A close-up photograph of a red king crab's legs and body. The crab has a dark, reddish-brown shell with numerous small white spots. Its long, spindly legs are a lighter orange color. The background is a soft, out-of-focus grey.

# Spatiotemporal model-based indices of abundance for Norton Sound red king crab

Crab Plan Team, May 2025

Caitlin Stern

# Norton Sound red king crab and model-based indices

SSC and CPT concerns:

- consistency of area over which abundance is estimated
- sufficient diagnostics for evaluating spatiotemporal models

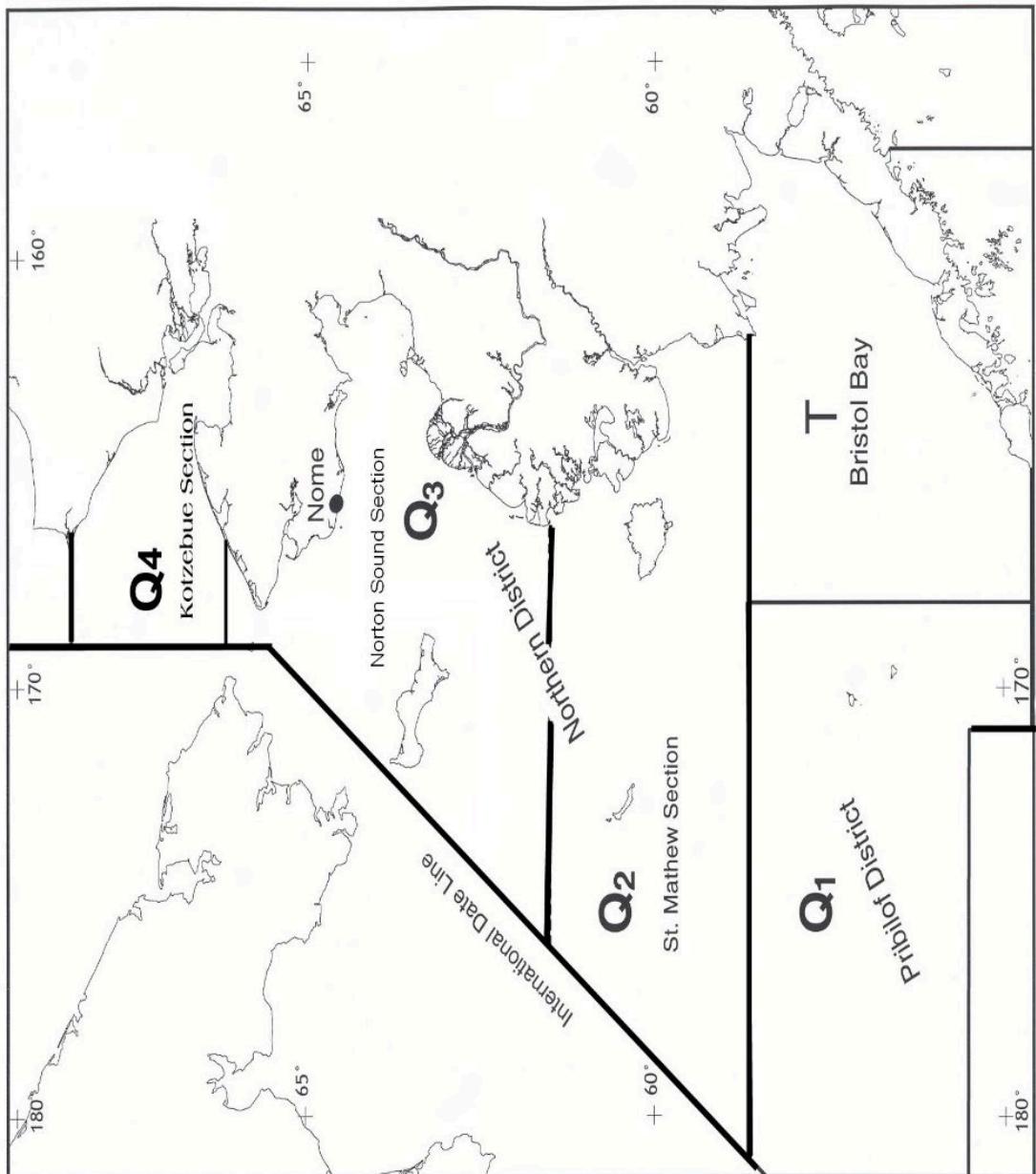
Outline:

- stock and surveys
- modeling approach
- model evaluation and diagnostics
- model-based vs. design-based indices
- future work

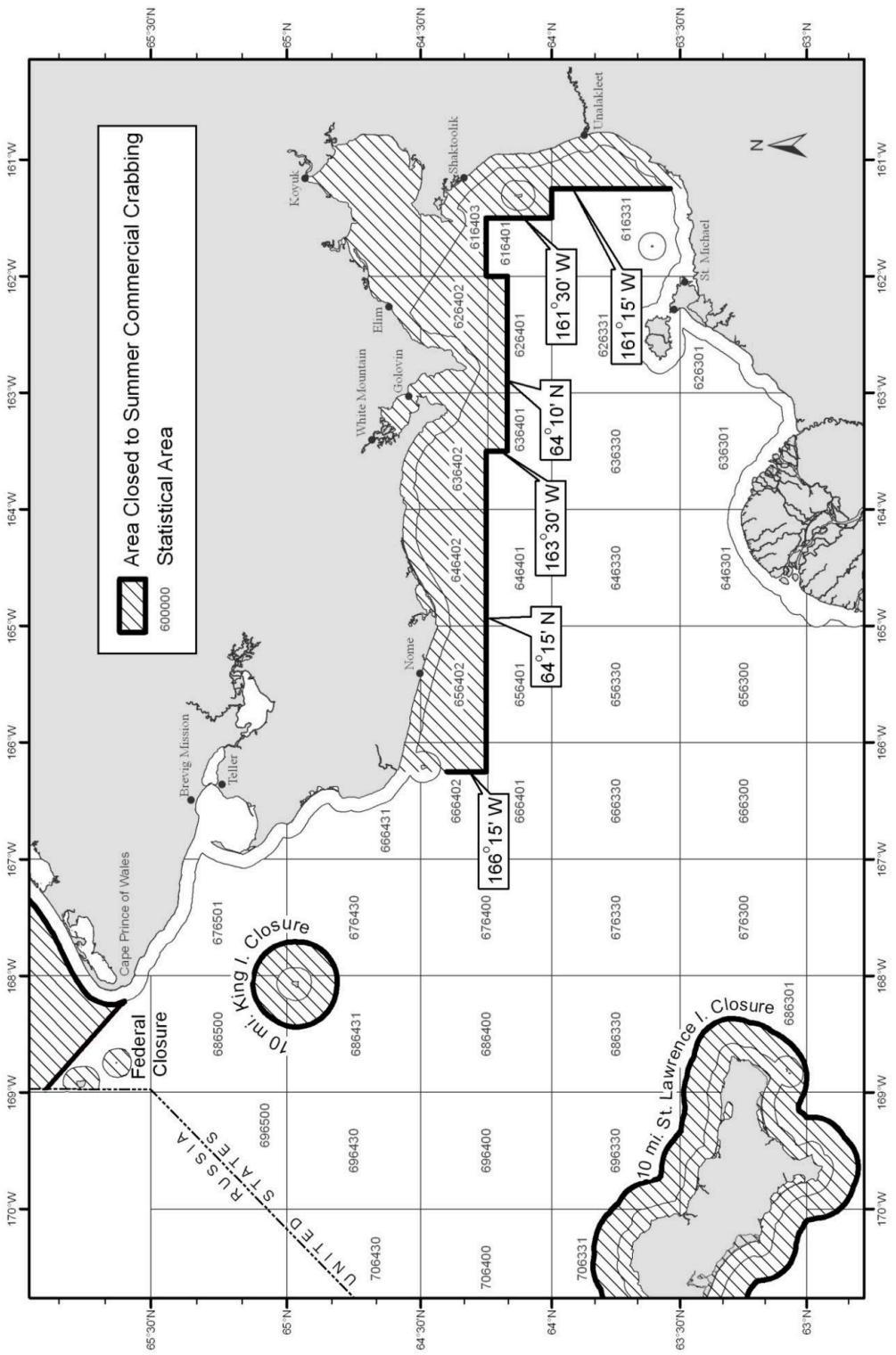
Feedback: area over which to estimate abundance



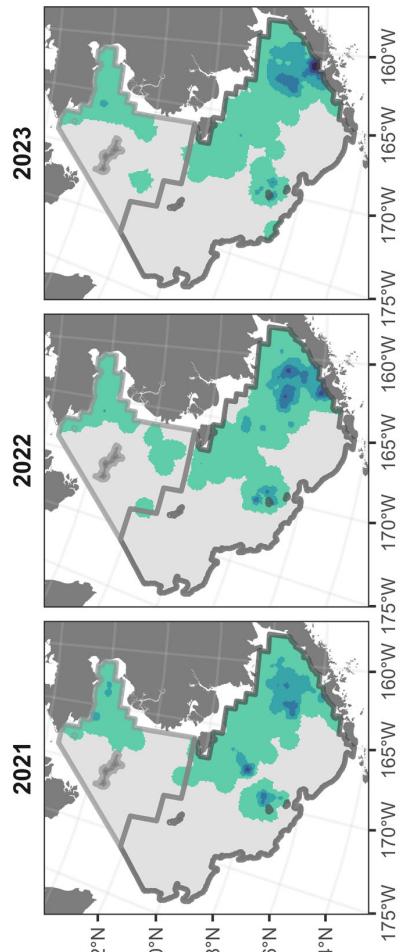
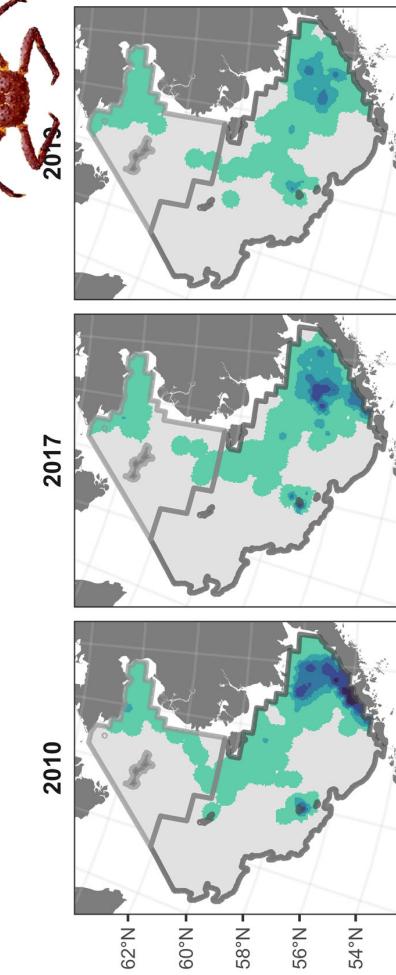
# Norton Sound red king crab stock



# Norton Sound red king crab stock



# Norton Sound red king crab stock



Markowitz et al. (2023)  
Northern Bering Sea  
groundfish and crab trawl  
survey highlights. NOAA  
Community Report.

Red king crab  
Weight CPUE (kg/km<sup>2</sup>)

No catch	>0–3	>3–9	>9–19	>19–40	>40–82
Light gray	Medium green	Dark green	Dark blue	Very dark blue	Black



# Trawl surveys

Survey	Years	Grid	Gear	Net width	Tow length	Stations (median)
NOAA NS	1976-1991	10 nm	83-112	50 ft	1.3-1.7 nm	53-104 (78.5)
ADF&G	1996-2024	10 nm	400	40 ft	1.0 nm	39-100 (54.5)
NOAA NBS	2010-2023	20 nm	83-112	50 ft	1.3-2.5 nm	34-35 (35)

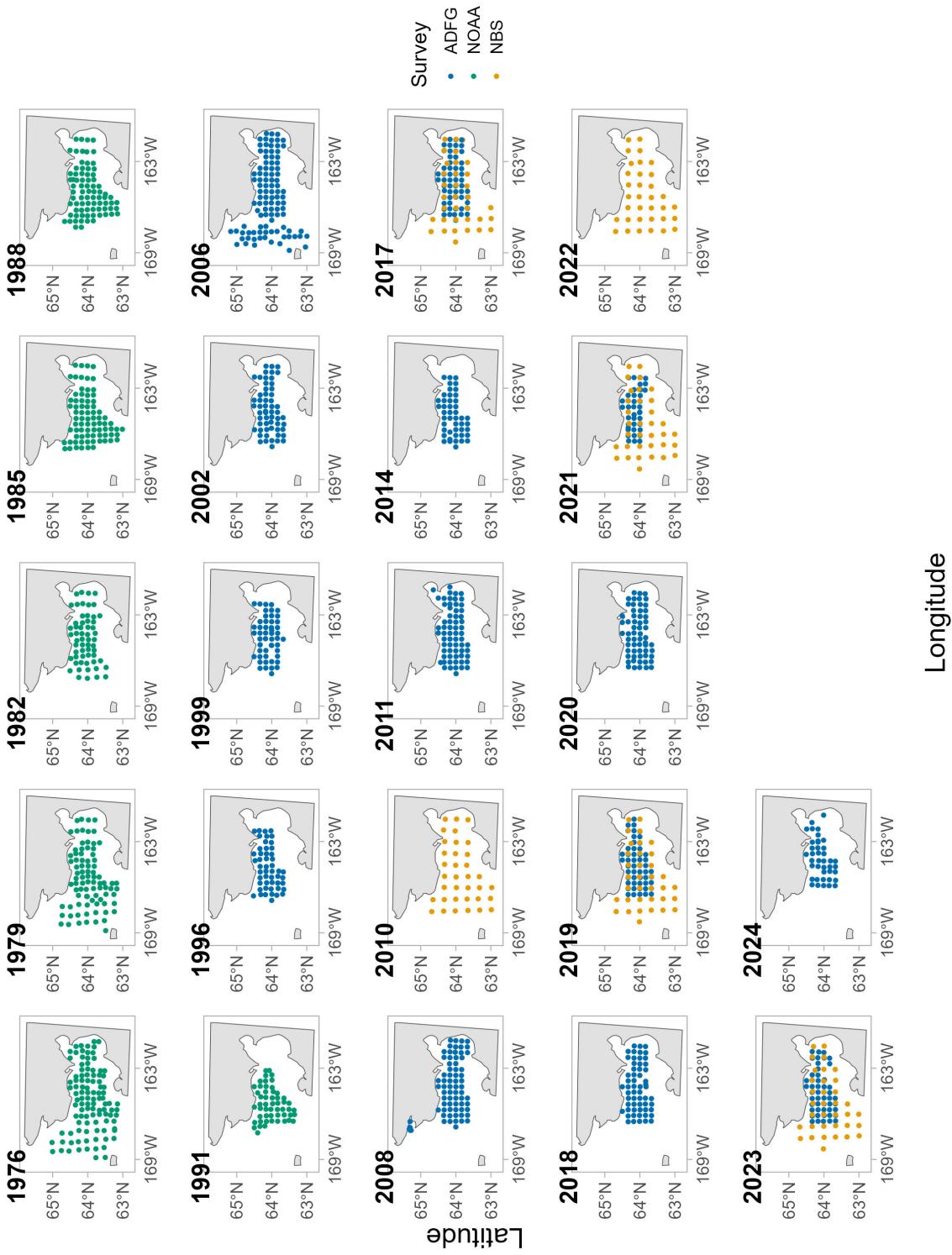
All surveys use Eastern Otter trawl gear

