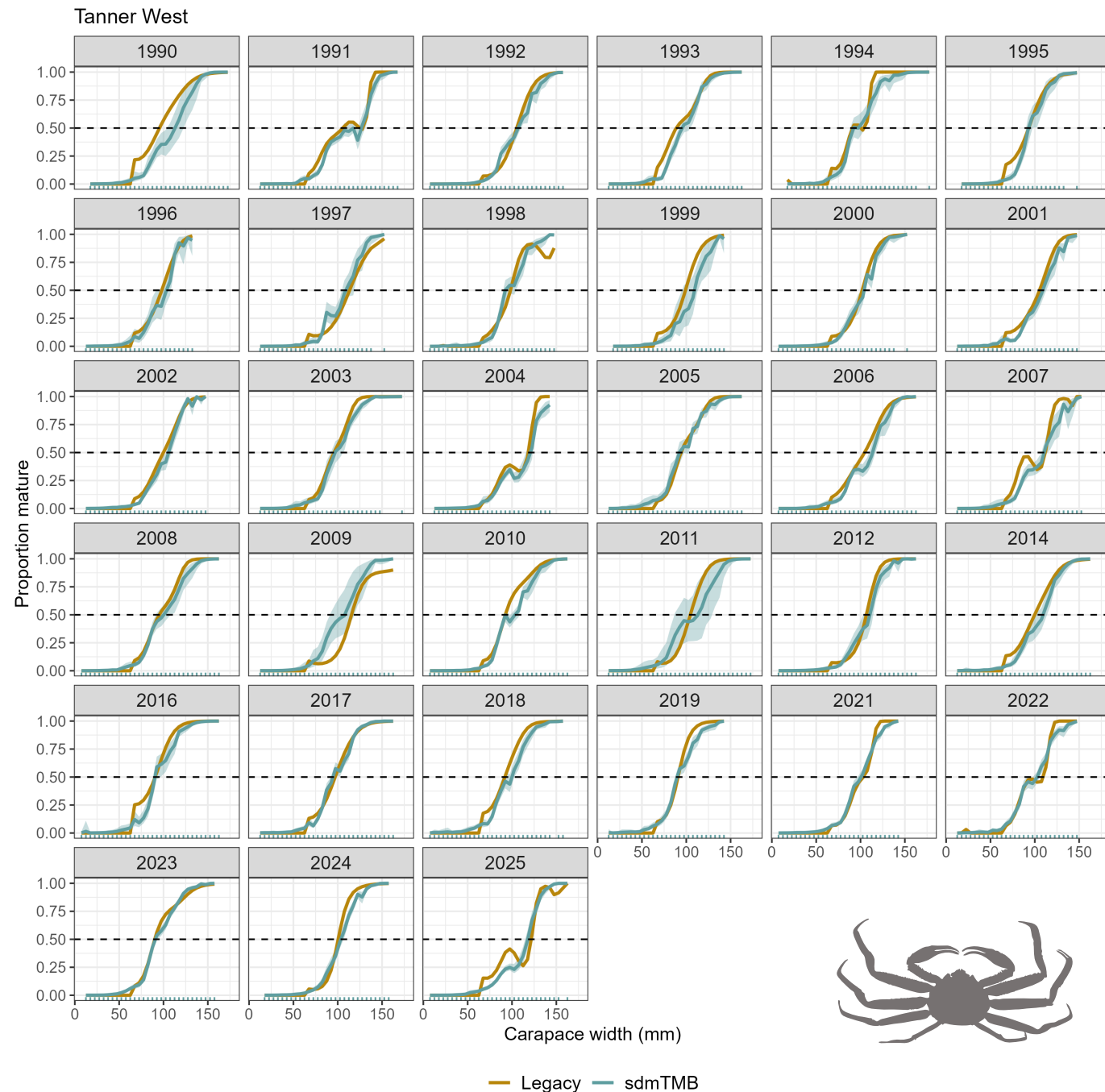


7

Calculate ogives, SAM, and mature biomass/abundance

Ogives calculated by:

1. Simulating 500 draws from each model's joint precision matrix
2. Computing the mean probability mature at size across draws each year, weighted by abundance at size
3. Quantifying uncertainty by summarizing ogive variation across draws