ADF&G and NOAA NBS surveys expected to occur in 2025

Only including males  $\geq$  64 mm in carapace length

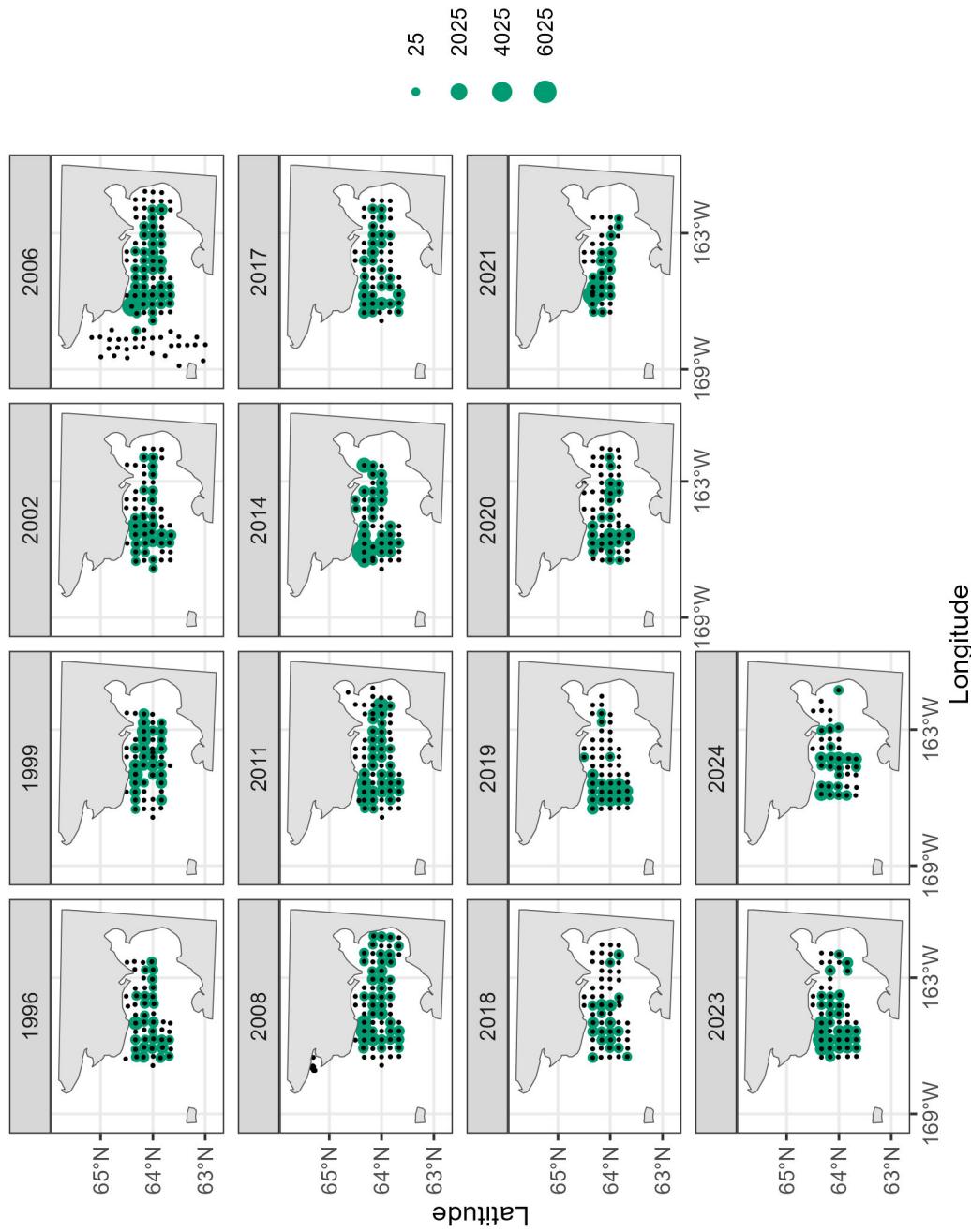


# Survey areas sampled



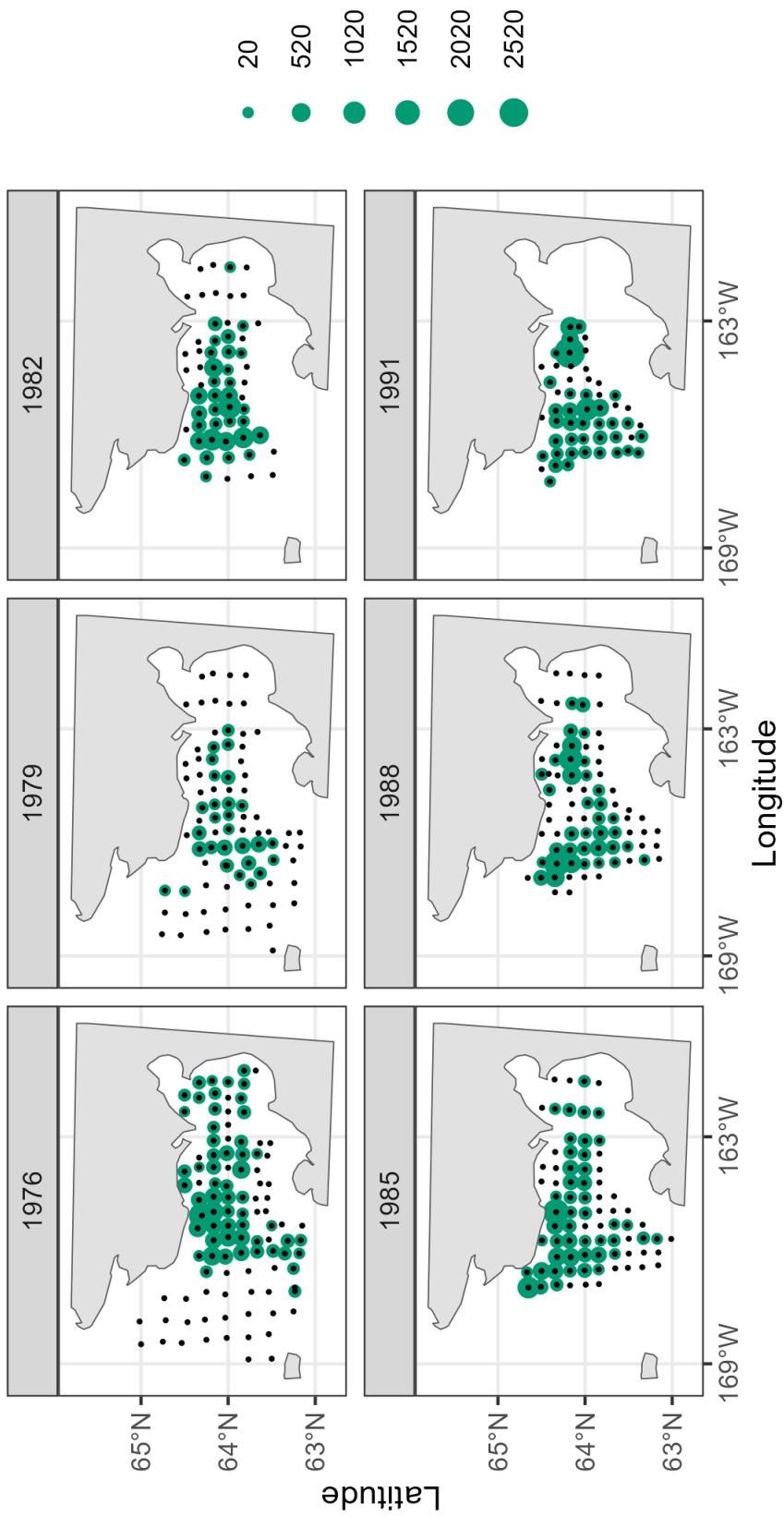
# Survey abundance by station

ADFG trawl survey estimated crab per km<sup>2</sup>



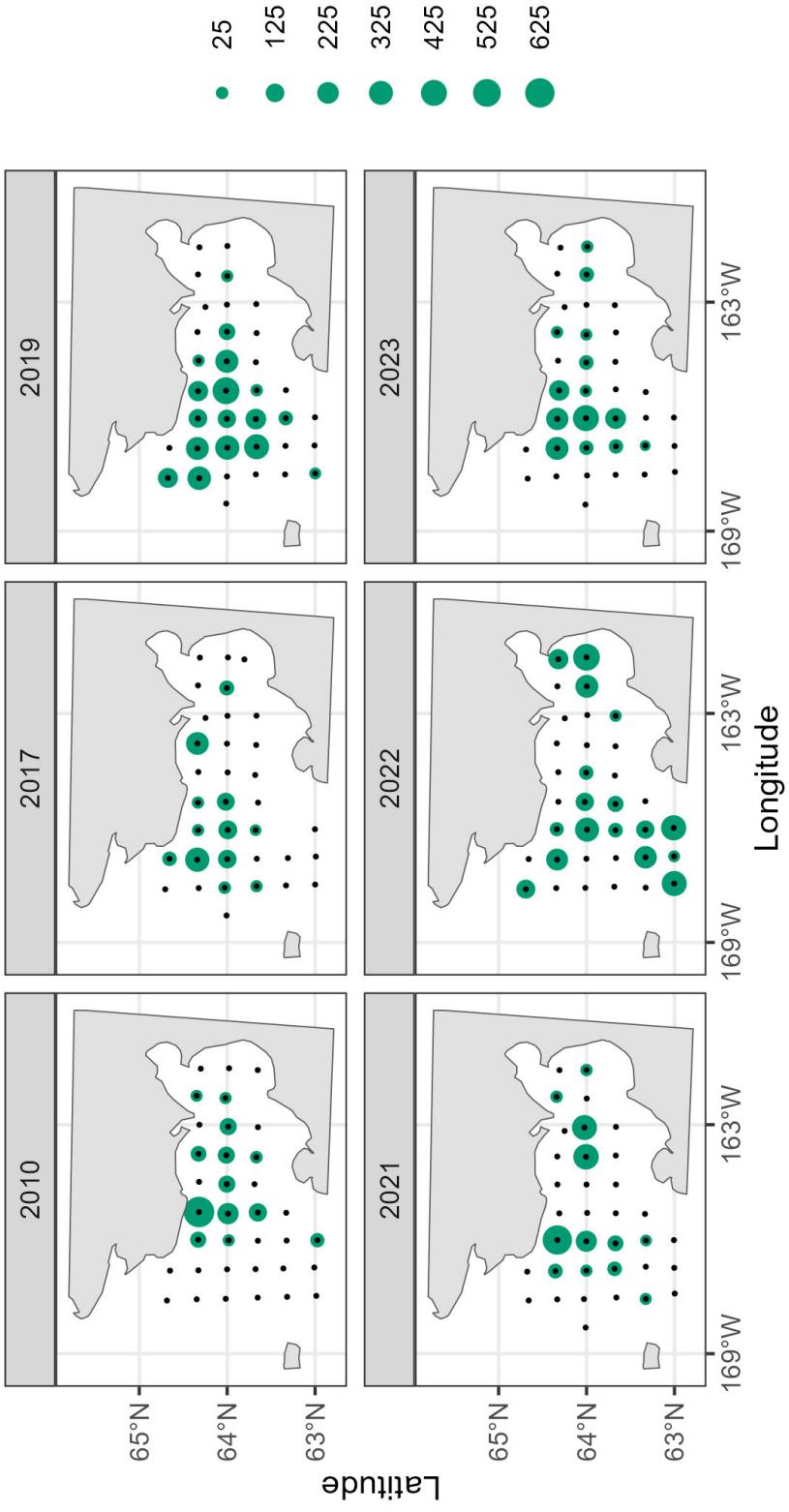
# Survey abundance by station

NOAA Norton Sound trawl survey estimated crab per km<sup>2</sup>



# Survey abundance by station

NOAA Northern Bering Sea trawl survey estimated crab per  $\text{km}^2$



# Design-based abundance estimates

From the 2024 NSRKC SAFE:

*"The fundamental issue regarding NSRKC assessment is a lack of clearly defined spatial boundaries"*

*"Abundance of the 1976-1991 NMFS trawl survey is standardized to 7600 nm<sup>2</sup> ... whereas that of ADF&G survey is unexpanded, with coverage ranging from 4700–5200 nm<sup>2</sup>"*

*"The standardized ADF&G trawl survey area is a fraction of Norton Sound where NSRKC lives and can be subject to fisheries ... using the "Total abundance" would be more appropriate."*

- Matching ADF&G survey design-based abundance estimates may not be desirable
- A consistent definition of the area over which to estimate abundance is needed



# Outline

Stock and surveys

**Modeling approach, evaluation, diagnostics**

Prediction grids and spatial predictions

Indices, comparison to design-based indices

Future work and feedback



# Modeling approach

Fit geostatistical GLMMs with spatiotemporally correlated random effects using **sdmTMB**

Constructed triangulation meshes using `make_mesh()` and `add_barrier_mesh()`

Ensured that the number of mesh vertices was lower than the number of data points



# Model specification

Estimated spatiotemporal random fields as independent and identically distributed (IID)

Predictors: year or year + survey station depth

Model structures:

- Tweedie with a log link
- delta-gamma with a logit link for the binomial distribution and a log link for the gamma distribution
- delta-lognormal with a logit link for the binomial distribution and a log link for the lognormal distribution.



# Model convergence

Evaluated convergence using sdmTMB function `sanity_check()`

ADF&G survey converged models:

- Tweedie with a year effect only
- Tweedie with year and depth effects
- delta-gamma with year and depth effects

NOAA NBS trawl survey converged models:

- Tweedie with a year effect only
- Tweedie with year and depth effects

All six NOAA Norton Sound trawl survey models converged



# Model predictive skill

Model predictive skill: predictive ability of the model for new observations

- cross validation using sdmTMB\_cv()
- 10 randomly arranged folds for each model

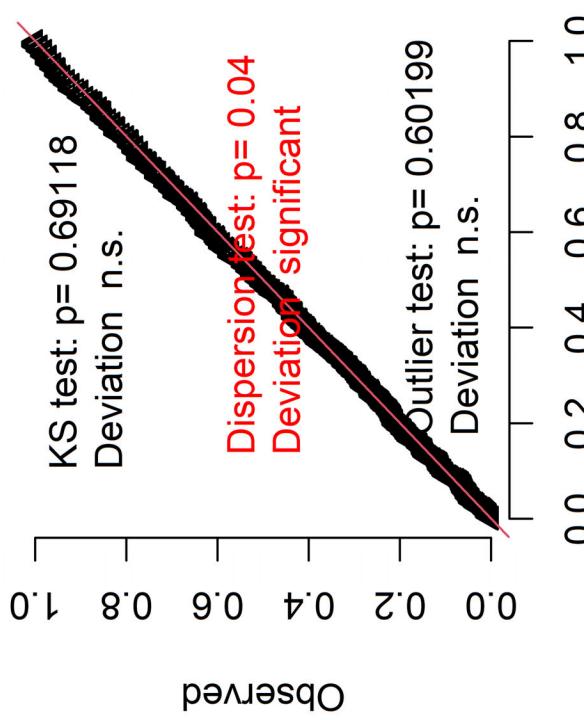
Models with best predictive skill:

- ADF&G survey: delta-gamma model with year and depth
- NOAA NS survey: delta-lognormal model with year and depth
- NOAA NBS survey: Tweedie model with year only



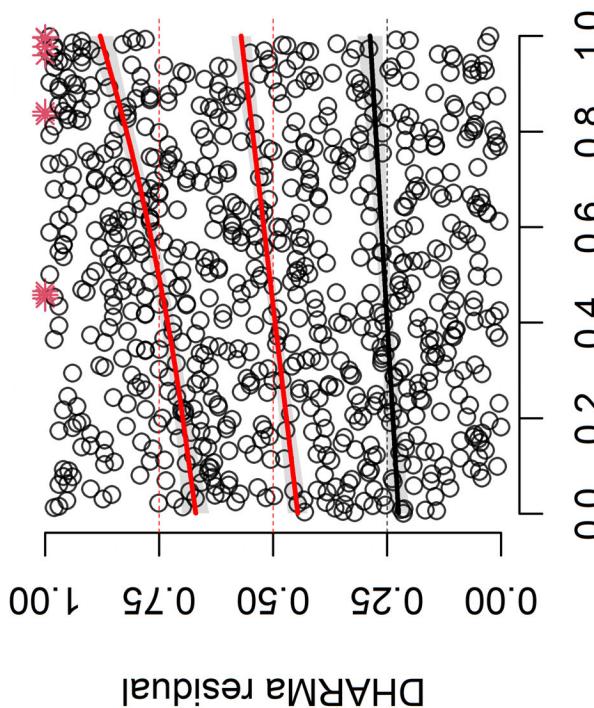
# Model diagnostics: ADF&G survey

QQ plot residuals



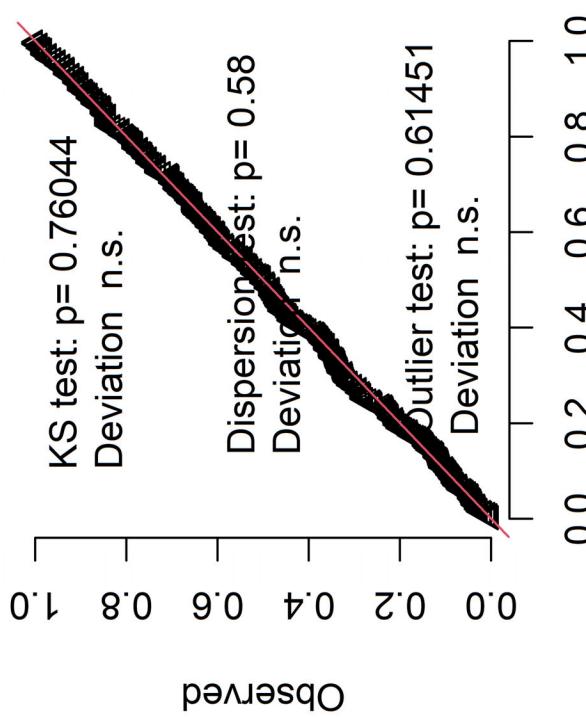
DHARMA residual vs. predicted

Quantile deviations detected (red curves)  
Combined adjusted quantile test significant

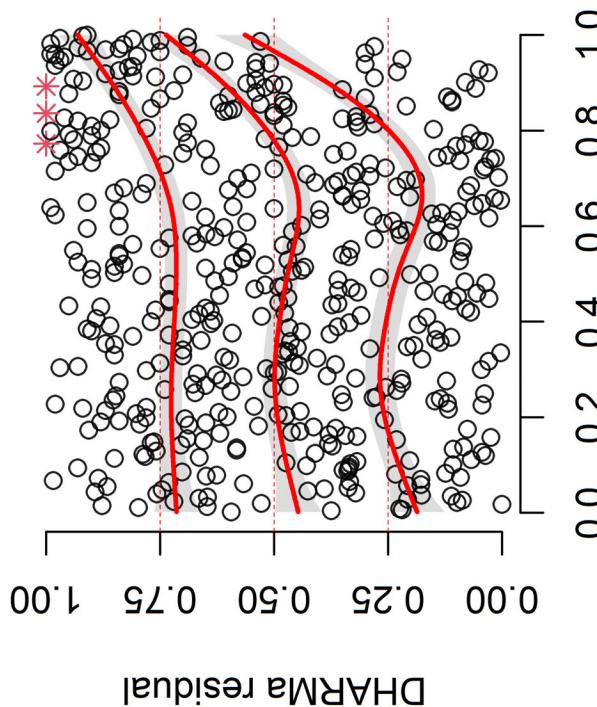


# Model diagnostics: NOAA NS survey

QQ plot residuals



DHARMA residual vs. predicted  
Quantile deviations detected (red curves)  
Combined adjusted quantile test significant



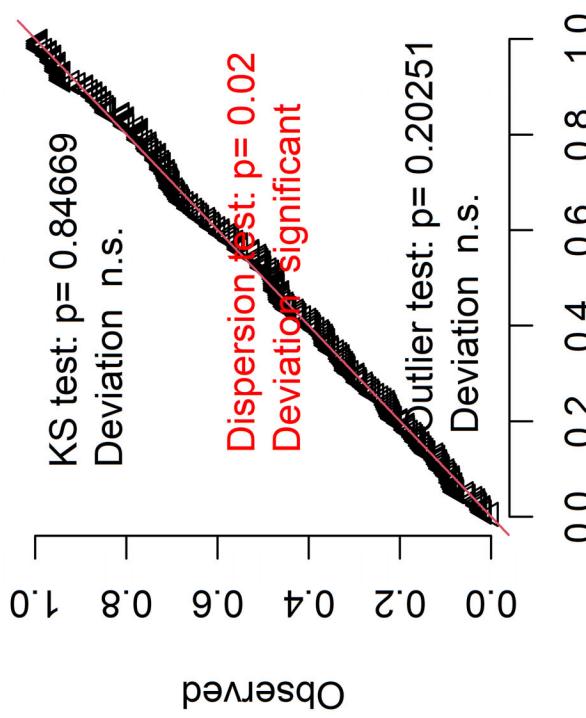
Expected

Model predictions (rank transformed)

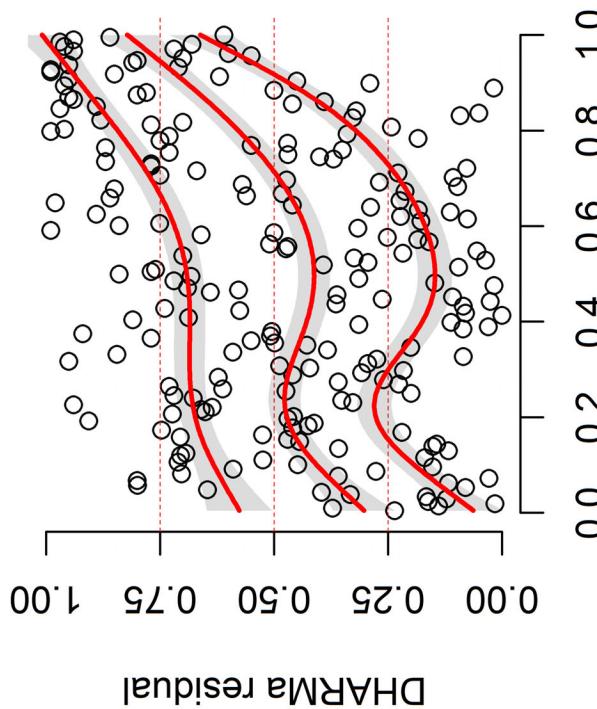


# Model diagnostics: NOAA NBS survey

QQ plot residuals



DHARMA residual vs. predicted  
Quantile deviations detected (red curves)  
Combined adjusted quantile test significant



Expected

Model predictions (rank transformed)



# Model diagnostics summary

Survey	Model	Effects	Log-likelihood	Kolmogorov-Smirnov	Quantiles	Dispersion	Outliers	Zero inflation
ADF&G	Tweedie	year	-3,069	0.415	<0.01	0.02	0.38	0.88
ADF&G	Tweedie	year, depth	-3,026	0.473	<0.01	0.62	0.30	0.76
ADF&G	DG	year, depth	-2,985	0.691	<0.01	0.04	0.60	0.96
NOAA NS	Tweedie	year	-1,791	0.574	<0.01	<0.01	0.61	0.84
NOAA NS	DG	year	-1,703	0.537	<0.01	0.94	0.87	0.52
NOAA NS	DL	year	-1,648	0.717	<0.01	0.22	0.31	0.44
NOAA NS	Tweedie	year, depth	-1,732	0.312	<0.01	<0.01	0.61	0.92
NOAA NS	DG	year, depth	-1,706	0.062	<0.01	0.82	0.24	0.18
NOAA NS	DL	year, depth	-1,642	0.760	<0.01	0.58	0.61	0.72
NOAA NBS	Tweedie	year	-662	0.847	<0.01	0.02	0.20	0.42
NOAA NBS	Tweedie	year, depth	-1,124	0.613	<0.01	<0.01	0.80	0.82



# Moran's I clustering analysis

Tests for spatial patterns in residuals

Applied across each year of the time series for each survey

- Monte Carlo sims of Moran's I; null hypothesis that the residual values were randomly distributed in space
- Moran's I statistic for each year is an overall score of clustering for the spatial residuals across the spatial domain
- positive Moran's I statistic values indicate spatial autocorrelation;  
negative values indicate negative spatial autocorrelation
- p-values < 0.05 indicate significant clustering of spatial residuals



# Moran's I analysis: ADF&G survey

Survey	Model	Year	Moran's I statistic	p-value
ADF&G	DG, year + depth	1996	-0.01	0.38
ADF&G	DG, year + depth	1999	0.02	0.23
ADF&G	DG, year + depth	2002	-0.02	0.49
ADF&G	DG, year + depth	2006	0.06	0.09
ADF&G	DG, year + depth	2008	0.00	0.32
ADF&G	DG, year + depth	2011	-0.05	0.74
ADF&G	DG, year + depth	2014	-0.01	0.36
ADF&G	DG, year + depth	2017	0.02	0.18
ADF&G	DG, year + depth	2018	0.06	0.09
ADF&G	DG, year + depth	2019	0.10	0.02
ADF&G	DG, year + depth	2020	-0.03	0.60
ADF&G	DG, year + depth	2021	0.02	0.19
ADF&G	DG, year + depth	2023	-0.05	0.72
ADF&G	DG, year + depth	2024	0.03	0.17



# Moran's I analysis: NOAA NS survey

Survey	Model	Year	Moran's I statistic	p-value
NOAA NS	DL, year + depth	1976	0.125	0.002
NOAA NS	DL, year + depth	1979	0.051	0.088
NOAA NS	DL, year + depth	1982	-0.014	0.425
NOAA NS	DL, year + depth	1985	0.134	0.006
NOAA NS	DL, year + depth	1988	0.039	0.124
NOAA NS	DL, year + depth	1991	-0.022	0.476

Two years with significant spatial autocorrelation



# Moran's I analysis: NOAA NBS survey

Survey	Model	Year	Moran's I statistic	p-value
NOAA NBS	Tweedie, year	2010	0.05	0.09
NOAA NBS	Tweedie, year	2017	0.02	0.16
NOAA NBS	Tweedie, year	2019	0.05	0.09
NOAA NBS	Tweedie, year	2021	-0.02	0.38
NOAA NBS	Tweedie, year	2022	-0.04	0.55
NOAA NBS	Tweedie, year	2023	0.06	0.08

No years with significant clustering of spatial residuals

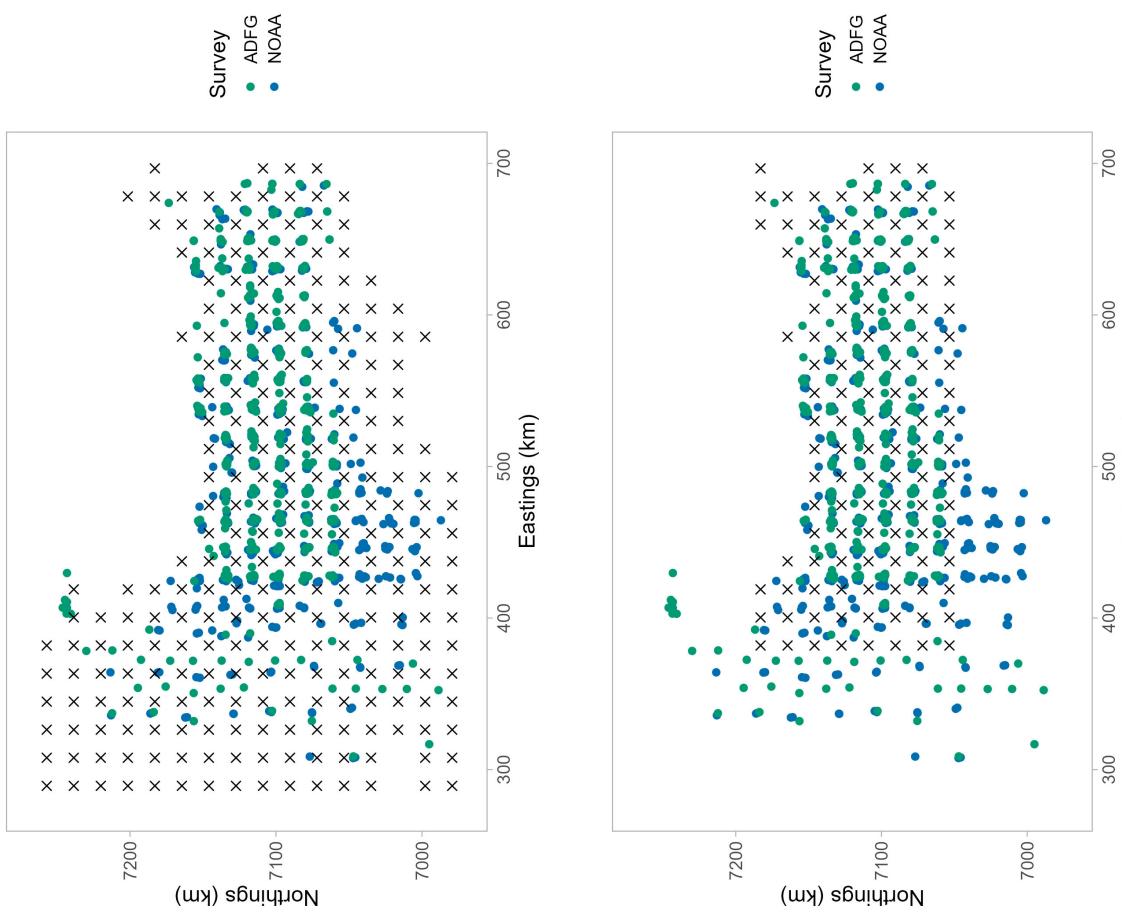


# Outline

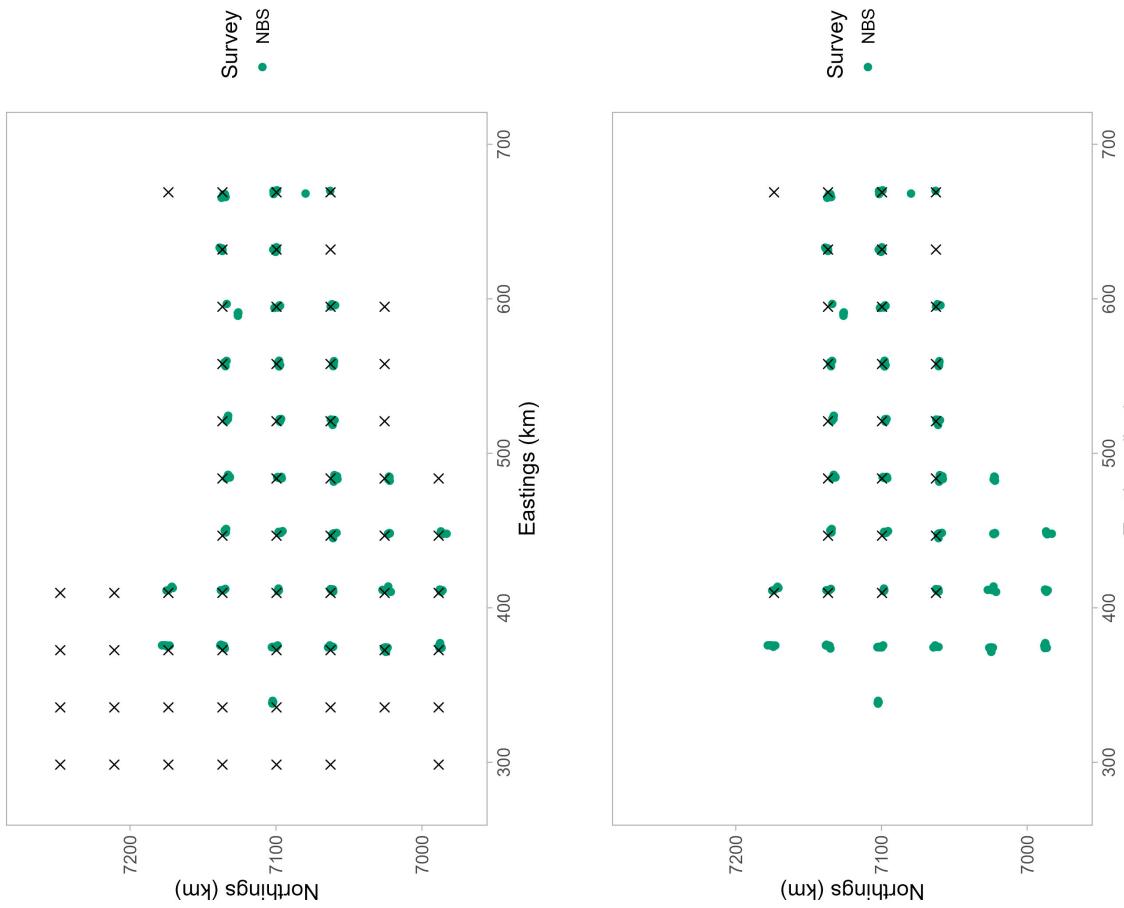
- Stock and surveys
- Modeling approach, evaluation, diagnostics
- Prediction grids and spatial predictions**
- Indices, comparison to design-based indices
- Future work and feedback