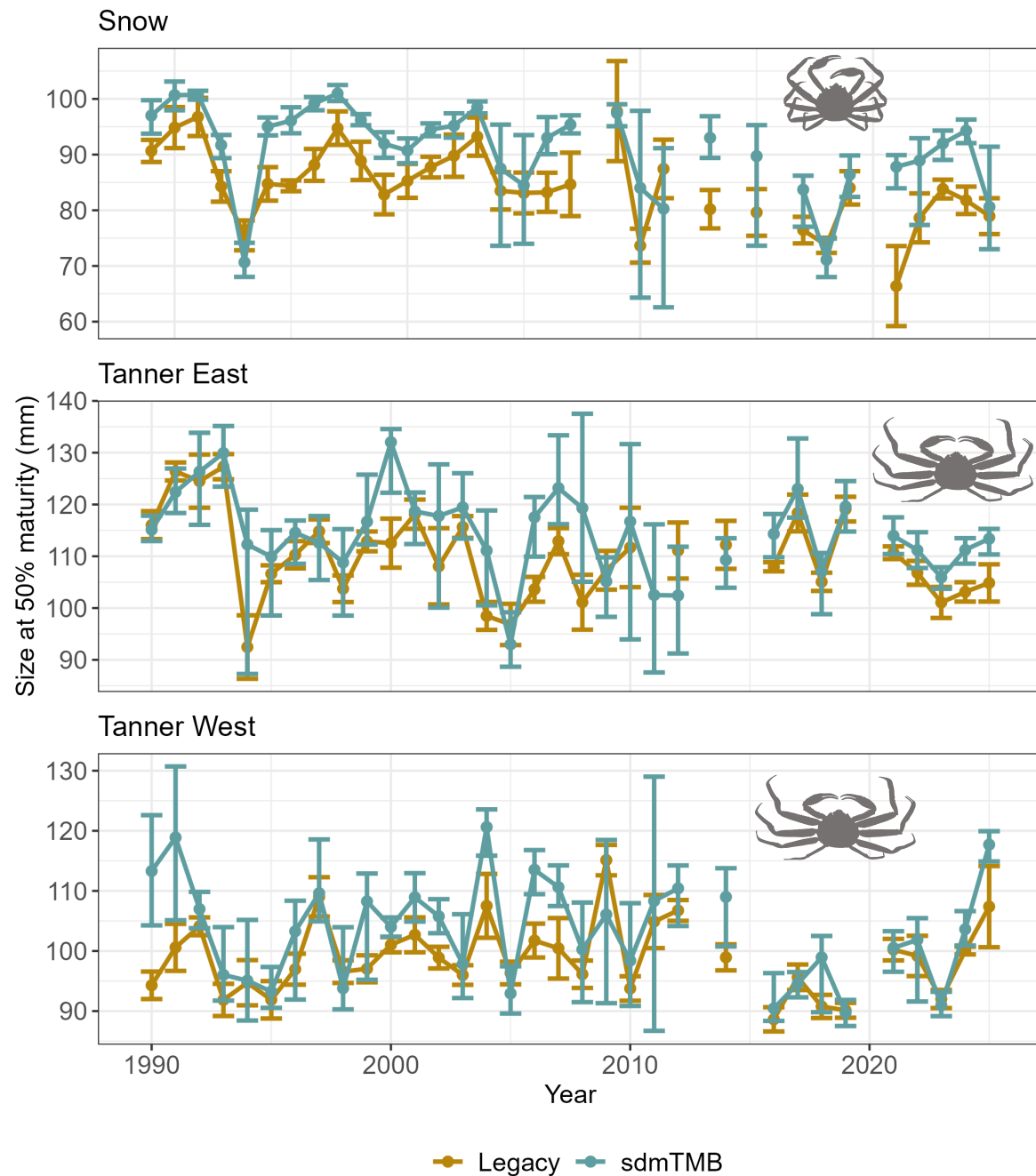


7

Calculate ogives, SAM, and mature biomass/abundance

SAM calculated by:

1. Using weighted probability mature to calculate the size at which each yearly ogive first crosses 50%, averaged across the 500 draws
2. Quantifying uncertainty by summarizing SAM variation across draws