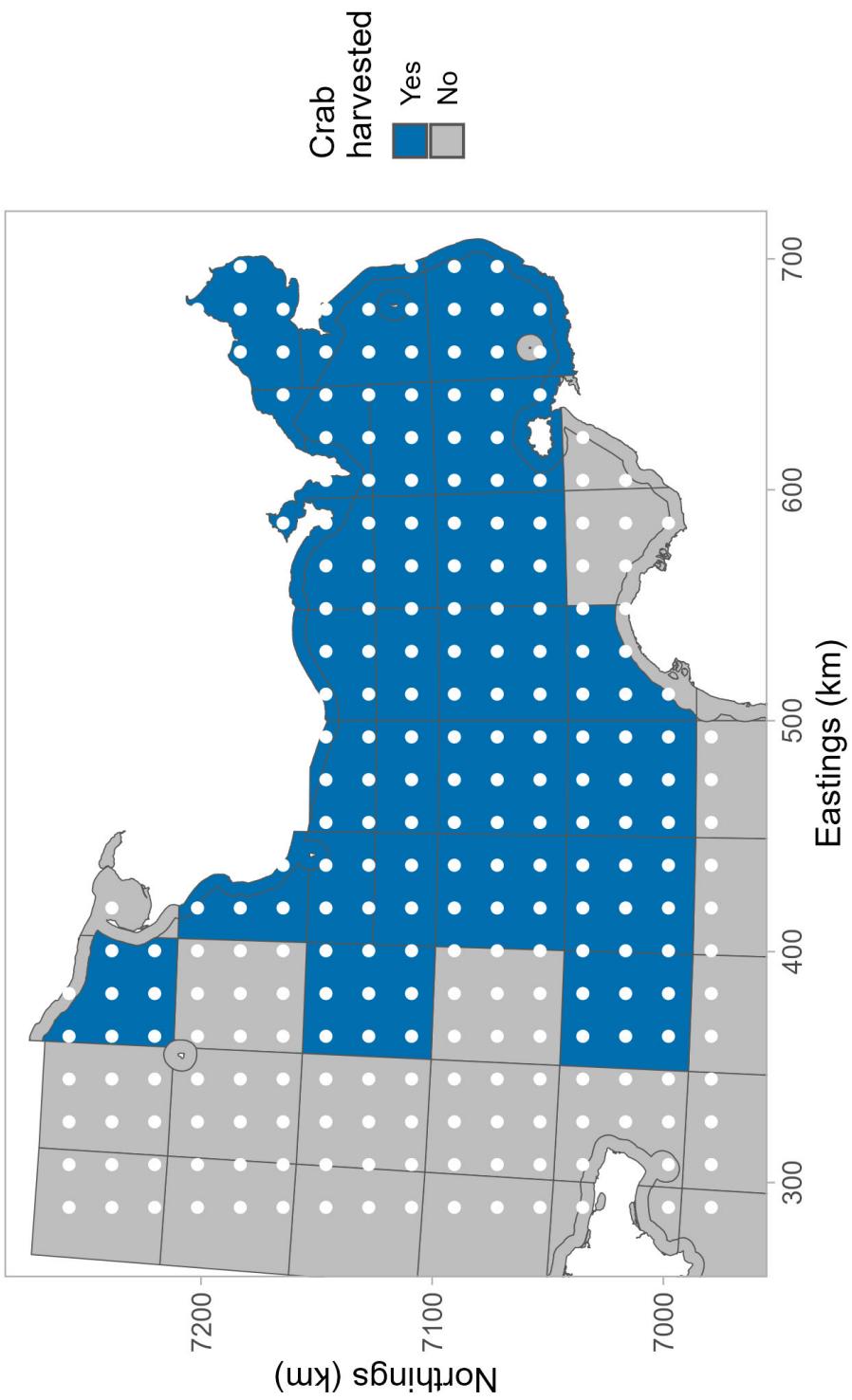
# Prediction grids



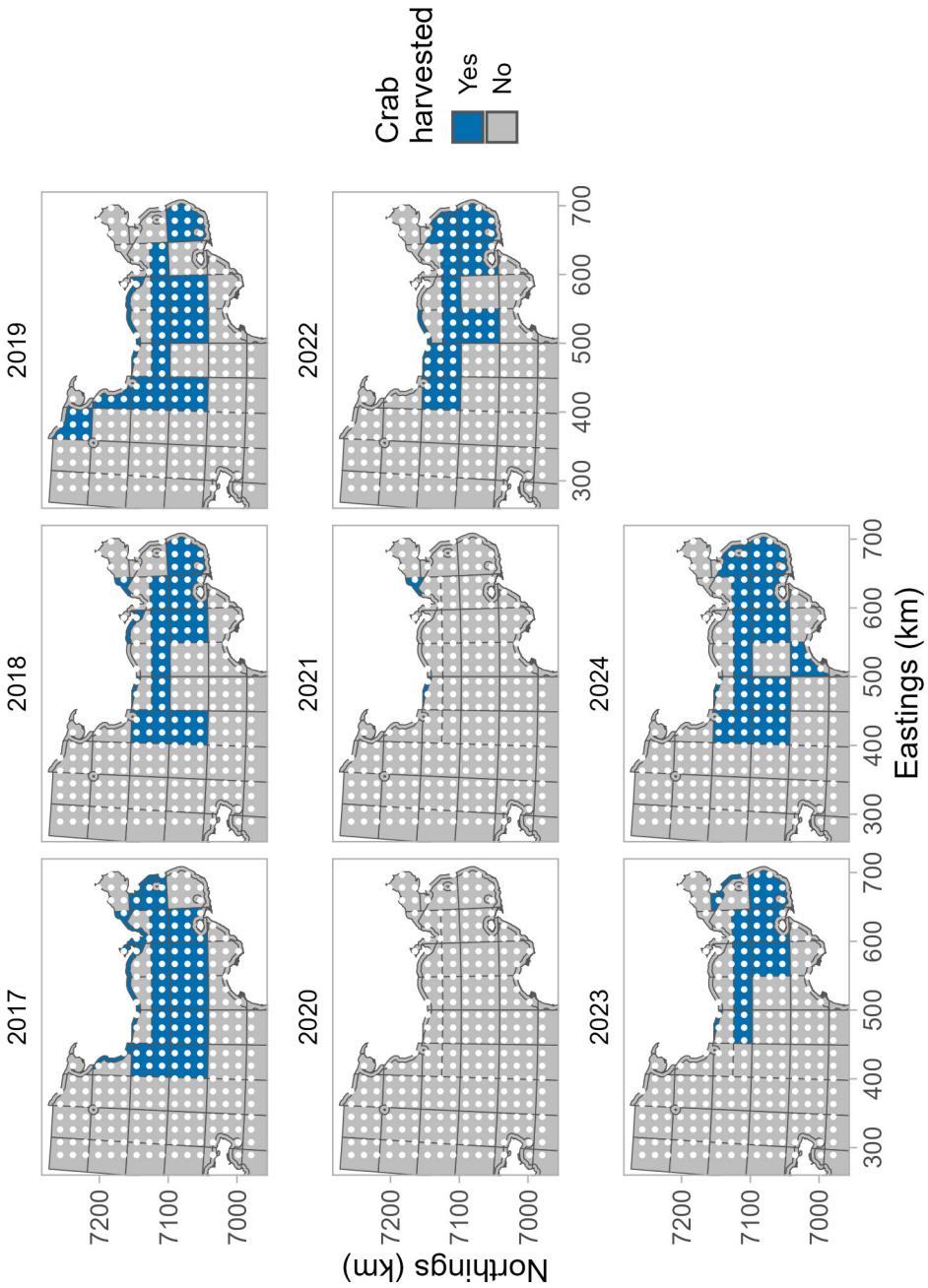
# Prediction grids



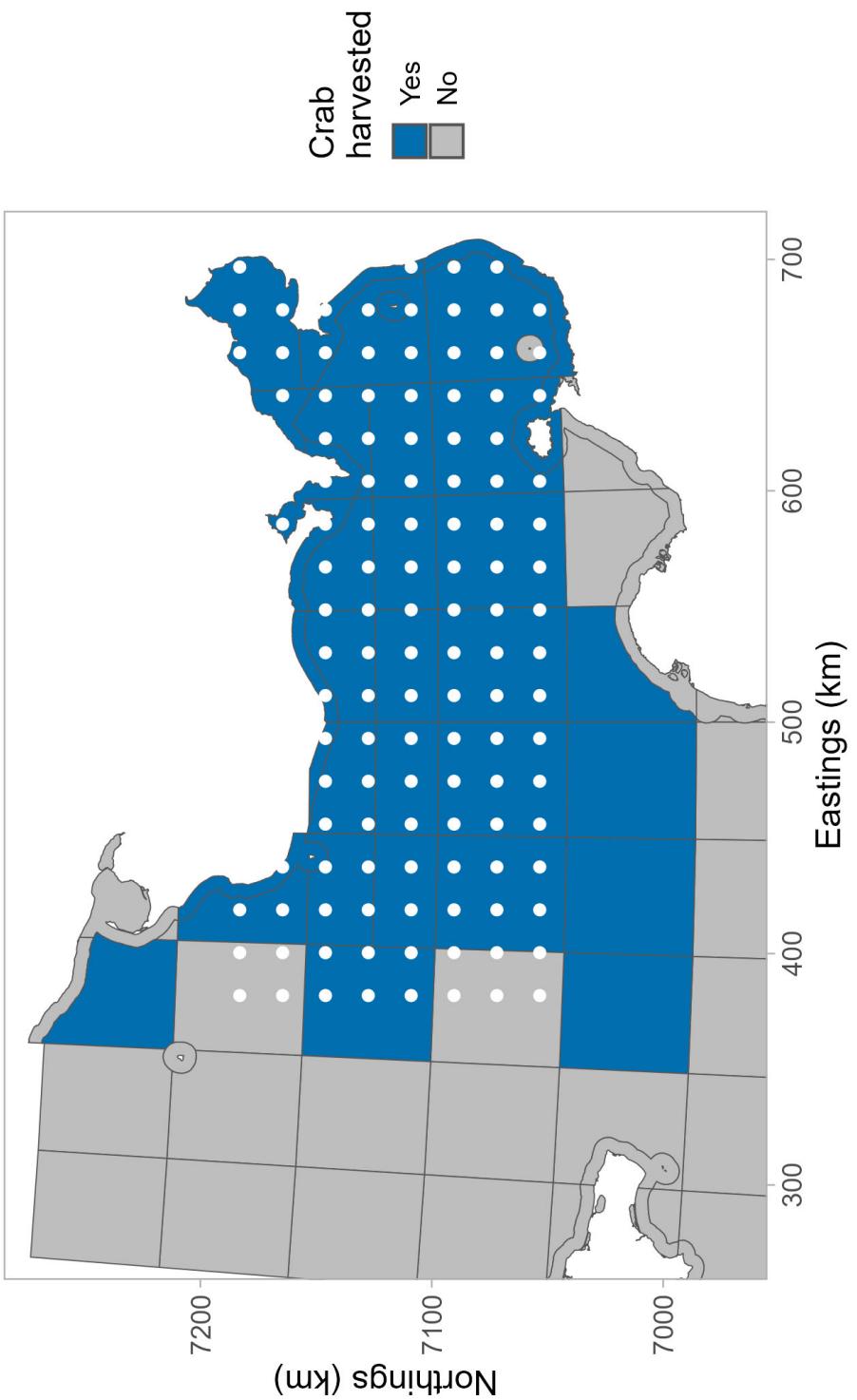
# Harvest information



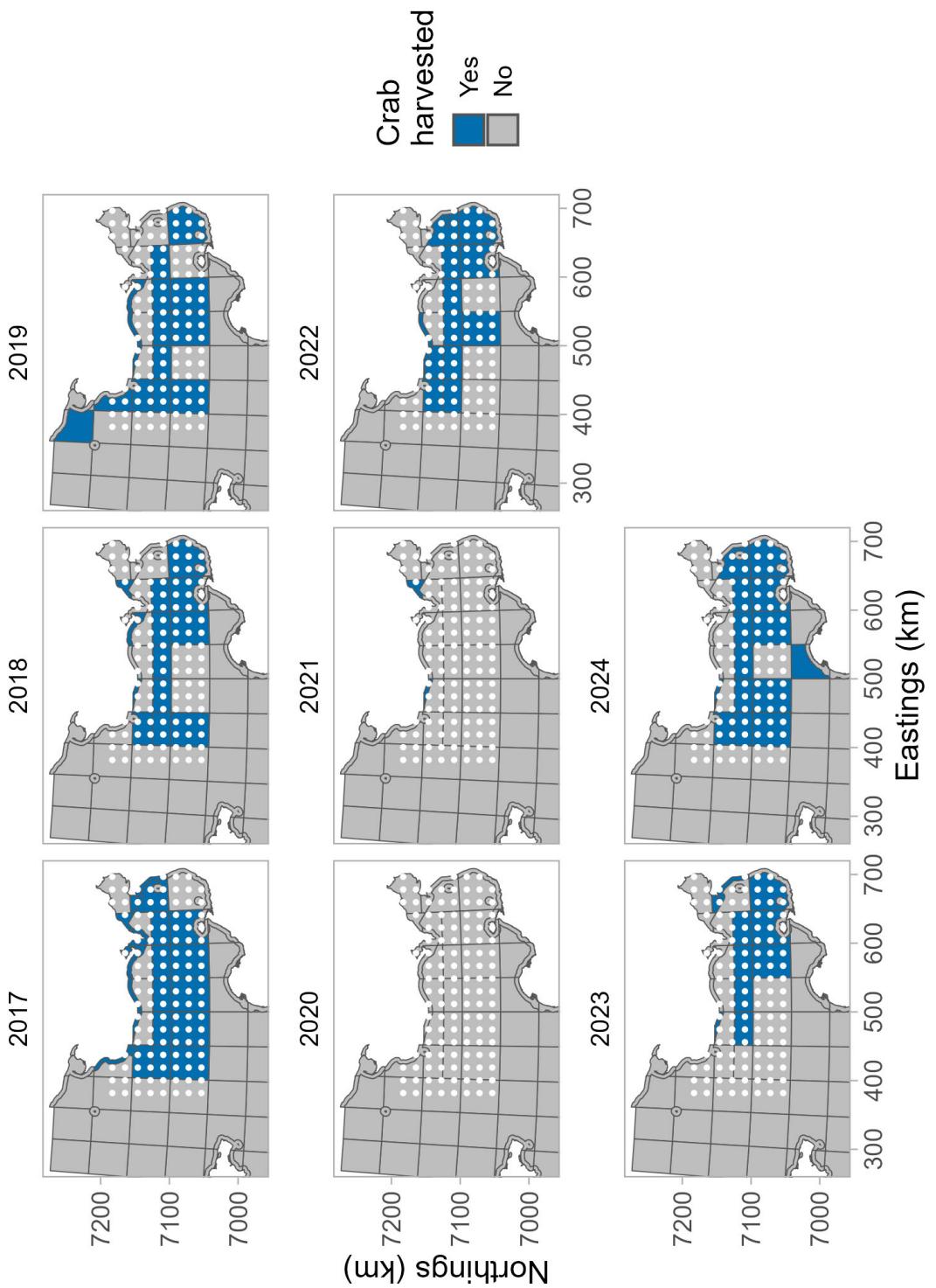
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# Harvest information

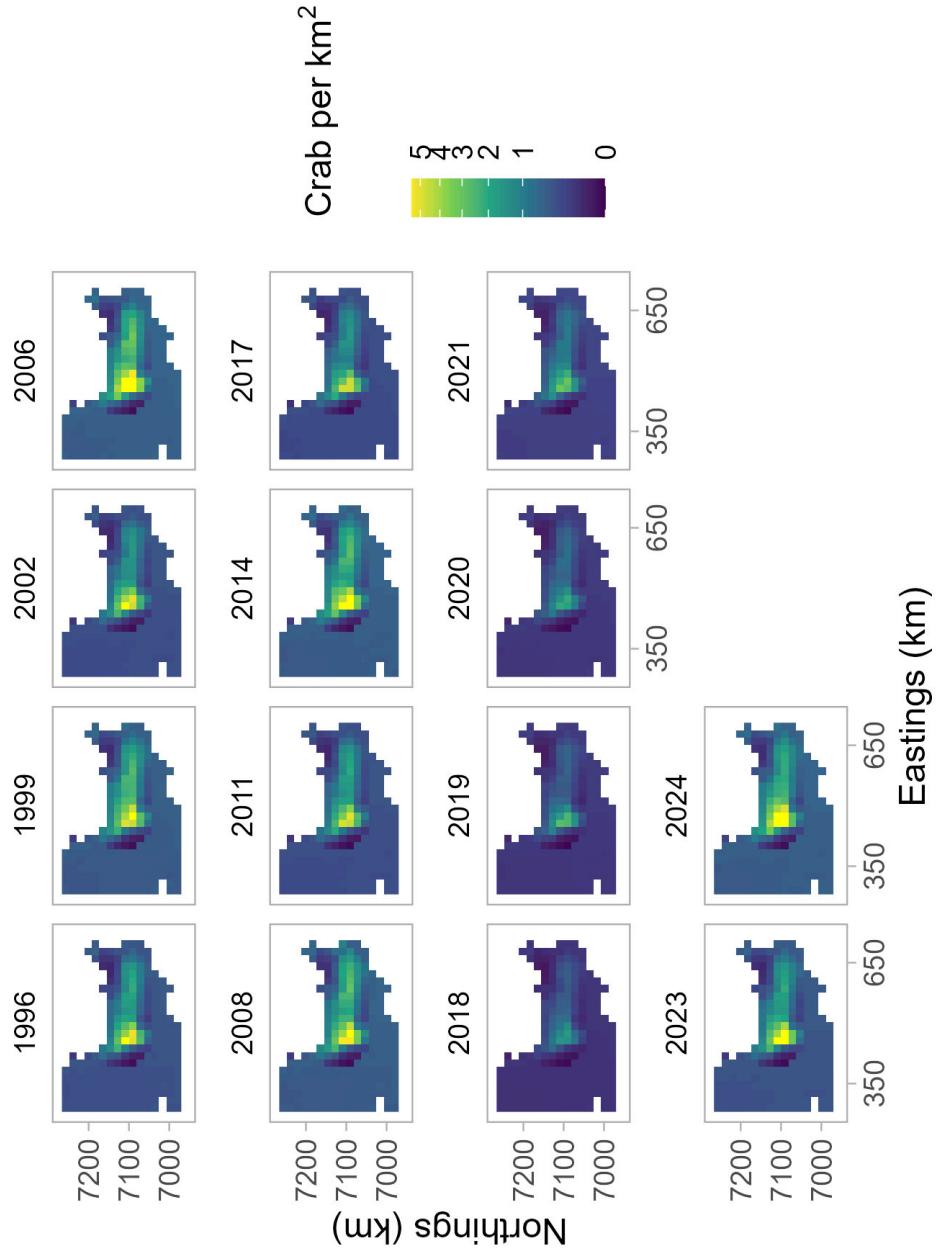


## Harvest information



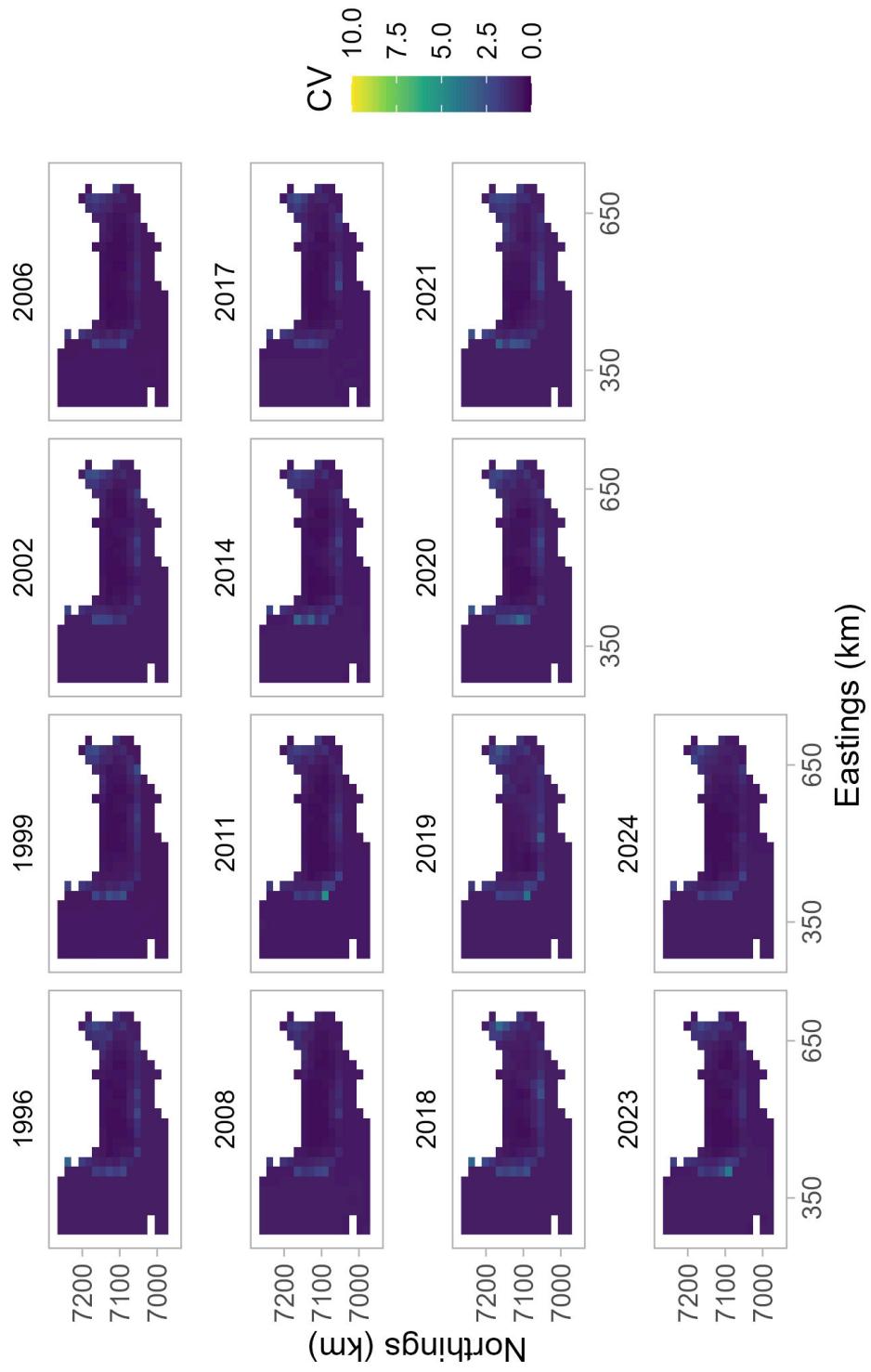
# Predicted abundance

Predicted male abundance from ADF&G trawl survey  
DG, year + depth, full prediction grid



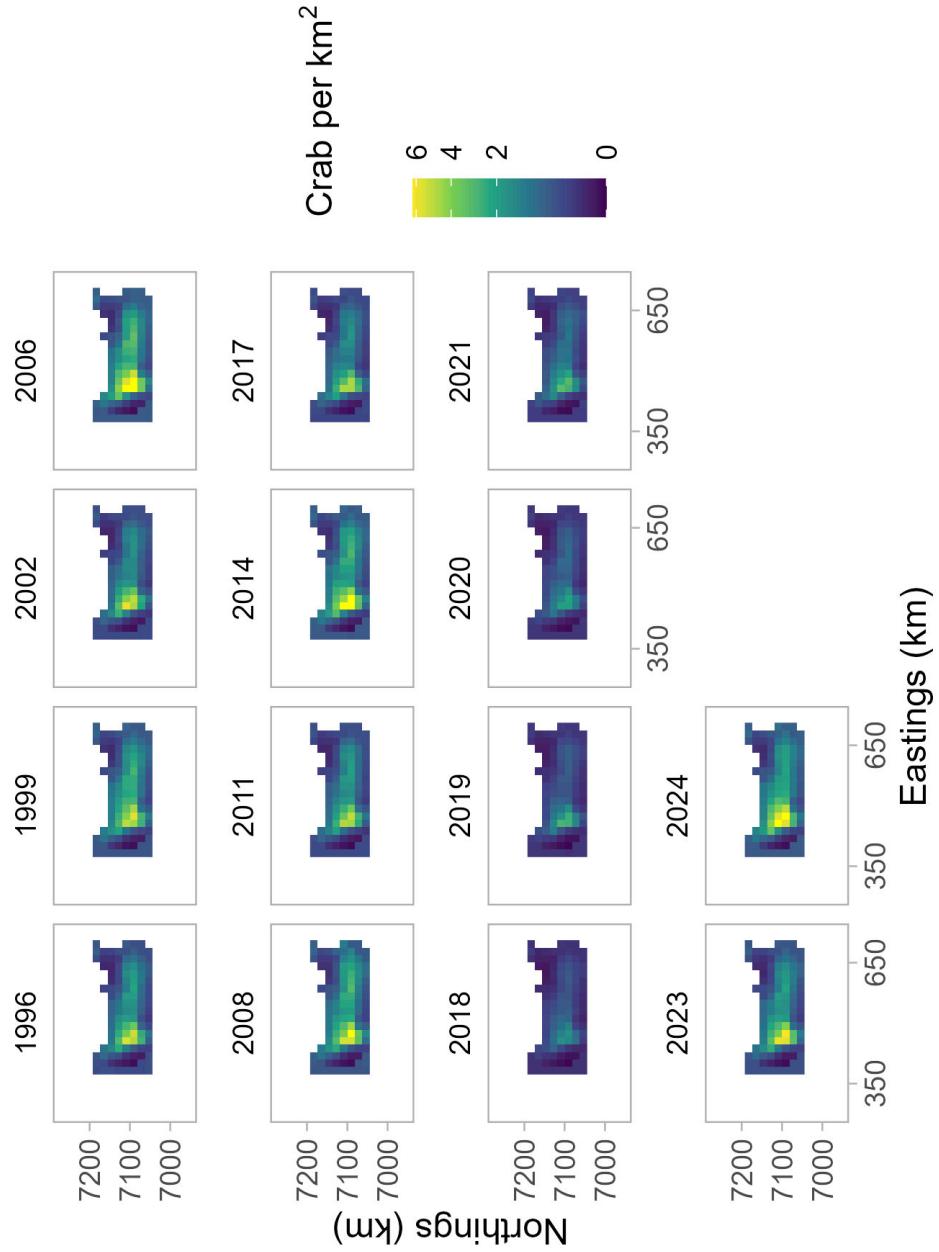
# Predicted abundance CV's

Coefficient of variation for predicted male abundance  
ADF&G trawl survey, DG, year + depth, full prediction area



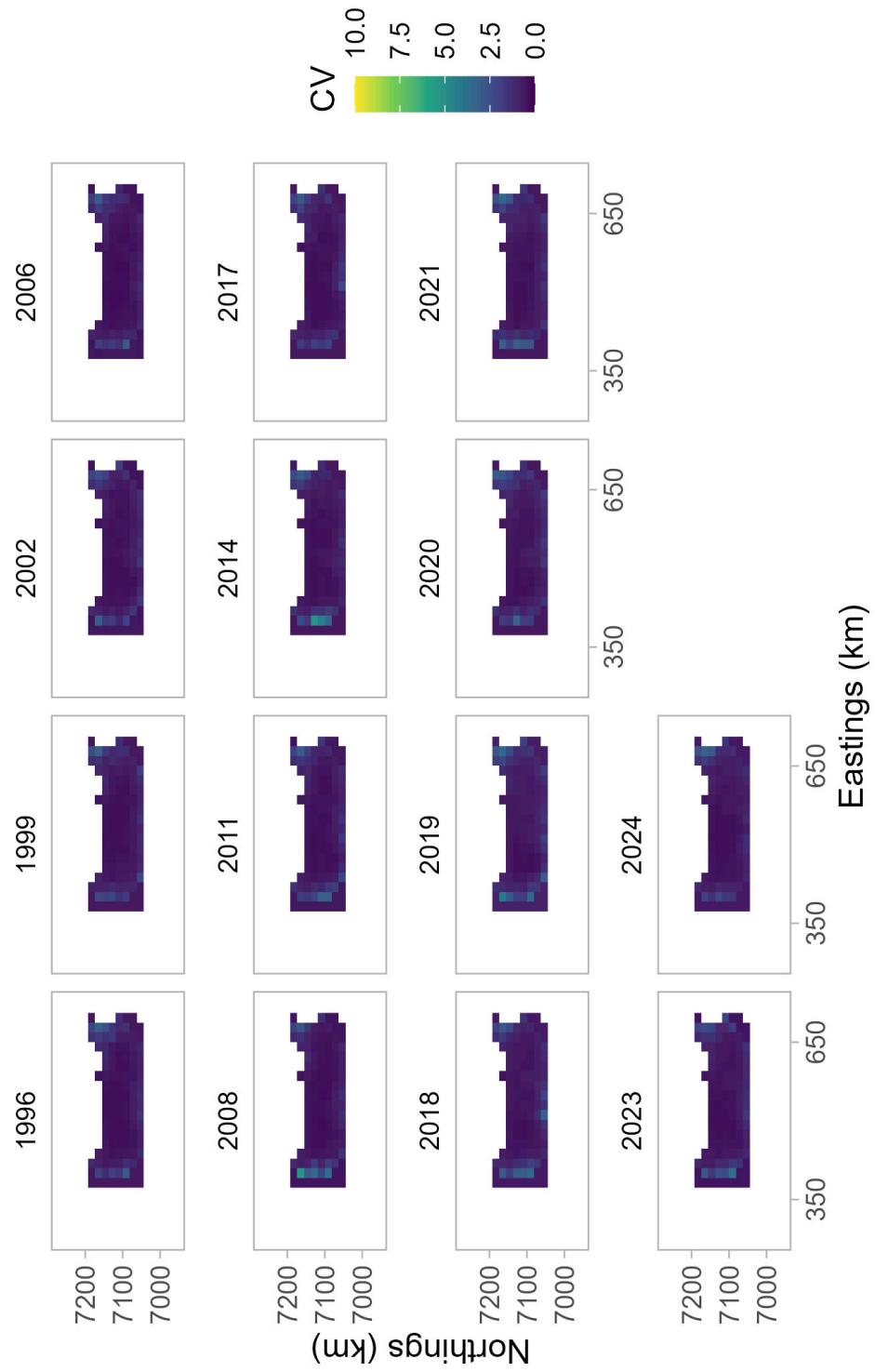
# Predicted abundance

Predicted male abundance from ADF&G trawl survey  
DG, year + depth, reduced prediction grid

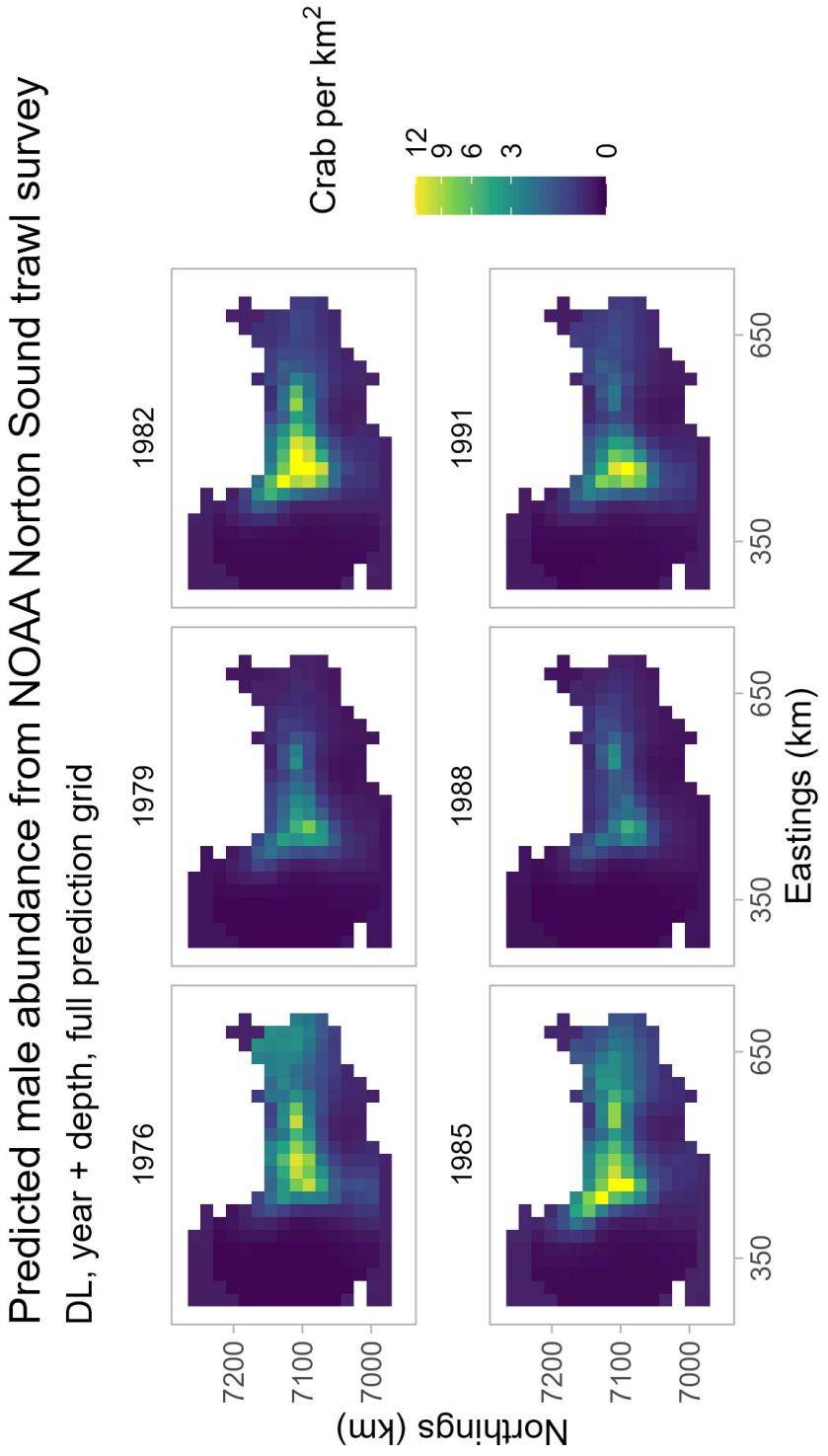


# Predicted abundance CV's

Coefficient of variation for predicted male abundance  
ADF&G trawl survey, DG, year + depth, reduced prediction area