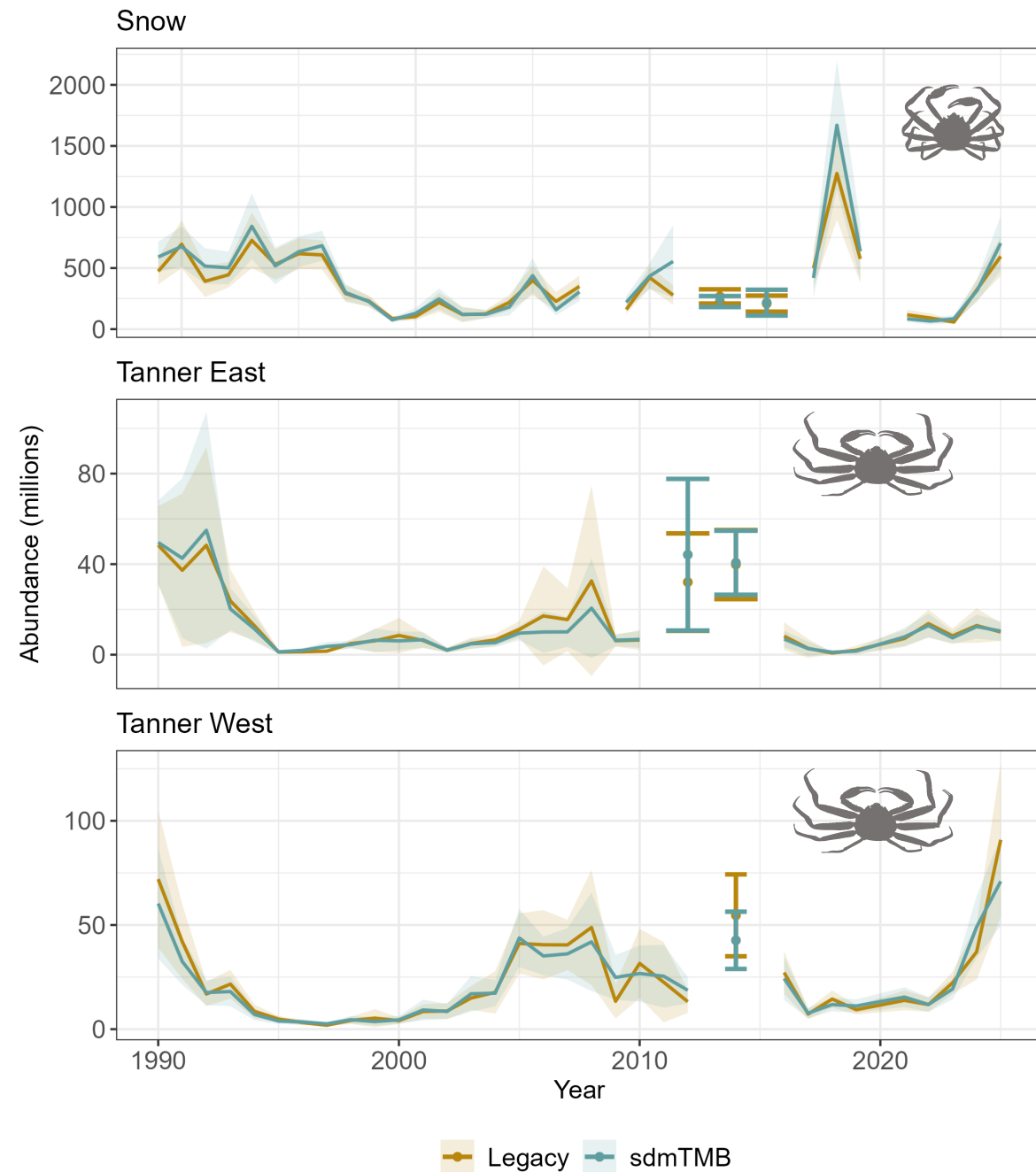


7

Calculate ogives, SAM, and mature biomass/abundance

Mature abundance/biomass calculated by:

1. Expanding mature abundance/biomass at size via standard design-based methods for each draw, then averaged across the 500 draws
2. Quantifying uncertainty as model variation across draws combined with design-based expansion uncertainty



Conclusions

Accounting for spatiotemporal variation and multiple uncertainty sources in *Chionoecetes* maturity is essential for stock biology and reliable assessment inputs.

The updated workflow:

1. Removes the use of the sampling factor to model maturity in subsample two, eliminating inappropriate commingling of subsamples.
2. Uses sdmTMB to account for spatiotemporal variation, handles data gaps from uneven sampling, and enables future spatiotemporal maturity research.
3. Propagates uncertainty from model-based maturity estimates into downstream outputs.
4. Flexibly models maturity-at-size, strengthening confidence that non-logistic ogives represent biological signal via strong diagnostics