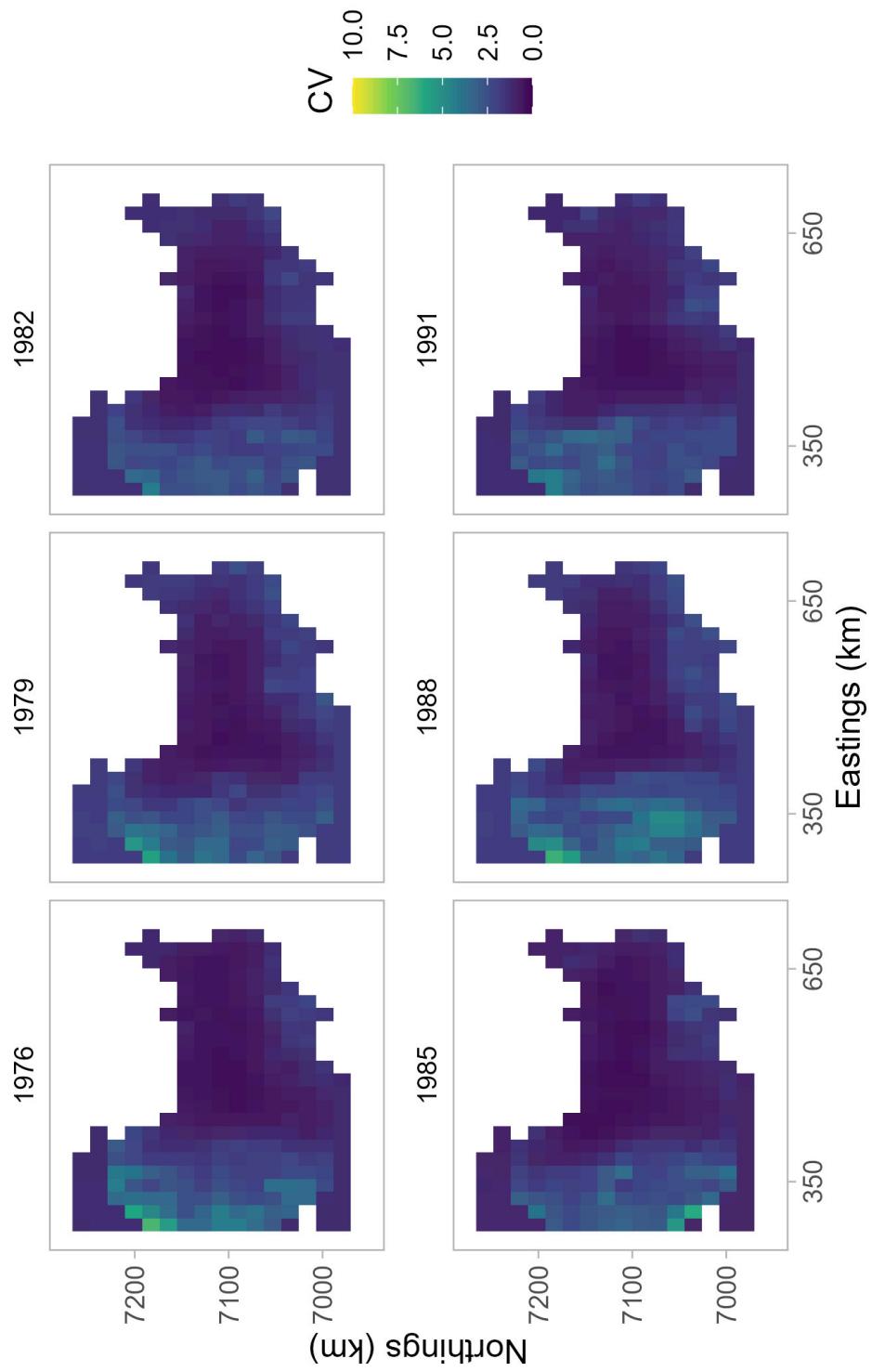
# Predicted abundance



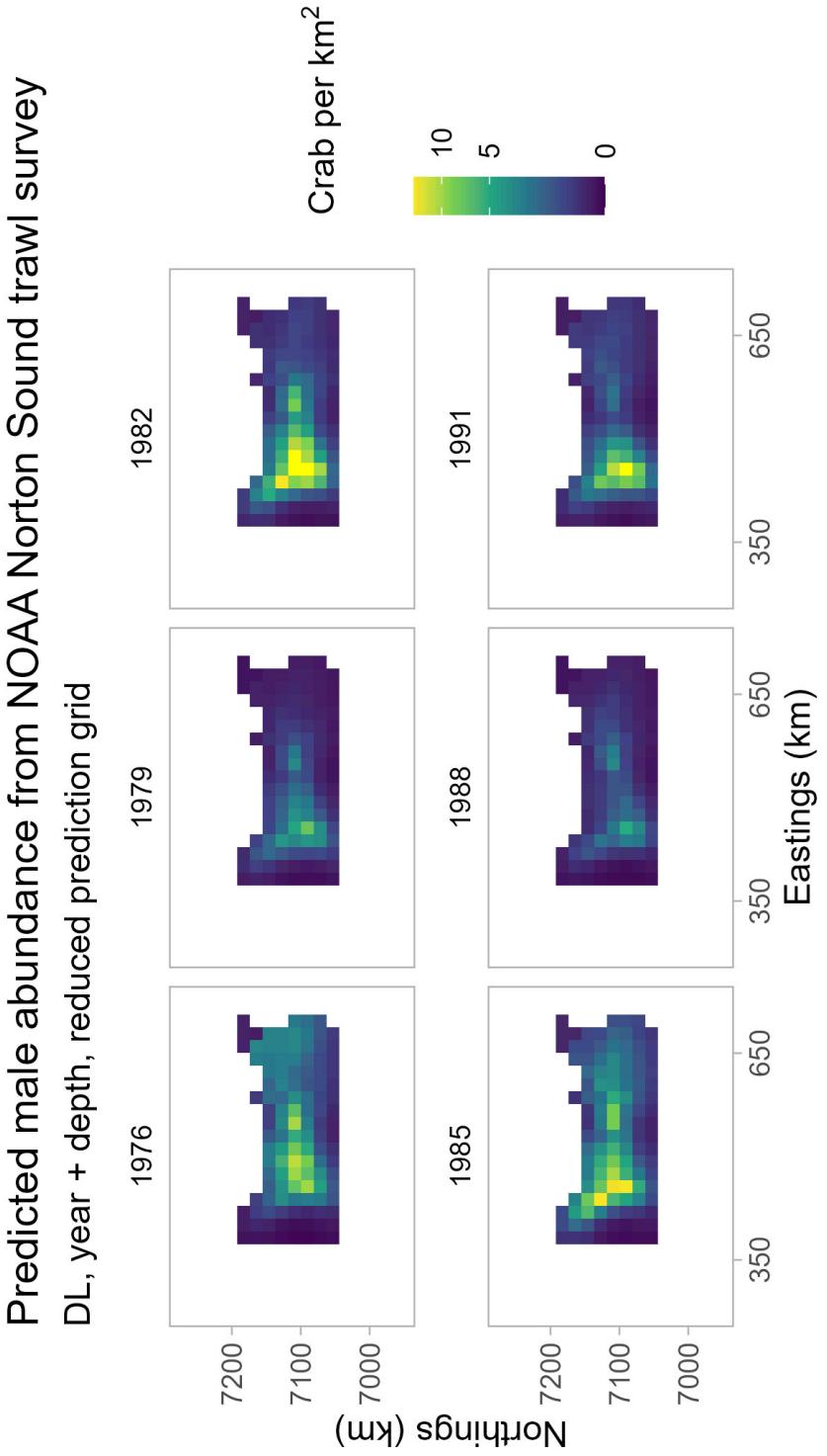
# Predicted abundance CV's

Coefficient of variation for predicted male abundance

NOAA Norton Sound trawl survey, DL, year + depth, full prediction area



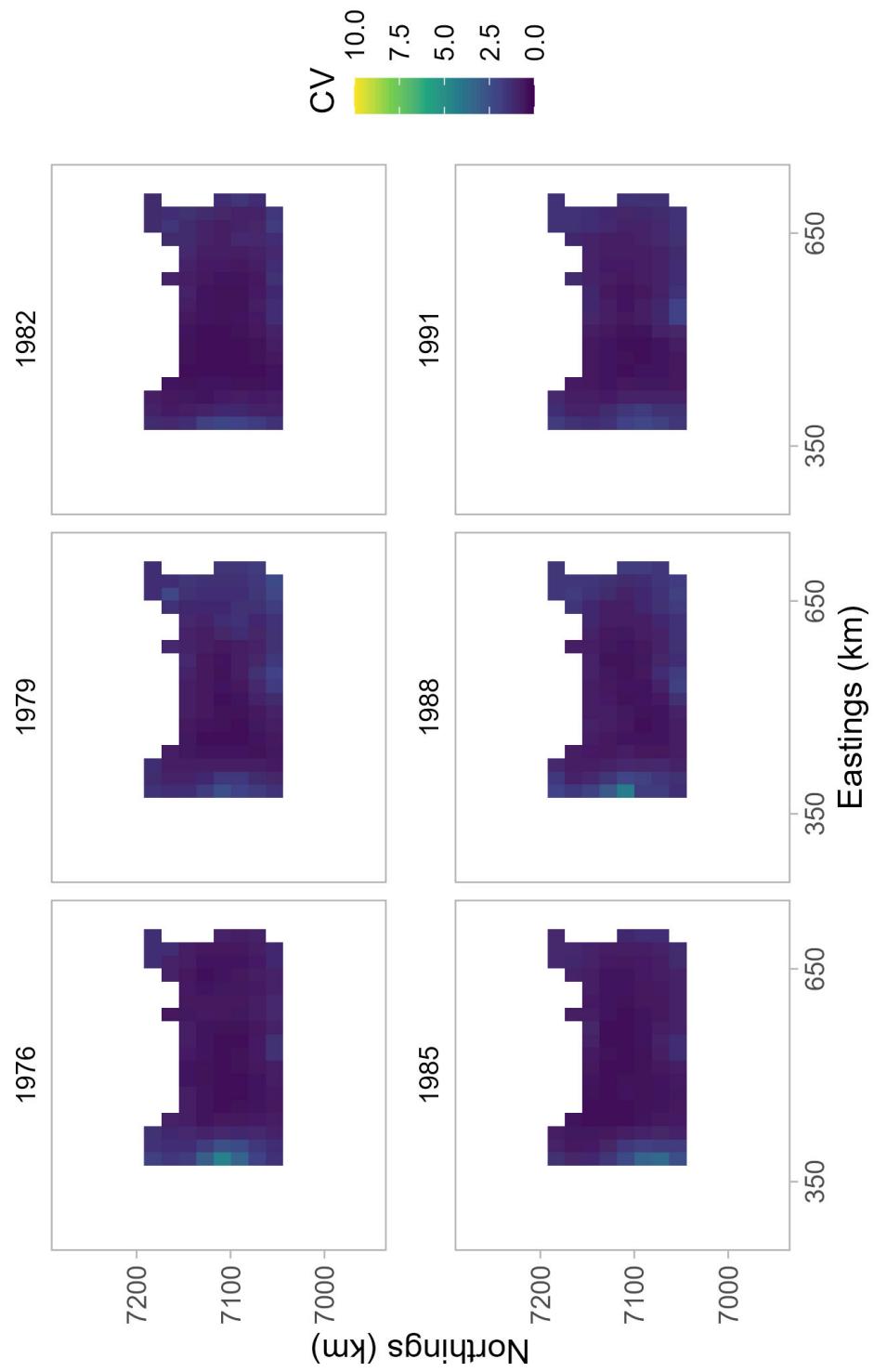
# Predicted abundance



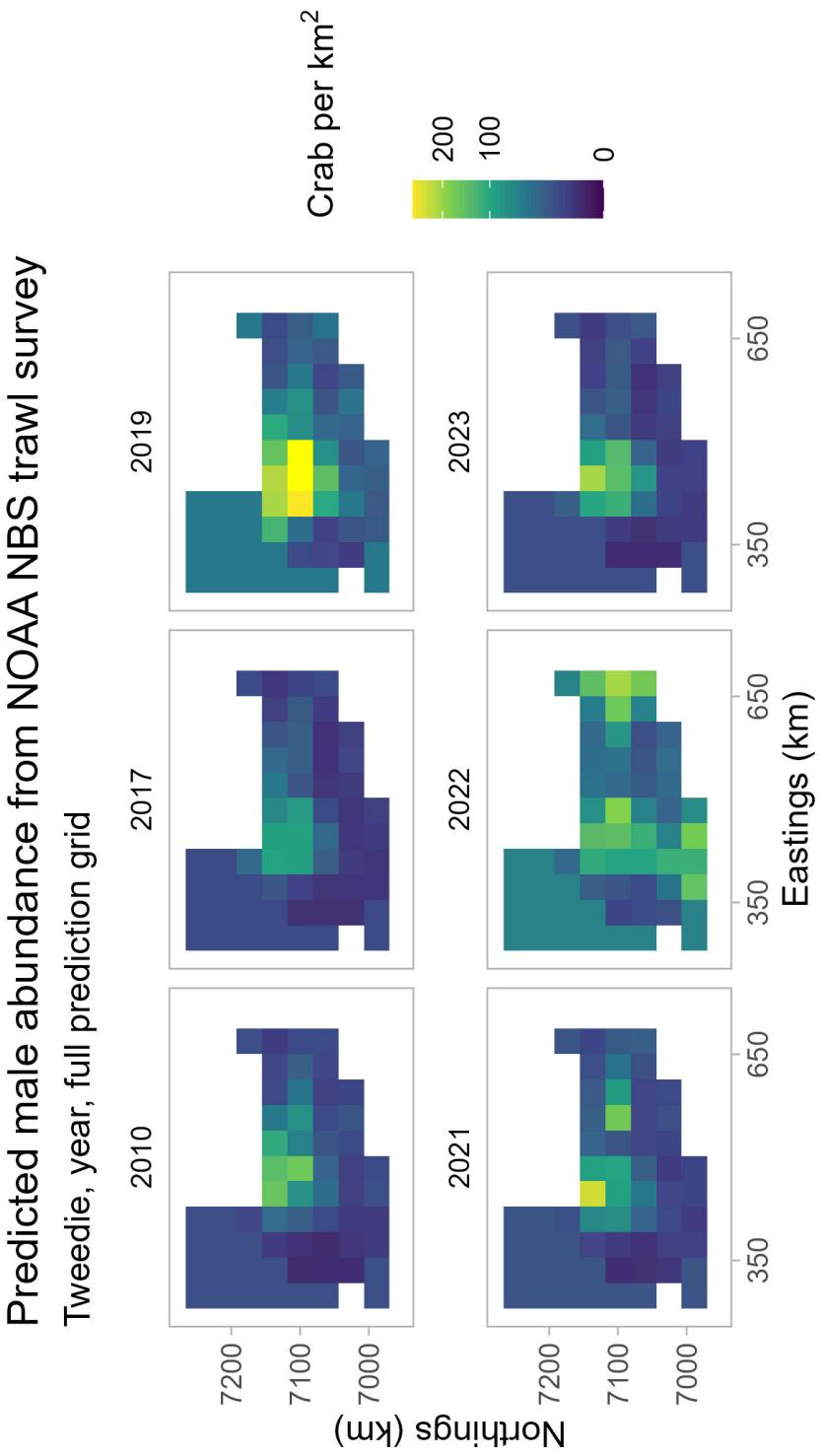
# Predicted abundance CV's

Coefficient of variation for predicted male abundance

NOAA Norton Sound trawl survey, DL, year + depth, reduced prediction area

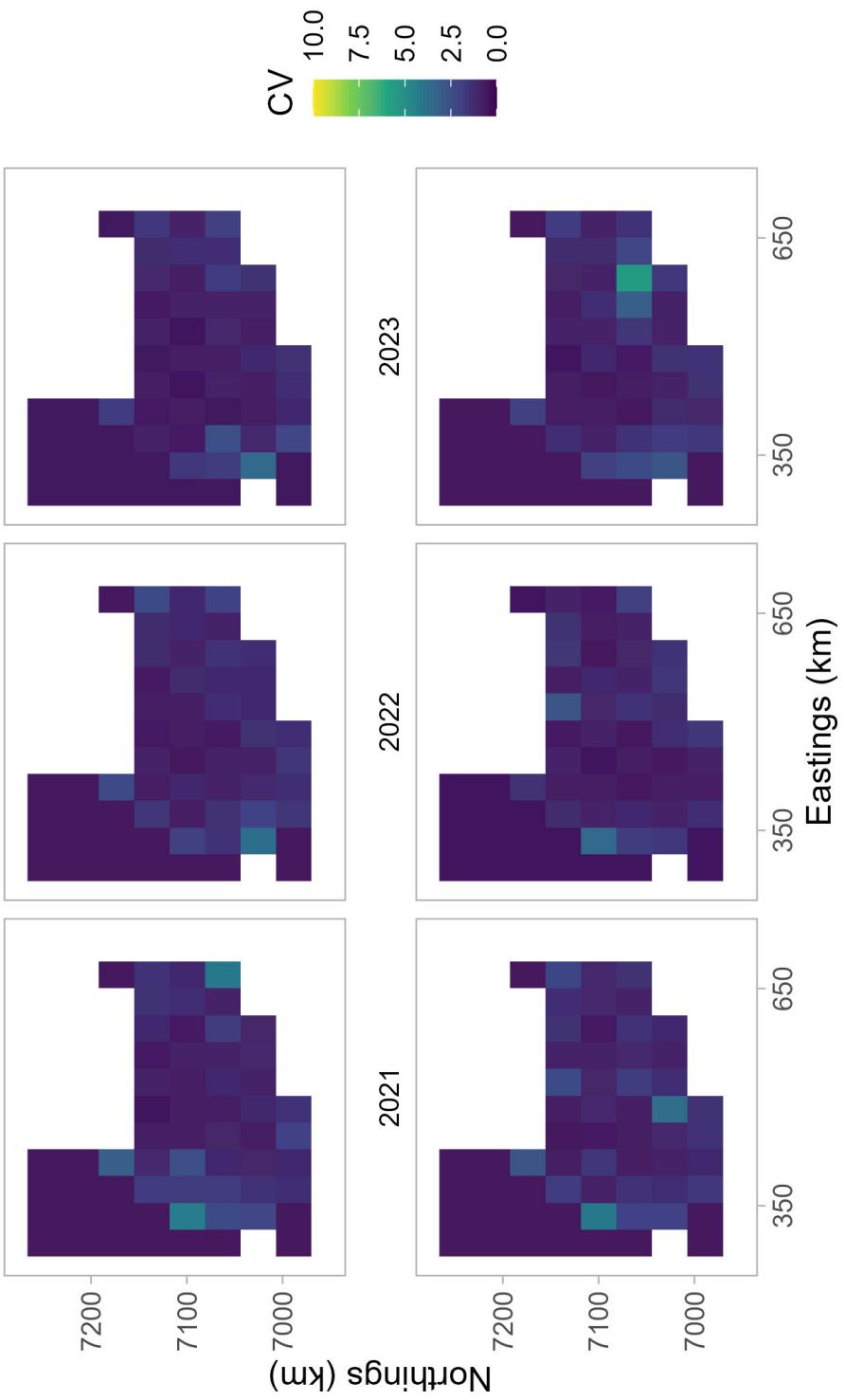


# Predicted abundance

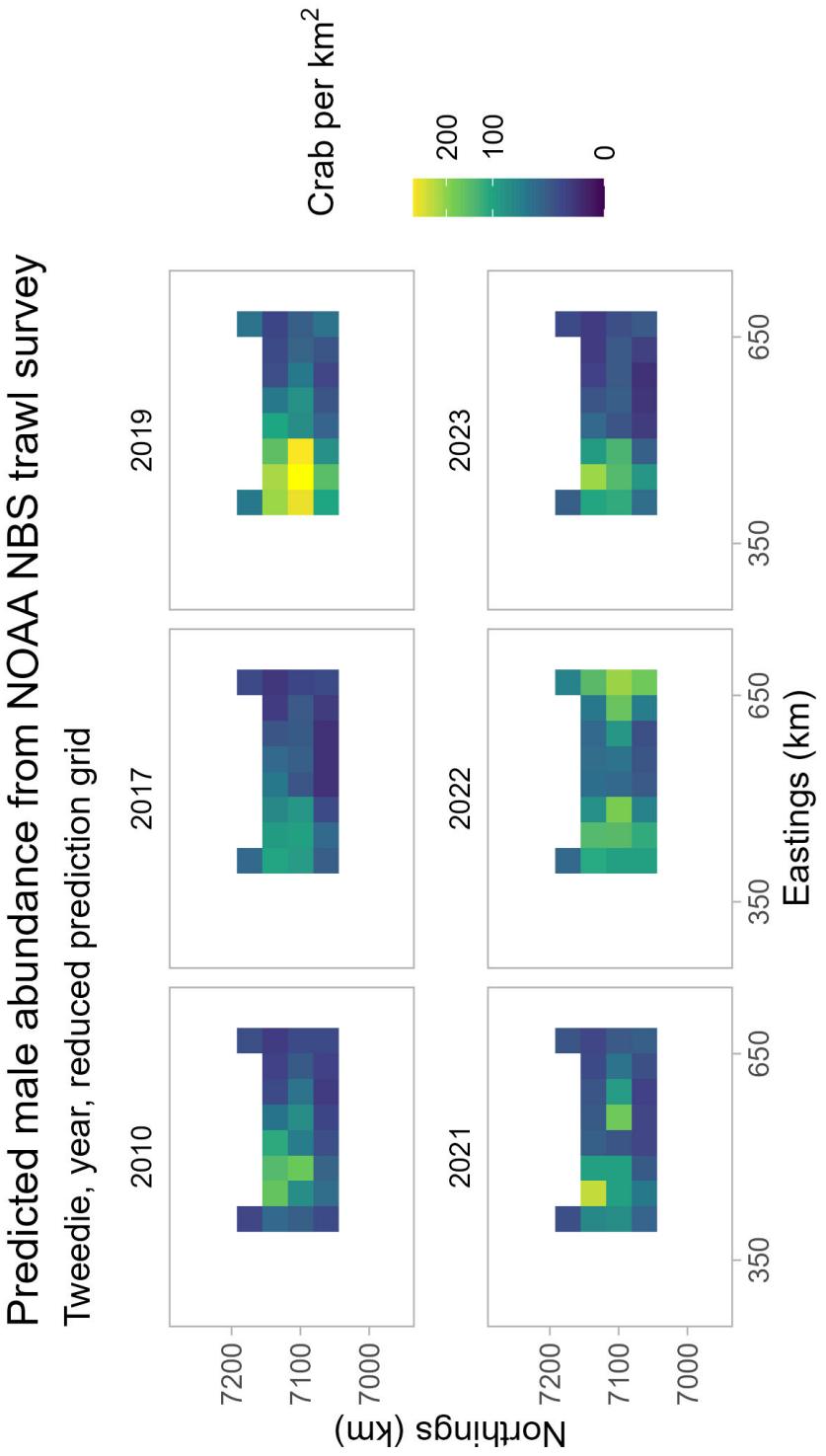


# Predicted abundance CV's

Coefficient of variation for predicted male abundance  
NOAA NBS trawl survey, Tweedie, year, full prediction area

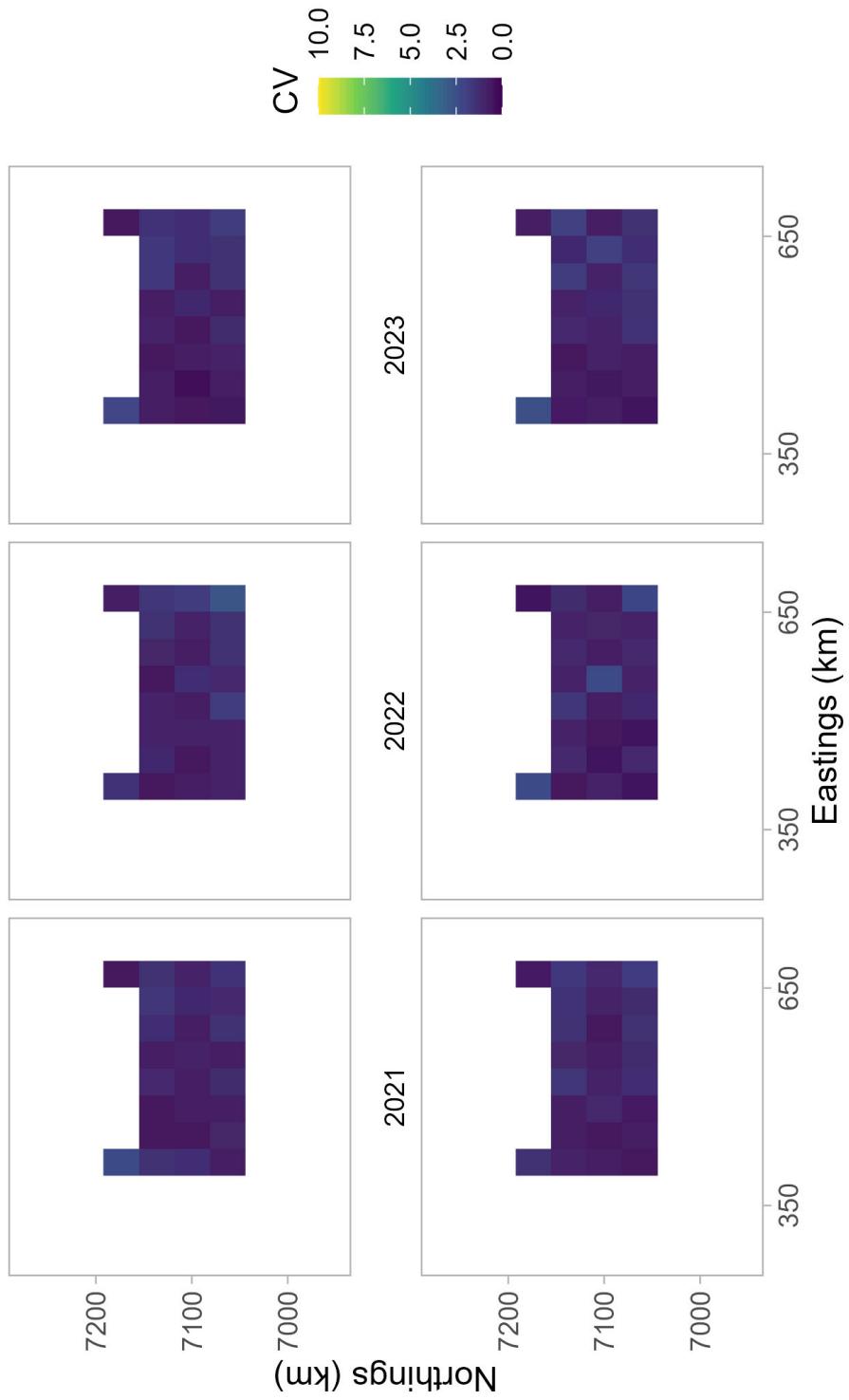


# Predicted abundance



# Predicted abundance CV's

Coefficient of variation for predicted male abundance  
NOAA NBS trawl survey, Tweedie, year, reduced prediction area



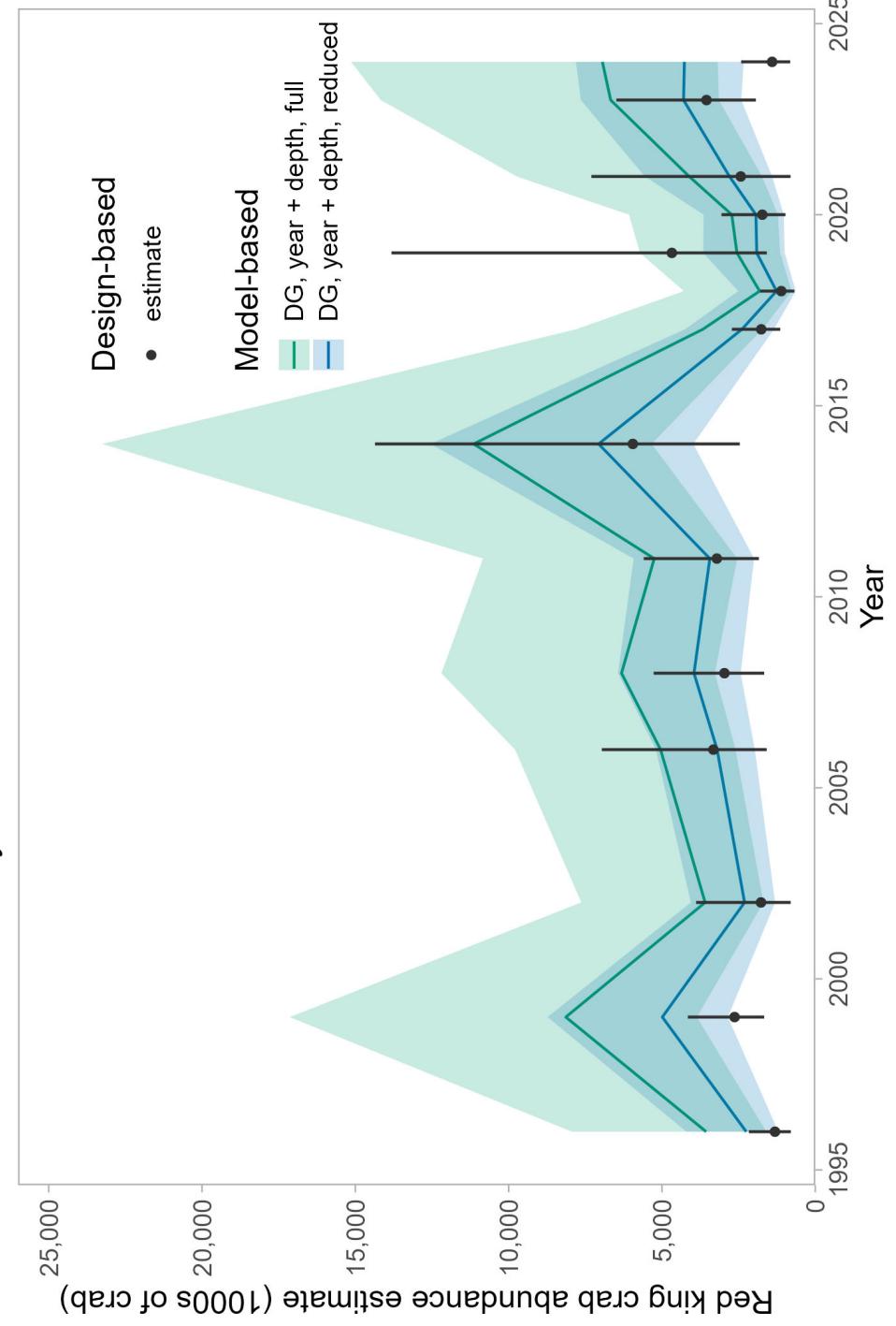
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- Stock and surveys
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- Future work and feedback



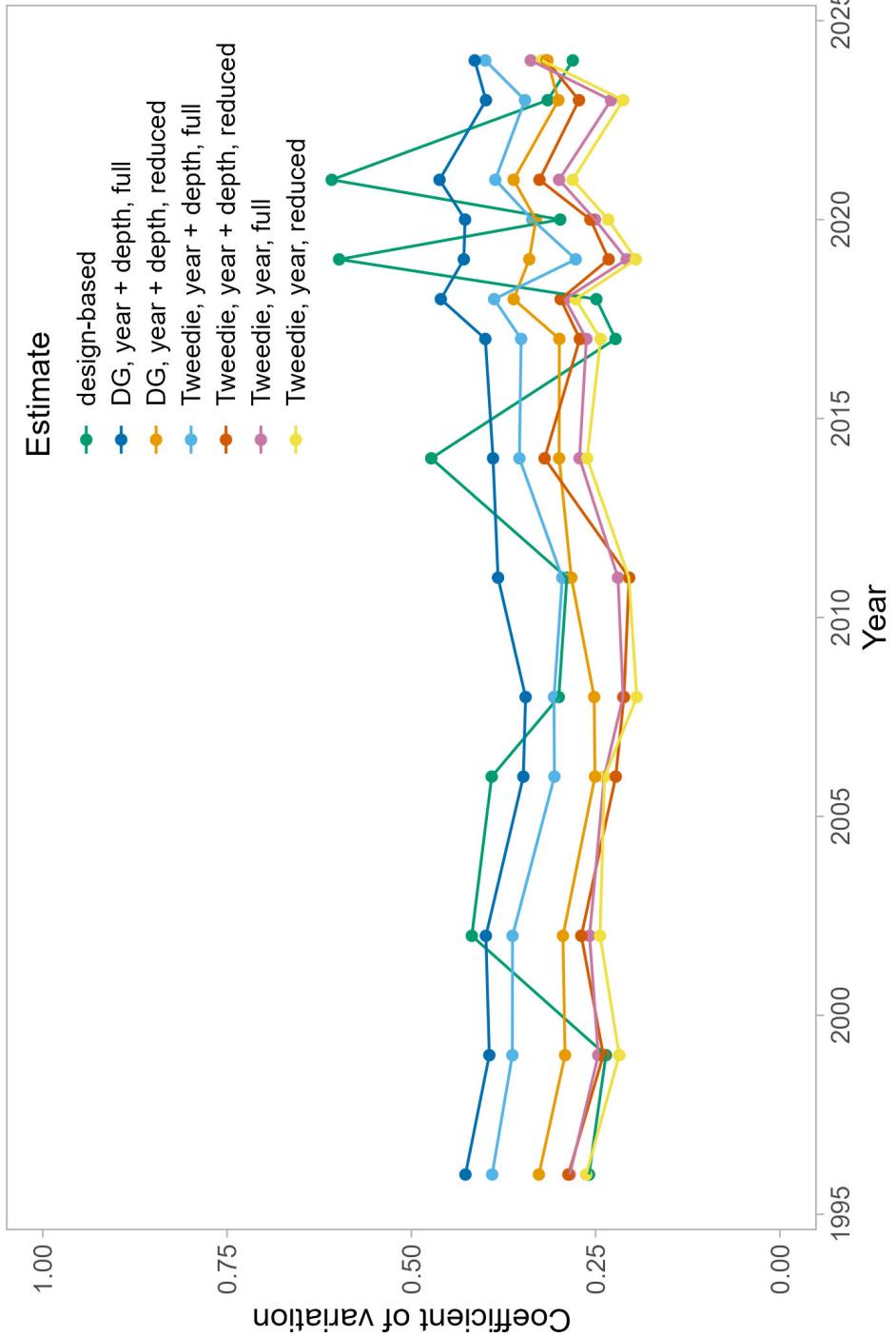
# Indices: ADF&G survey

ADF&G trawl survey



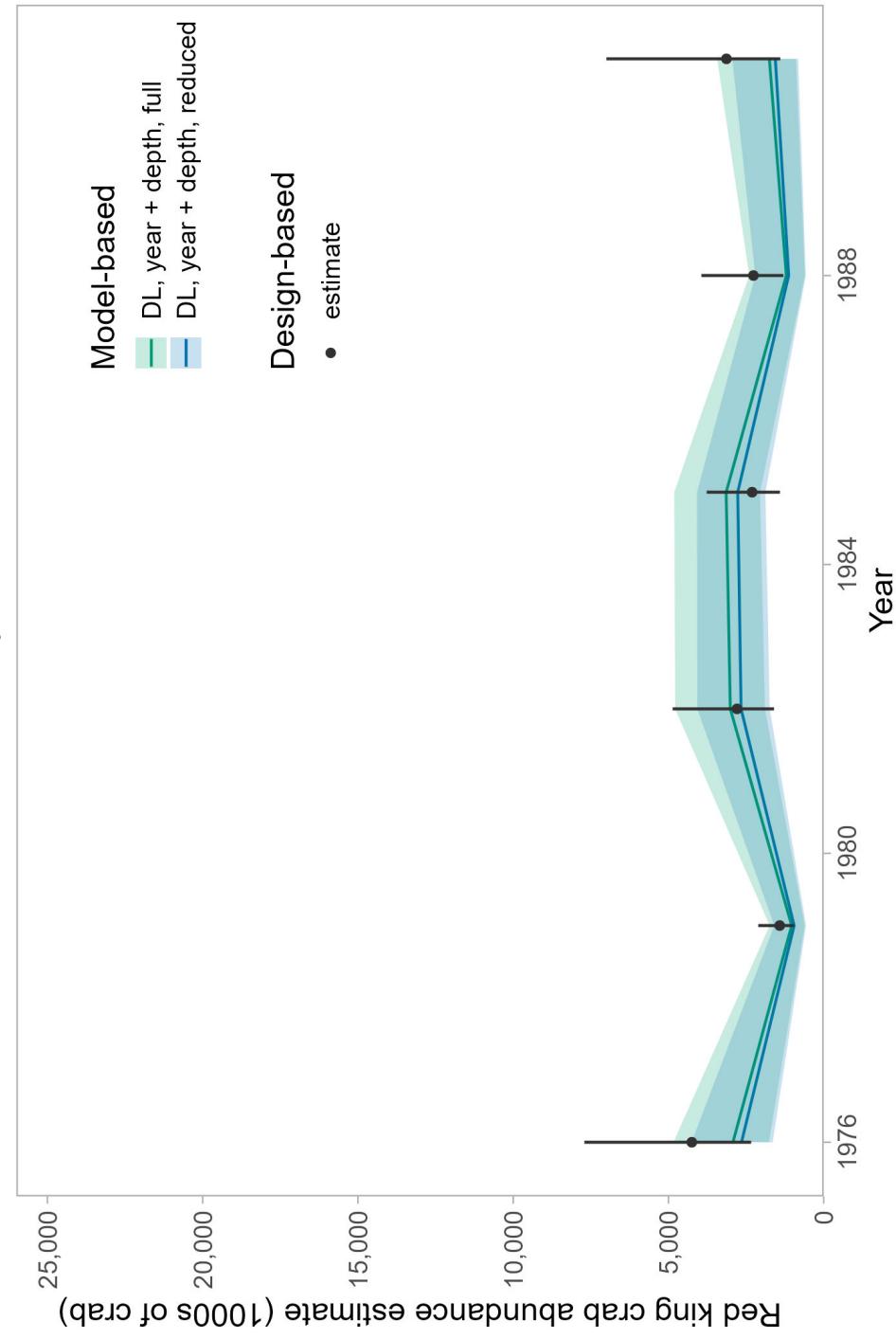
# Index CV's: ADF&G survey

ADF&G trawl survey



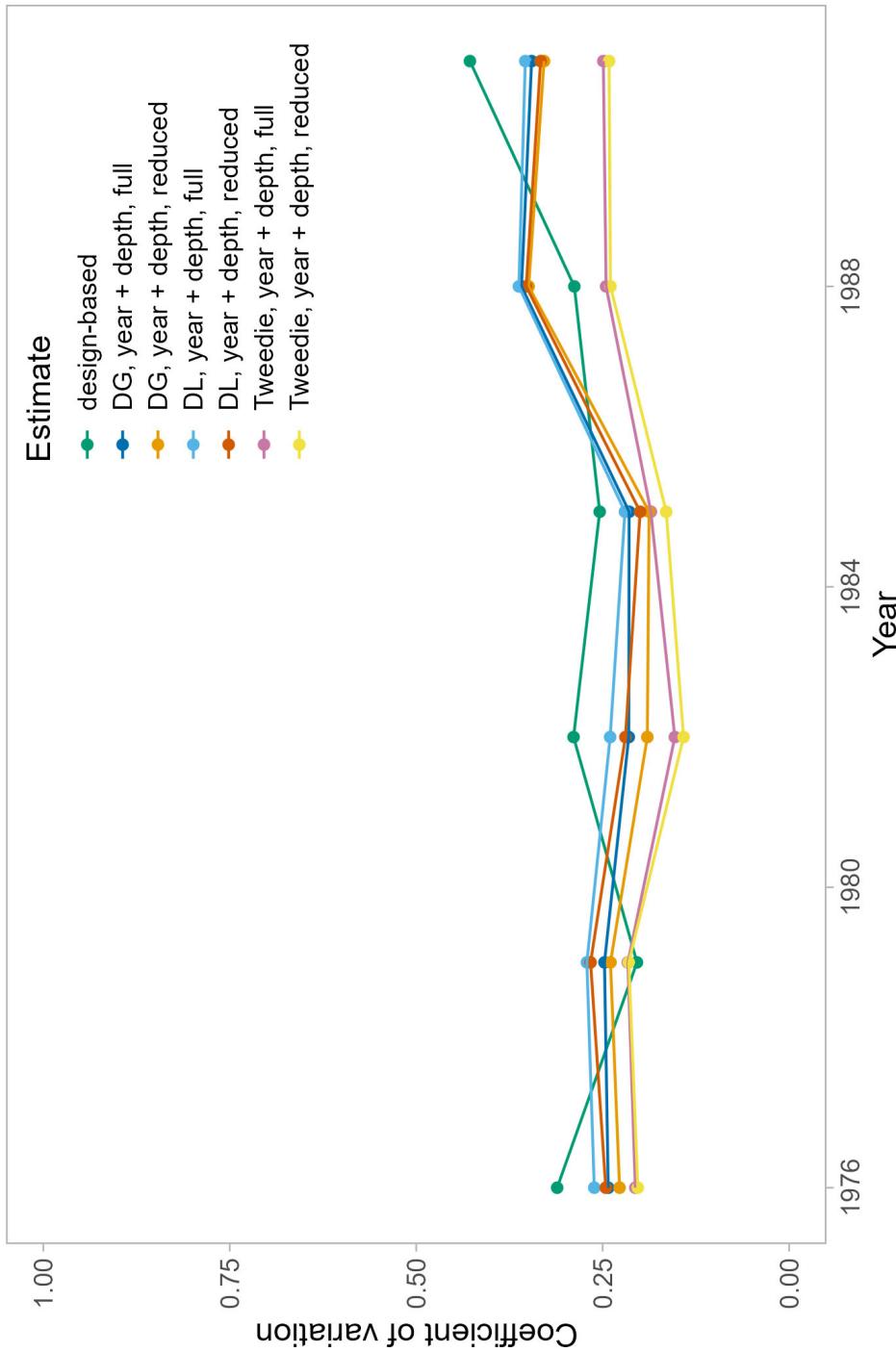
# Indices: NOAA Norton Sound survey

NOAA Norton Sound trawl survey



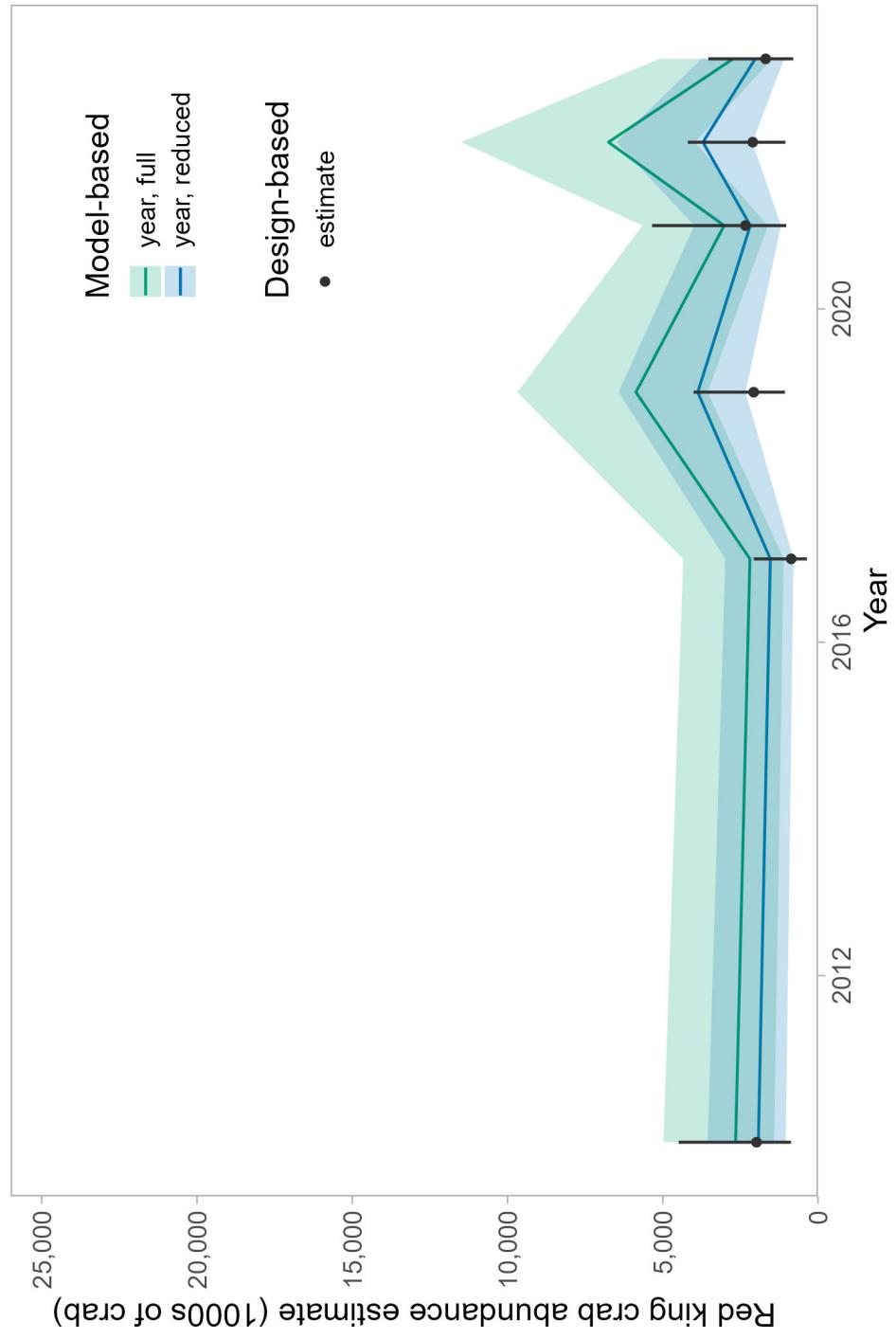
# Index CV's: NOAA Norton Sound survey

NOAA Norton Sound trawl survey



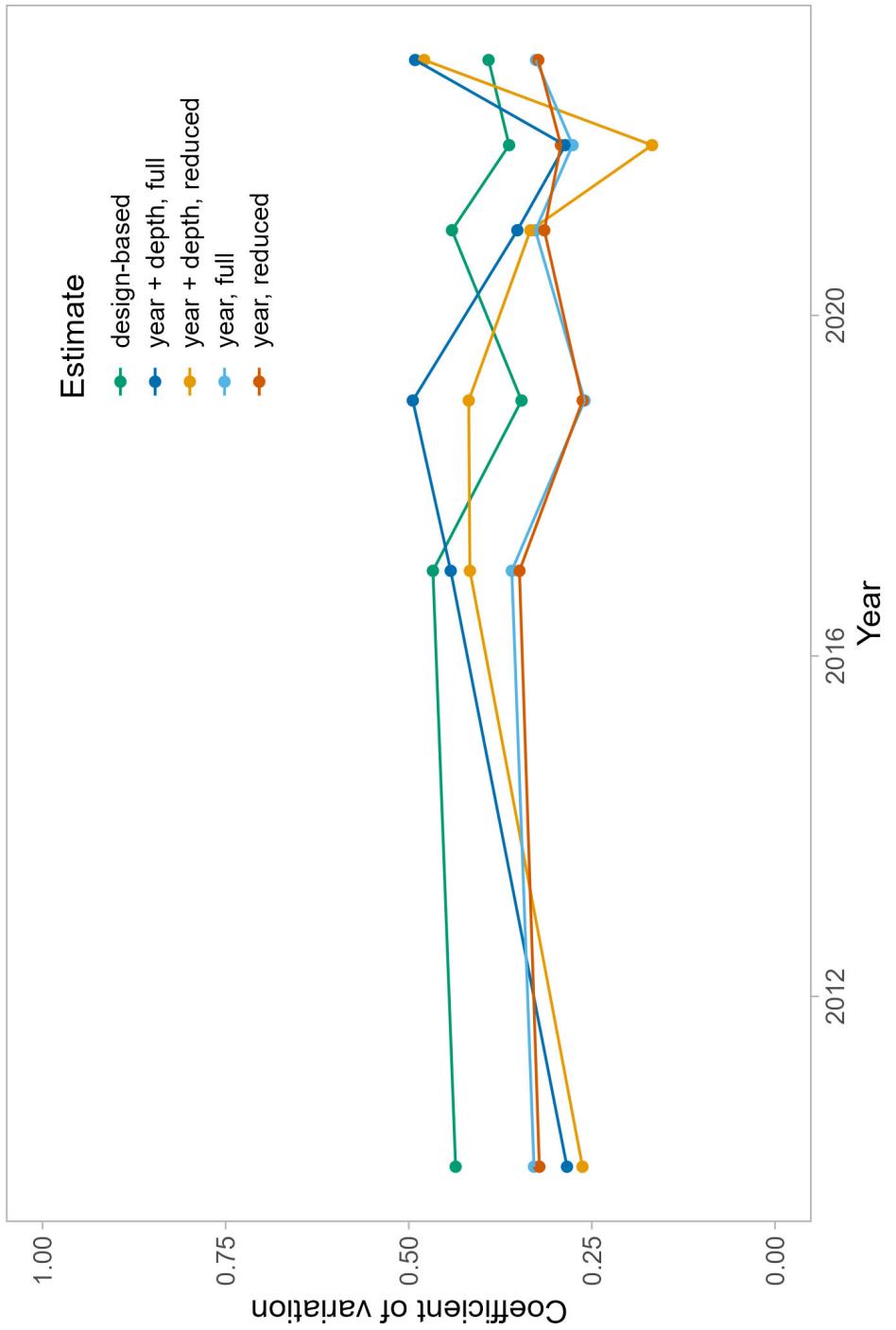
# Indices: NOAA NBS survey

NOAA Northern Bering Sea trawl survey



# Index CV's: NOAA NBS survey

NOAA Northern Bering Sea trawl survey



# Model- vs. design-based indices

Survey	Model	Effects	Prediction grid	Ratio	TimeOut	Magnitude	CV Ratio
ADF&G	delta-gamma	year + depth	full	1.89	0.50	11.46	1.15
ADF&G	delta-gamma	year + depth	reduced	1.22	0.21	3.64	0.87
NOAA NS	delta-lognormal	year + depth	full	0.81	0.17	-0.47	0.96
NOAA NS	delta-lognormal	year + depth	reduced	0.73	0.33	-0.83	0.91
NOAA NBS	Tweedie	year	full	2.10	0.50	5.58	0.77
NOAA NBS	Tweedie	year	reduced	1.38	0.00	0.00	0.76

Ratio: time series mean of MBI / time series mean of DBI

TimeOut: proportion of years with MBI outside 95% CI of DBI ("outside years")

Magnitude: sum across outside years of magnitude of MBI relative to DBI

CVRatio: time series mean of MBI CV / DBI CV



# Model- vs. design-based indices

Takeaways:

- model-based indices are standardized and use consistent prediction areas
- model-based index abundance estimates are higher than design-based for ADF&G and NOAA NBS surveys but lower for NOAA NS survey
- model-based index abundance estimates are higher when predicting over the full than the reduced area
- CV's are relatively similar for model-based and design-based indices, and actually higher for model-based for ADF&G survey index predicting over the full area



# Future work and feedback

SSC and CPT concerns:

- consistency of area over which abundance is estimated
- sufficient diagnostics for evaluating spatiotemporal models

Next steps:

- use model-based indices in stock assessment models
- combine survey data to produce a single index of abundance
- develop model-based indices for survey size comps

Feedback: which prediction area to use? (stock identification)



Thanks!



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